

1 **Ultimate behaviour and serviceability analysis of stainless steel reinforced concrete beams**

2 Musab Rabi^{a, b}, K.A. Cashell^a, Rabee Shamass^c

3 ^a Dept of Civil Engineering, Jerash University, Jordan

4 ^b Dept of Civil and Environmental Engineering, Brunel University London, UK

5 ^c Division of Civil and Building Services Engineering, School of Build Environment and Architecture,
6 London South Bank University, UK

7 8 Abstract

9 Stainless steel reinforcement has become a very attractive option for reinforced concrete structures
10 owing to its distinctive properties including outstanding corrosion resistance, excellent fire behaviour,
11 long life cycle as well as low maintenance requirements. Additionally, stainless steel reinforcement
12 offers exceptional ductility and strain hardening characteristics compared with other common materials,
13 which are very desirable in design to avoid sudden collapse. However, most global design standards do
14 not incorporate an appropriate design approach for reinforced concrete members with stainless steel.
15 The substantial strain hardening characteristics of stainless steel are typically not represented in
16 standardised material models and therefore this attractive characteristic is not exploited in design
17 resulting in structural and economic inefficiencies. Hence, the aim of this paper is to propose and
18 validate a new deformation-based design approach for stainless steel reinforced concrete beams based
19 on the continuous strength method, with reference to the current design rules provided in Eurocode 2.
20 This approach is shown to be an effective design tool that exploits the distinctive characteristics of
21 stainless steel reinforcement in an efficient and reliable manner. It is shown to provide a more efficient
22 design with less over-conservatism and greater accuracy, compared with other methods. A
23 comprehensive parametric study is conducted using Abaqus software to study the influence that various
24 geometric and material properties have on the capacity of the members. Moreover, the serviceability
25 limit state is also explored through a detailed analysis of the deflection behaviour.

26 Highlights

- 27 • The behaviour of stainless steel reinforced concrete beams is investigated.
- 28 • A full and simplified version of a deformation-based design method is proposed and examined
29 herein with reference to the current design rules in Eurocode 2.
- 30 • A comprehensive parametric study is conducted to study the most influential parameters.
- 31 • The serviceability limit state is also explored through a detailed analysis of the deflection
32 behaviour.

33

34 Keywords: Stainless steel; Reinforced concrete; Beams; Continuous strength method, Numerical
35 analysis; Abaqus; Deflections; Eurocode 2.

36 1. Introduction

37 Stainless steel is an exceptional construction material that has recently become an attractive choice for
38 reinforced concrete structures owing principally to its excellent corrosion resistance and durability. In
39 addition, stainless steel exhibits favourable mechanical properties, great ductility, a long life cycle and
40 is fully recyclable. These distinctive characteristics mainly depend on the constituent elements of the
41 stainless steel alloys and thus it is essential to carefully select the appropriate grade for each particular
42 application. Stainless steels are defined as a group of corrosion resistant, alloying steels which possess
43 a minimum chromium content of 10.5% and a maximum carbon content of 1.2%. There are five main
44 categories of stainless steel, and each grade is classified according to its metallurgical structure: (1)
45 austenitic, (2) ferritic, (3) duplex, (4) martensitic and (5) precipitation hardened stainless steel [1].

46 The durability, resilience and efficiency of structures and infrastructure are highly topical at the current
47 time, especially following the Polcevera Viaduct tragedy in Italy 2018 [2]. Whilst there are ever-
48 increasing demands for civil engineering structures and infrastructure to be more durable, there are also
49 significant pressures to achieve long service periods without requiring rehabilitative or remedial works,
50 to be more efficient in terms of material usage, and to be more resilient to both natural and man-made
51 environments and scenarios. It is estimated that Western Europe spends around €5 billion annually on

52 repairing corroding concrete infrastructure [3], with a corresponding figure of \$8.3 billion for the United
53 States [4]. In addition, there can be significant further indirect costs associated with important
54 infrastructure being out-of-service. In this context, there is a clear motivation for improving the life of
55 reinforced concrete (RC) elements, especially for those in sensitive or harsh environments such as
56 bridges, tunnels and marine structures.

57 For structures subjected to aggressive conditions and reinforced with traditional carbon steel, corrosion
58 is difficult to avoid. The typical approaches for improving durability are to control the alkalinity of
59 concrete, increase the depth of concrete cover or use cement inhibitors or reinforcement coating
60 materials. However, in harsh or exposed environments, all of these measures may not be sufficient to
61 prevent the development of unacceptable levels of corrosion in which case, the use of stainless steel
62 reinforcement may provide an ideal solution. Stainless steel reinforcement may even result in an
63 increase in the life time of structures, and a significant reduction in the cost of expensive inspections
64 and rehabilitation works.

65 There are a number of reasons that stainless steel reinforcement is not more commonly employed in
66 every-day reinforced concrete structures. Firstly, there is a common perception amongst engineers that
67 stainless steel reinforcement is prohibitively expensive, particularly in terms of their initial cost, and
68 the full life cycle costs are not always considered when selecting the materials [5]. Secondly, there is a
69 lack of design guidance and performance data available in the public domain, mainly owing to this
70 being a relatively new topic in structural engineering terms. Given the high initial cost of stainless steel,
71 it is crucial that efficient design rules which exploit the advantageous and distinctive properties of the
72 material should be made available. However, most global design standards [6] do not incorporate an
73 efficient design approach for RC members with stainless steel. In particular, they generally include an
74 elastic-plastic material model for idealising the reinforcement behaviour, which does not exploit the
75 significant strain hardening and high ductility characteristics of stainless steel. Although, this
76 assumption could be acceptable for the design of traditional concrete structures reinforced with carbon
77 steel, it results in inaccurate predictions for stainless steel RC members since stainless steel exhibits a

78 nonlinear response from an early stage followed by significant strain hardening. Therefore, designing
79 RC structures with stainless steel using the current design rules, is neither efficient nor accurate.

80 There has been extensive research in recent years into the behaviour of structural stainless steel
81 including retrofitting applications [7, 8], the flexural behaviour [9, 10], compressive response [11, 12]
82 and the mechanical characteristics [13-15]. However, most of this research has focused on bare stainless
83 steel sections, rather than stainless steel reinforced concrete which is the main concern of the current
84 paper. There has been some research in recent years into the flexural behaviour of reinforced concrete
85 beams which were repaired using a hybrid system of stainless steel rebars and CFRP sheets [16].
86 Recently, Hasan et al. has investigated a series of geographical locations which are suitable for using
87 stainless steel rebars in reinforced concrete girder bridges using a life cycle costing (LCC) based system
88 [17]. However, the current paper is concerned with the behaviour of stainless steel reinforced concrete
89 flexural members, and the principal objective is to propose and validate an alternative design method
90 to those available in the current design standards. The proposed method is based on the increasingly
91 popular continuous strength method (CSM), which is a deformation-based design approach that
92 harnesses the advantages of material strain hardening. The CSM was originally developed for stainless
93 steel structural members with non-slender cross-sections [18] and has been developed many times over
94 the last 15 years [19-21]. The approach has also been adapted for composite construction [22; 23] and
95 has most recently been extended to include RC beams reinforced with stainless steel [24]. This paper
96 presents the results of a comprehensive parametric study in which the most influential geometric and
97 material properties are examined, in terms of the structural performance of stainless steel RC members.
98 Building on previous work, the CSM approach is examined over an extensive range of parameters, with
99 emphasis given to the geometry of the section, reinforcement ratio and also deflections, in the context
100 of the nonlinear stress-strain behaviour.

101 2. Design of stainless steel reinforced concrete beams

102 Two versions of the continuous strength method (CSM) have been developed for the design of stainless
103 steel reinforced concrete beams, accounting for the distinct material properties of the reinforcement.

104 The full analytical model (hereafter referred to as AM) considers the full stress-strain response of
 105 stainless steel whereas the simplified model (SM) considers simplified material model for the stainless
 106 steel which is a bilinear elastic-linear strain hardening relationship; these are both presented in Fig. 1.
 107 The full details of these models are available in [24], and a concise overview is presented herein.

108 2.1. Material model

109 The constitutive behaviour of stainless steel is noticeably different from that of carbon steel, as shown
 110 in Fig. 2. Stainless steel exhibits a nonlinear response from the beginning, does not have a clearly
 111 defined yield point and develops significant strain hardening and ductility. In contrast, carbon steel
 112 exhibits a linear relationship in the elastic range with a well-defined yield point, followed by a
 113 moderate degree of stain hardening. Hence, the 0.2% proof stress ($\sigma_{0.2}$) is typically used to identify the
 114 yield limit in stainless steel.

115 The modified Ramberg-Osgood stainless steel material model developed by Mirambell and Real [14]
 116 and Rasmussen [15], which is an extension of the original version [13], is employed to represent the
 117 stainless steel constitutive stress-strain relationship. This material model was developed on the basis of
 118 empirical data and has been adopted in an extensive number of research papers [18-25]. It includes the
 119 two expressions presented in Eqs. 1 and 2, for the elastic and non-elastic stages of the behaviour,
 120 respectively:

$$\varepsilon = \frac{\sigma}{E} + 0.002 \left(\frac{\sigma}{\sigma_{0.2}} \right)^n \quad \text{for } \sigma \leq \sigma_{0.2} \quad (1)$$

$$\varepsilon = \varepsilon_{0.2} + \frac{\sigma - \sigma_{0.2}}{E_2} + \left(\varepsilon_u - \varepsilon_{0.2} - \frac{\sigma_u - \sigma_{0.2}}{E_2} \right) \left(\frac{\sigma - \sigma_{0.2}}{\sigma_u - \sigma_{0.2}} \right)^m \quad \text{for } \sigma_{0.2} < \sigma \leq \sigma_u \quad (2)$$

121 In these expressions, ε and σ are the engineering strain and stress, respectively; E is the elastic modulus;
 122 E_2 is the tangent modulus at the 0.2% proof stress; σ_u and ε_u are the ultimate stress and corresponding
 123 strain, respectively; $\varepsilon_{0.2}$ is the strain corresponding to $\sigma_{0.2}$; and n and m are material constants related to
 124 the strain hardening behaviour. It is noteworthy that all equations in this paper are applied using SI
 125 units, unless stated otherwise.

126 However, in order to implement the material model in conjunction with the design method, it is
 127 necessary to determine the stress as a function of strain. Therefore, the inversion relationship proposed
 128 by [26] for the full stress-strain relationship of stainless steel is employed, as presented in Eqs. 3 and 4.

$$\sigma_1(\varepsilon) = \sigma_{0.2} \frac{r \left(\frac{\varepsilon}{\varepsilon_{0.2}} \right)}{1 + (r-1) \left(\frac{\varepsilon}{\varepsilon_{0.2}} \right)^p} \quad \text{for } \varepsilon \leq \varepsilon_{0.2} \quad (3)$$

129

$$\sigma_2(\varepsilon) = \sigma_{0.2} \left[1 + \frac{r_2 \left[\frac{\varepsilon}{\varepsilon_{0.2}} - 1 \right]}{1 + (r^* - 1) \left(\frac{\frac{\varepsilon}{\varepsilon_{0.2}} - 1}{\frac{\varepsilon_u}{\varepsilon_{0.2}} - 1} \right)^{p^*}} \right] \quad \text{for } \varepsilon > \varepsilon_{0.2} \quad (4)$$

130 where the material parameters are:

$$\varepsilon_{0.2} = \frac{\sigma_{0.2}}{E} + 0.002$$

$$r = \frac{E \varepsilon_{0.2}}{\sigma_{0.2}}$$

$$E_2 = \frac{E}{1 + 0.002 n/e}$$

$$p = r \frac{1 - r_2}{r - 1}$$

$$e = \frac{\sigma_{0.2}}{E}$$

$$m = 1 + 3.5 \frac{\sigma_{0.2}}{\sigma_u}$$

$$\sigma_u = \sigma_{0.2} \frac{1 - 0.0375(n - 5)}{0.2 + 185e}$$

$$E_u = \frac{E_2}{1 + (r^* - 1)m}$$

$$r_2 = \frac{E_2 \varepsilon_{0.2}}{\sigma_{0.2}}$$

$$r_u = \frac{E_u (\varepsilon_u - \varepsilon_{0.2})}{\sigma_u - \sigma_{0.2}}$$

$$\varepsilon_u = \min \left(1 - \frac{\sigma_{0.2}}{\sigma_u}, A \right)$$

$$p^* = r^* \frac{1 - r_u}{r^* - 1}$$

$$r^* = \frac{E_2 (\varepsilon_u - \varepsilon_{0.2})}{\sigma_u - \sigma_{0.2}}$$

$$n = \frac{\ln(20)}{\ln(\sigma_{0.2}/\sigma_{0.01})}$$

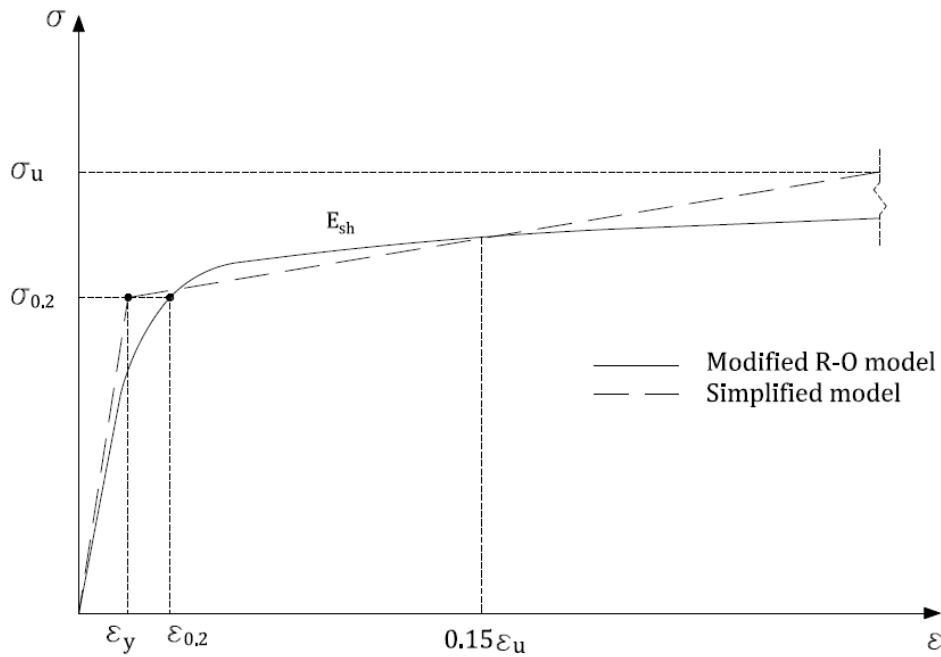
131 In these expressions, A is the stainless steel elongation; E_u is the slope of the stress-strain curve at ε_u ;
 132 and r , r_2 , r^* , r_u , p and p^* are parameters that need to be determined.

133 For the simplified design model, a bilinear stress-strain relationship is employed to avoid the complexity
 134 of nonlinear equations, as presented in Eqs. 5 and 6, and depicted in Fig. 1. In this approach, the yield
 135 point is identified as the 0.2% proof stress ($\sigma_{0.2}$) and the corresponding yield strain (ϵ_y) is determined
 136 by dividing this value by the elastic modulus, E. The difference between ϵ_y and $\epsilon_{0.2}$ as employed in the
 137 full analytical model are demonstrated in Fig. 1. The slope of the strain hardening region (E_{sh}) is
 138 obtained from the line passing through the yield ($\epsilon_y, \sigma_{0.2}$) and ultimate ($C_2\epsilon_u, \sigma_u$) points, as defined in
 139 Eq. 7. It has been found that a value of 0.15 is an appropriate value for the constant C_2 [24].

$$\sigma = E\epsilon \quad \epsilon \leq \epsilon_y \quad (5)$$

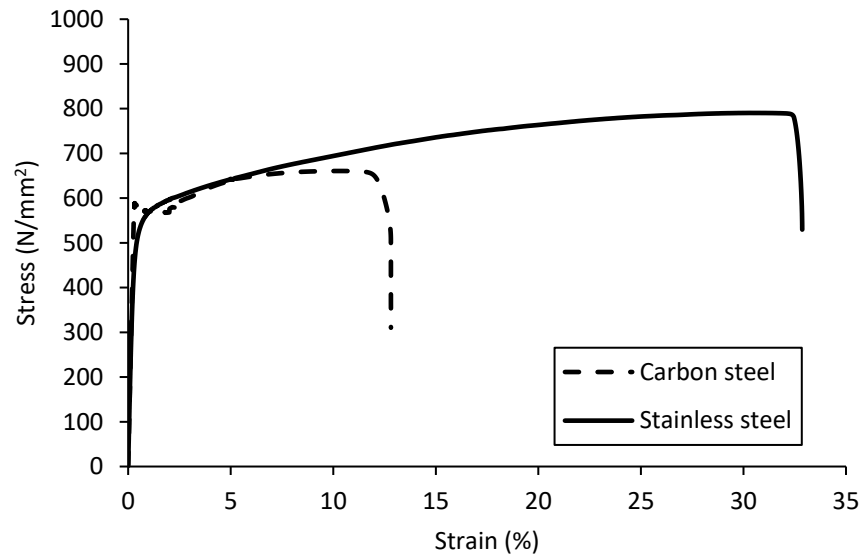
$$\sigma = \sigma_{0.2} + E_{sh}(\epsilon - \epsilon_y) \quad \epsilon > \epsilon_y \quad (6)$$

$$E_{sh} = \frac{\sigma_u - \sigma_{0.2}}{C_2\epsilon_u - \epsilon_y} \quad (7)$$



140

141 Fig. 1: The simplified and modified Ramberg-Osgood material models for stainless steel.



142

143 Fig. 2: Stress-strain constitutive response for stainless steel grade 1.4301 and carbon steel, with
 144 diameter of 10 mm [27].

145 **2.2. Analytical models**

146 The plastic bending moment capacity of the stainless steel reinforced concrete beam is obtained using
 147 either the full or simplified material models discussed in the previous section. In both of these
 148 approaches, the internal tensile and compressive forces are equated, assuming that the cross-section is
 149 in equilibrium. The internal forces are determined based on the stainless steel stress-strain material
 150 model and the equivalent rectangular compressive stress distribution in the concrete, together with the
 151 strain distribution in the section.

152 There are two possible cases for calculating the bending moment capacity of the section using the full
 153 and simplified material models. Case 1 is when the tensile strain of the reinforcement is less than the
 154 total strain corresponding to $\sigma_{0.2}$ (i.e. $\epsilon \leq \epsilon_{0.2}$ in the case of full material model and $\epsilon \leq \epsilon_y$ for the
 155 simplified material model) and Case 2 is when the tensile strain of the reinforcement is greater than the
 156 total strain corresponding to $\sigma_{0.2}$ (i.e. $\epsilon > \epsilon_{0.2}$ for the full material model and $\epsilon > \epsilon_y$ in the case of the
 157 simplified material model).

158 The stress in the reinforcement at failure of the beam is determined from the corresponding strain which
 159 is determined based on the strain distribution in the section, as follows:

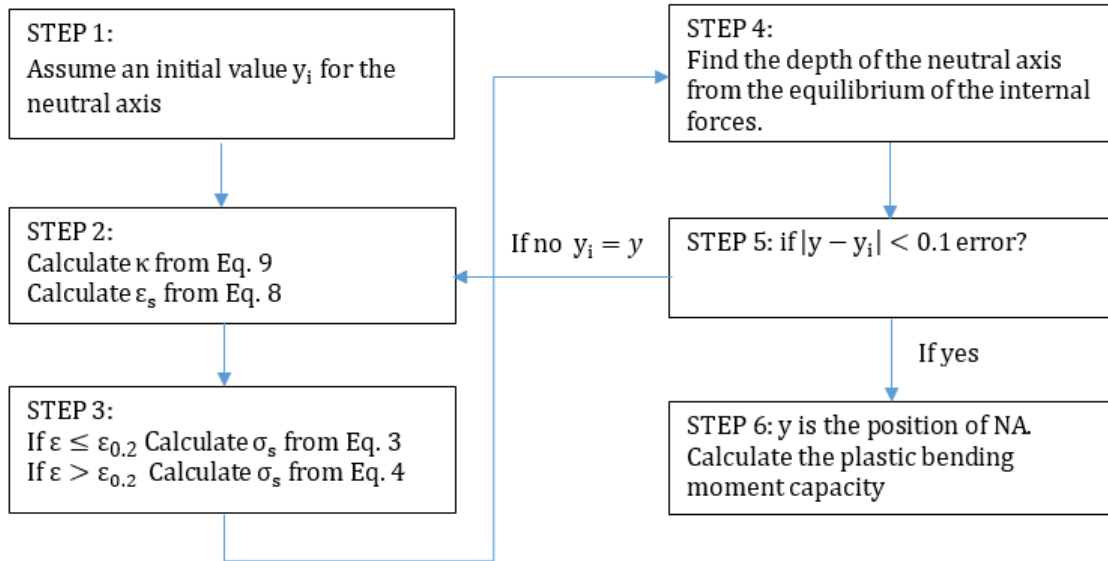
$$\varepsilon = \kappa(d - y) \quad (8)$$

$$\kappa = \min(\kappa_{su}, \kappa_{cu}) \quad (9)$$

160 In these expressions, d is the depth of the reinforcement in the section from the top of the beam, κ is the
161 ultimate curvature of the section, and κ_{su} and κ_{cu} are the limiting curvatures for stainless steel and
162 concrete failures, respectively. There are two possible failure modes of the section, either crushing of
163 the concrete (i.e. when $\kappa_{su} > \kappa_{cu}$) or by rupture of the reinforcement ($\kappa_{su} < \kappa_{cu}$). Because of the brittle
164 nature of concrete and the high ductility of stainless steel, the failure mode of the section is dominated
165 by crushing of the concrete in most cases. The values of κ_{su} and κ_{cu} are determined as:

$$\begin{aligned} \kappa_{su} &= \frac{\varepsilon_u}{d - y} \\ \kappa_{cu} &= \frac{\varepsilon_{cu}}{y} \end{aligned} \quad (10)$$

166 The bending moment capacity of the section is obtained by firstly establishing the stress in the
167 reinforcement and then locating the position of the neutral axis by applying equilibrium of the internal
168 forces to the cross-section of the beam. In the case of full model, this results in complex nonlinear
169 equations that require an iterative solution method whereas the simplified model provides a straight
170 forward solution procedure. The full solution procedures for both methods are discussed in more detail
171 in [24]. A flow chart presenting the full procedure for determining the neutral axis and the plastic
172 bending moment capacity is given in Fig. 3.



173

174 Fig. 3: Flow chart of the solution procedure for a singly reinforced concrete beam.

175 3. Numerical model

176 A finite element (FE) model has been developed using the Abaqus software [28] to simulate the
 177 behaviour of a stainless steel RC beam, with the aim of using it to examine the proposed analytical
 178 methods discussed in the previous section. This was shown to accurately predict the behaviour of
 179 reinforced concrete beams in terms of bending moment capacity, initial bending stiffness and crack
 180 propagation and patterns [24]. A similar approach is utilised herein to investigate the effect of beams
 181 geometries and materials properties of concrete and stainless steel on the structural behaviour of
 182 stainless steel RC beams, deflection at service moment and to further validate the proposed simplified
 183 model for the flexural capacity of stainless steel RC beams. In addition, in the current paper, the model
 184 is employed to conduct a detailed study into the deflection behaviour, which has not been previously
 185 considered.

186 The FE model is developed using an implicit dynamic solution procedure for quasi-static behaviour,
 187 which is able to achieve numerical convergence despite the nonlinearities of the behaviour. In the
 188 model, the concrete elements are represented using 3D eight-node hexahedral elements whereas the
 189 reinforcement is simulated using 2-node beam elements available in the Abaqus library [28]. The

190 reinforcement is embedded in the concrete and the translational degrees of freedom at each node of the
 191 reinforcement are constrained to the interpolated values of the corresponding degrees of freedom of the
 192 concrete element.

193 In terms of the materials, the modified Ramberg-Osgood material model described previously in Eqs.
 194 1 and 2 is implemented to represent the behaviour of the stainless steel reinforcement. On the other
 195 hand, the nonlinear concrete behaviour in compression is modelled using Eq. 11, as given in Eurocode 2
 196 [6]:

$$\sigma_c = \left(\frac{k\eta - \eta^2}{1 + (k-2)\eta} \right) f_{cm} \quad (11)$$

197 where:

$$k = 1.05 E_c \frac{\varepsilon_{c1}}{f_{cm}} \quad f_{cm} = f_{ck} + 8$$

$$\eta = \frac{\varepsilon_c}{\varepsilon_{c1}} \quad \varepsilon_{c1} (\%) = 0.7 (f_{cm})^{0.31} \leq 2.8$$

$$E_c = 22000 (0.1 f_{cm})^{0.3}$$

198 In these expressions, σ_c is the concrete compressive stress; f_{cm} and f_{ck} are the mean and characteristic
 199 values of the concrete cylinder compressive strength, respectively; ε_{c1} is the strain at the peak stress of
 200 the concrete while ε_{cu} is the ultimate strain of concrete, which is taken as 0.0035; and E_c is the Young's
 201 modulus of concrete.

202 The tensile stress-strain behaviour of concrete is modelled using Eq. 12, which was proposed by [29],
 203 and provides an accurate post-failure tensile response compared with linear or bi-linear relationships:

$$\begin{aligned} \sigma_t &= E_c \varepsilon_t & \text{if } \varepsilon_t \leq \varepsilon_{cr} \\ \sigma_t &= f_t \left(\frac{\varepsilon_{cr}}{\varepsilon_t} \right)^{0.4} & \text{if } \varepsilon_t > \varepsilon_{cr} \end{aligned} \quad (12)$$

204 In these expressions, ε_t is the concrete tensile strain corresponding to the tensile stress (σ_t) and ε_{cr} is
 205 the tensile cracking strain corresponding to the tensile strength of concrete (f_t), determined as:

$$f_t = 0.3(f_{ck})^{2/3} \quad (13)$$

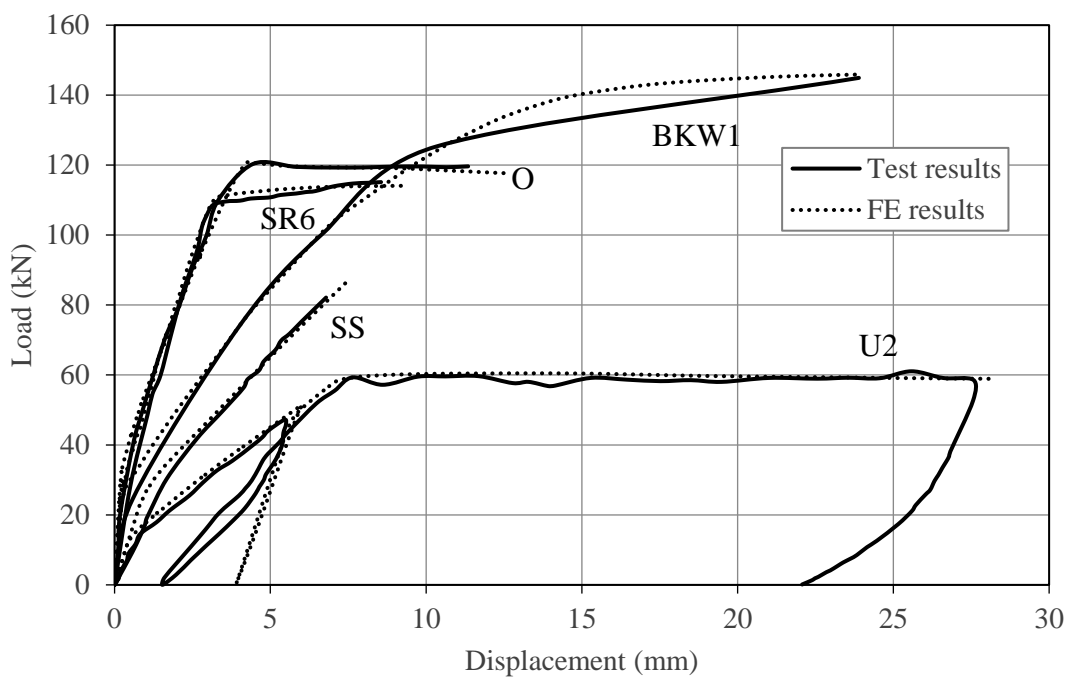
206 3.1. Failure criteria

207 In the numerical analysis, it is typically assumed that ultimate failure of a normally reinforced concrete
208 beam occurs when the outer fibre of the concrete in compression reaches the ultimate crushing strain
209 (usually taken as 0.003 or 0.0035). This is likely to occur when the reinforcement material exhibits
210 elastic perfectly-plastic stress-strain properties, because the compressive strain in the concrete at the top
211 surface is reached after the reinforcement yields so the steel no longer contributes towards the ultimate
212 bearing capacity of the section. However, this behaviour is different when the reinforcement is made
213 from stainless steel rather than carbon steel, owing to the significant levels of strain hardening and
214 ductility in the stainless steel, and the lack of a distinct yield point. Even when the concrete reaches the
215 crushing strain at the top surface, the stainless steel reinforcement is still contributing towards the
216 ultimate bearing capacity of the section. In addition, it is difficult to predict exactly when the concrete
217 has crushed and therefore, it is necessary to make an assumption regarding the exact point at which the
218 concrete is assumed to have failed (e.g. once the first node at the top surface reaches the assumed strain
219 limit or all nodes on the top surface). In order to avoid this uncertainty, in the current work the maximum
220 capacity of the section is taken at the ultimate load capacity of the section, in the same manner that this
221 is commonly determined experimentally.

222 3.2. Validation of the FE model

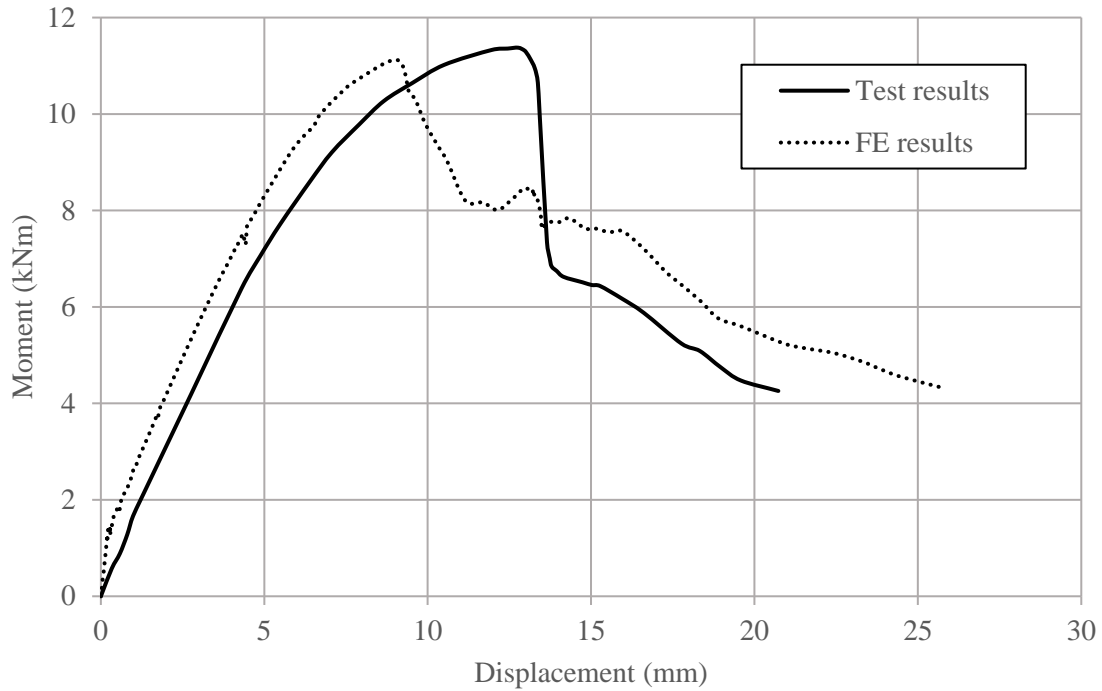
223 The FE model has been validated using six RC beams from different experimental programmes
224 available in the literature [30-35], three of which were reinforced with stainless steel reinforcement and
225 three of which had traditional carbon steel reinforcement. No further experimental data on stainless
226 steel reinforced concrete beams were available in the literature. All of the beams were tested under four-
227 point loading conditions in displacement control. The validation includes three stainless steel RC
228 beams, namely B3, SS and BKW1, and three other beams (SR6, U2 and O) reinforced with carbon steel
229 reinforcement for additional robustness. The full details of the geometry and material properties for
230 these beams are available in [24].

231 Fig. 4 shows the numerical load-displacement response for beams SS, SR6, U2, O and BKW1 in
 232 comparison with the corresponding experimental data. Fig. 5 presents the moment-displacement
 233 response for beam B3, since this is that manner that the experimental data is published [35]. It is
 234 observed that the model provides an excellent depiction of the experimental behaviour in all cases in
 235 terms initial stiffness, cracking point, and ultimate strength. It is found that the model slightly over-
 236 estimates the initial stiffness of the beams most likely because of some localized cracking in the
 237 experiment were not captured by the numerical model.



238

239 Fig. 4: Comparison between experimental and numerical load-displacement curves for beams U2
 240 [30], O [31], SS [32], SR6 [33] and BKW1 [34].



241

242 Fig. 5: Comparison between experimental and numerical moment-displacement curves for beam B3

243

[35].

244 4. Analysis of the behaviour

245 In this section, the performance of stainless steel reinforced concrete beams with different geometric
 246 and material properties is assessed using the FE model. Moreover, the accuracy of the proposed design
 247 models is analysed against the numerical results, with reference to the current design provisions in
 248 Eurocode 2. Around 200 numerical simulations have been conducted to investigate the influence that
 249 the design parameters have on the exploitation of strain hardening and ductility of the stainless steel
 250 reinforcement in the section, including concrete strength, grade of stainless steel, geometry and
 251 reinforcement ratio. In addition, a detailed study into the influence of these parameters on the deflections
 252 and the accuracy of the Eurocode 2 provisions, is also presented.

253 All of the members in this study are assumed to be simply supported beams under four-point loading
 254 conditions and have a clear span of 3300 mm in order to avoid shear failure in the beam. Each member
 255 has two reinforcements with diameter of 12 mm, unless it is stated otherwise. The full range of
 256 parameters examined is presented in Table 1. The material data presented by [36] for these grades is

257 given in Table 2, including the n and m parameters required for application of the modified Ramberg-
 258 Osgood material model.

259 Table 1: Range of geometrical parameters included in the study.

Parameter	Range examined
Concrete grade	C20, C30, C40, C50
Grade of stainless steel reinforcement	Austenitic 1.4311, lean duplex 1.4162 and Austenitic 1.4307
Width/height (b/h) ratio of the beam	0.55 to 1
Diameter of the reinforcement	12 mm and 20 mm
Reinforcement ratio (%)	0.187 – 5.2 %

260 Table 2: Material properties of stainless steel reinforcement included in the study [36].

Stainless steel type	Grade	$\sigma_{0.2}$ (N/mm ²)	σ_u (N/mm ²)	E (kN/mm ²)	ϵ_u (%)	n	m
Austenitic	1.4311 (304LN)	480	764	202.6	38.6	4.7	4.8
Lean duplex	1.4162 (LDX2101)	682	874	199.1	20.4	5.3	5.0
Austenitic	1.4307 (304L)	562	796	210.2	30.7	4.7	4.8

261

262 4.1. Bending moment capacity predictions

263 Figs. 6, 7 and 8 present the bending moment predictions obtained from the proposed full analytical
 264 model (AM), the simplified analytical model (SM) and the numerical model (FE) as well as those
 265 obtained using the design method provided in Eurocode 2 (i.e. elastic-perfectly-plastic behaviour of the
 266 material is assumed), for beams reinforced with stainless steel grades 1.4311, 1.4162, 1.4307,

267 respectively. The results are presented in terms of bending moment versus concrete strength (f_c), to
268 highlight how this parameter influences the behaviour.

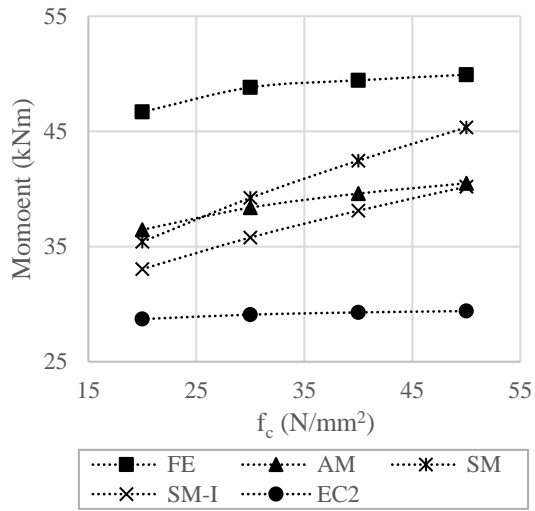
269 The figures show a good agreement between the results obtained numerically with those calculated
270 using the full proposed analytical model with average and maximum AM/FE values being -14.9% and
271 -22.3% whilst these same values obtained using the Eurocode 2 design rules (i.e. EC2/FE) are -28.3%
272 23 and -44.7%, respectively. It is noteworthy that a negative value for the AM/FE ratio indicates a
273 conservative result from the analytical model. Clearly, the Eurocode 2 design rules provide an overly
274 conservative prediction of the ultimate bending moment capacity, whereas the full analytical design
275 model provides less conservative yet accurate and reasonably realistic results. There are still some
276 disparities between the analytical and numerical results, which are most likely owing to some of the
277 simplifications in the analytical model. These include the assumption that concrete does not contribute
278 to the load carrying capacity in tension and also the idealisation of rectangular stress blocks.
279 Nevertheless, the results are better than the existing design provisions, and remain on the conservative
280 side consistently.

281 The simplified analytical model which incorporates the bilinear stress-strain curve for the stainless steel,
282 also provides conservative predictions for the bending moment capacity in most cases with the average
283 and maximum SM/FE values being -9.9% and -26.8%, respectively. It is noteworthy that the simplified
284 analytical model provides less conservative results overall compared with the full analytical model
285 mainly because the simplified material model has a greater slope in the strain hardening region. In
286 addition, in a small number of cases when beams have a relatively low b/h ratio and are made using
287 high strength concrete and grade 1.4162 stainless steel, the simplified analytical model tends to
288 overestimate the bending moment capacity compared with the numerical results, which slightly skews
289 the average and maximum SM/FE values given before. Therefore, it is necessary to recalibrate the
290 simplified method in order to achieve better agreement with full method predictions, and to provide
291 conservative predictions for all cases, as discussed in the following section.

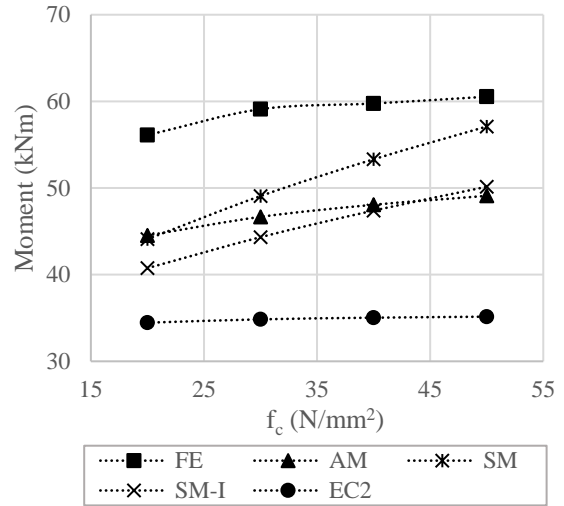
4.1.1. Proposed modifications into the simplified analytical model

In this section, the slope of the strain hardening portion of the stainless steel constitutive relationship is modified to improve the accuracy of the simplified analytical model, especially for the cases highlighted in the previous section where slightly unconservative results were obtained. This is achieved by recalibrating the C_2 parameter in Eq. 7 based on the extensive range of numerical data obtained. Since different stainless steel grades have their own mechanical properties, an optimization study for the C_2 parameter is conducted individually for each material type. Consequently, it has been found that the most accurate bending moment predictions for the full range of parameters examined in the current study are achieved using a C_2 value of 0.25 for beams with austenitic stainless steel grades 1.4311 and 1.4307, and 0.3 for beams with lean duplex stainless steel grade 1.4162. This is reasonably acceptable as a higher value of C_2 results in a lower E_{sh} value and hence lower strain hardening capacity, as is the case for lean duplex stainless steel compared with the austenitic grades.

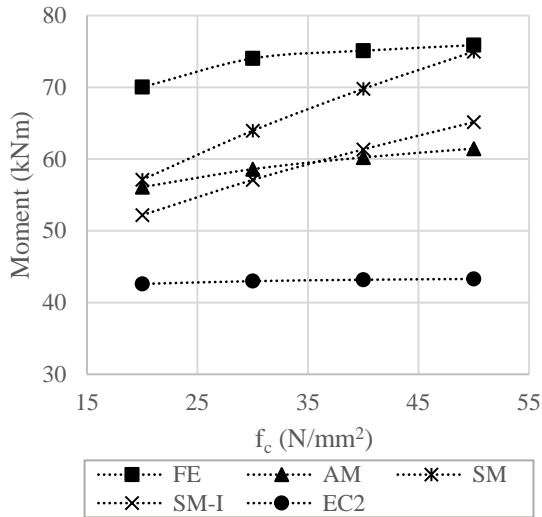
The results of the simplified analytical model predicted using the new proposed values for C_2 (denoted as SM-I) are presented in Figs. 6, 7 and 8, for beams made using grade 1.4311, 1.4162 and 1.4307 stainless steel, respectively. The figure also presents the data from the previous C_2 value of 0.15 (SM in the figures). It is observed that the simplified analytical model predictions with the newly proposed C_2 values are in excellent agreement with the predictions of the full analytical model. The average and maximum SM-I/AM ratios are -2.8% and -17.2%, respectively, whilst these same values for SM/AM are 5.9% and 34.5%, respectively. This also ensures that the simplified predictions are below that of the numerical model, for all examined cases. Therefore, the proposed values for C_2 parameter are implemented in the simplified analytical model for all the results presented in the following sections.



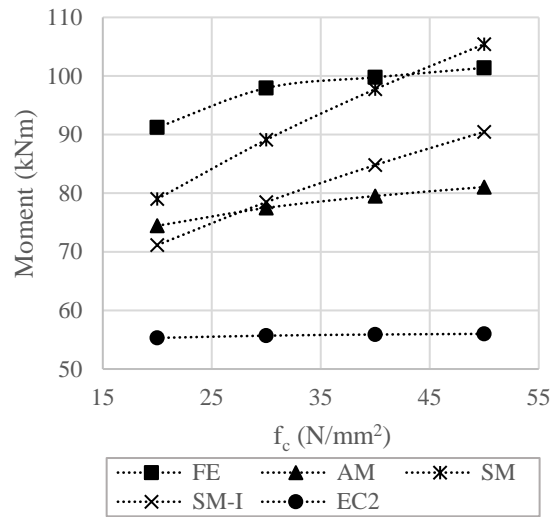
(a)



(b)



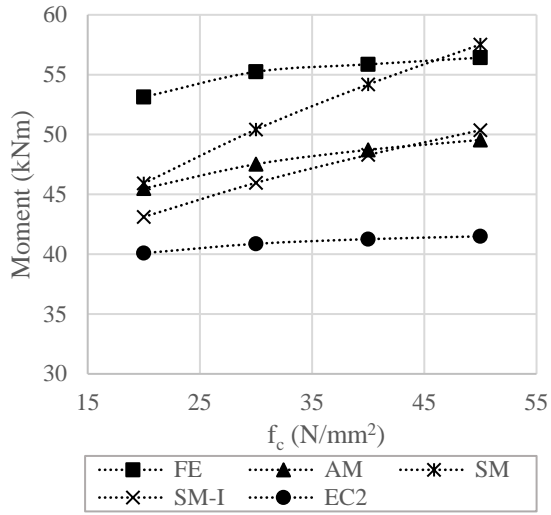
(c)



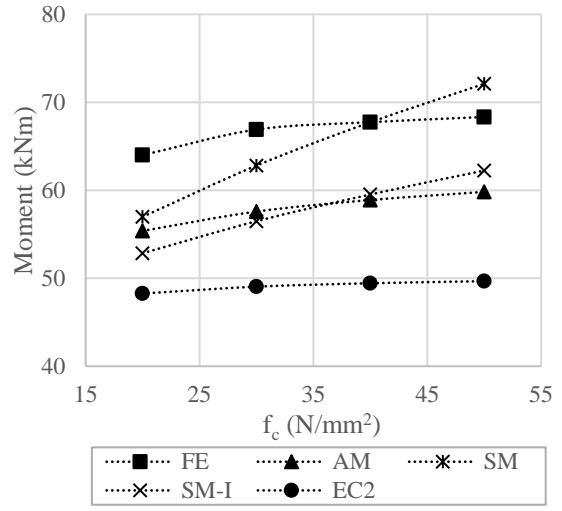
(d)

313 Fig. 6: Bending moment predictions for beams with grade 1.4311 austenitic stainless steel using a b/h

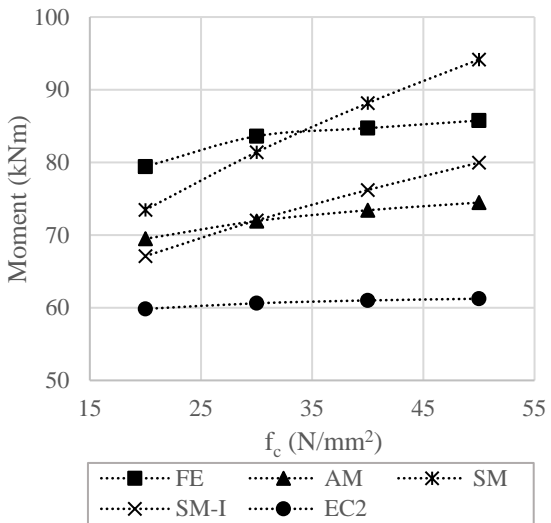
314 ratio of (a) 1.00 (b) 0.85 (c) 0.70 and (d) 0.55.



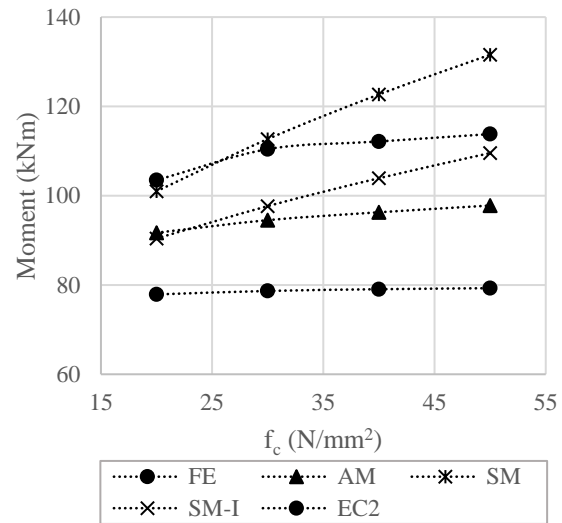
(a)



(b)

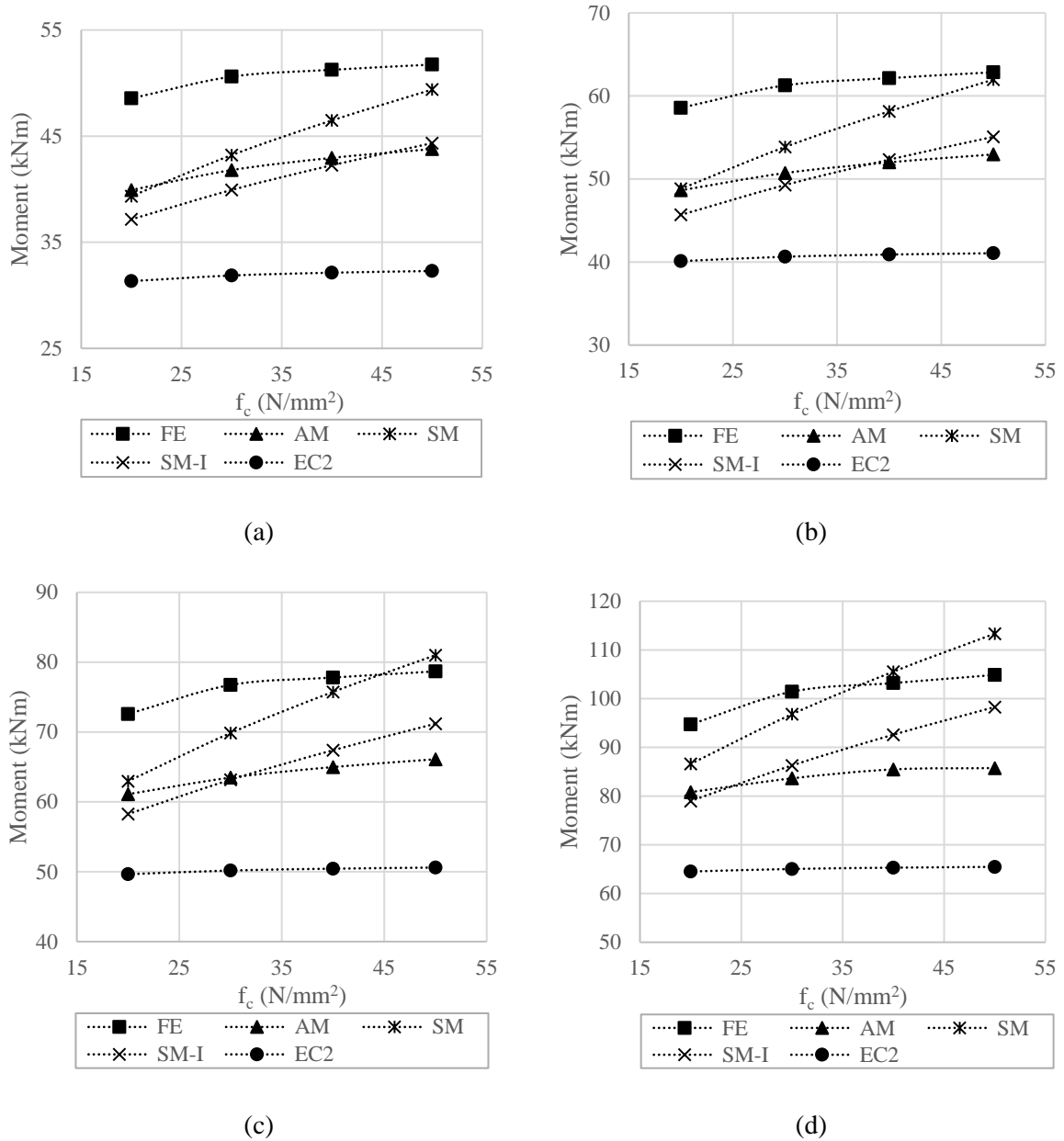


(c)



(d)

315 Fig. 7: Bending moment predictions for beams with grade 1.4162 duplex stainless steel using a b/h
 316 ratio of (a) 1.00 (b) 0.85 (c) 0.70 and (d) 0.55.



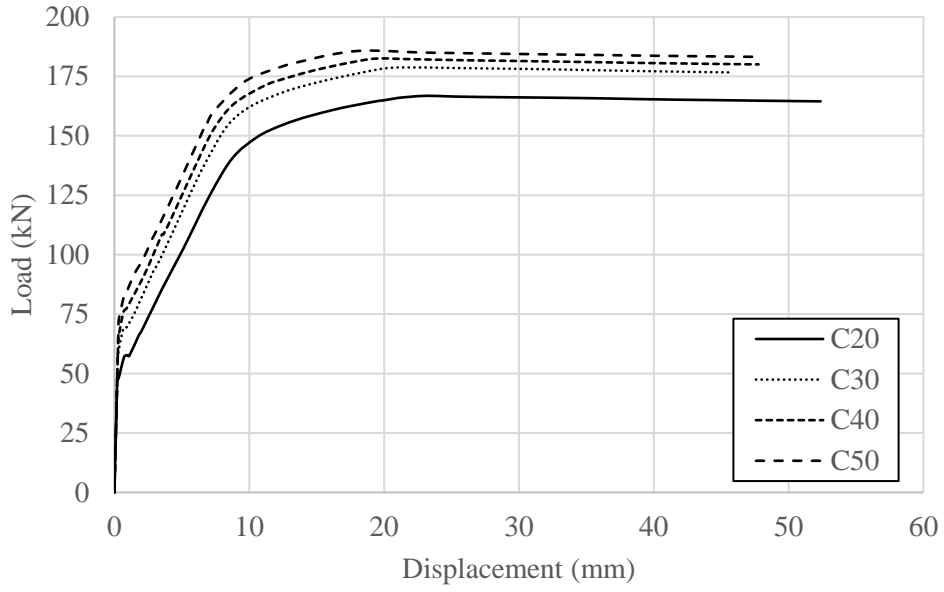
317 Fig. 8: Bending moment predictions for beams with grade 1.4307 austenitic stainless steel using a b/h
 318 ratio of (a) 1.00 (b) 0.85 (c) 0.7 and (d) 0.55.

319 **4.2. Influence of concrete strength**

320 The results presented in Figs. 6, 7 and 8 exhibit the influence that concrete strength has on the ultimate
 321 bending moment capacity for a range of beam geometries and different grades of stainless steel. It is
 322 observed that the ultimate bending moment capacity obtained using the numerical model and the full
 323 analytical model improves by around 8% on average, respectively, when the concrete strength is
 324 increased from 20 to 50 MPa, for all cases considered. Whilst this same value for the simplified

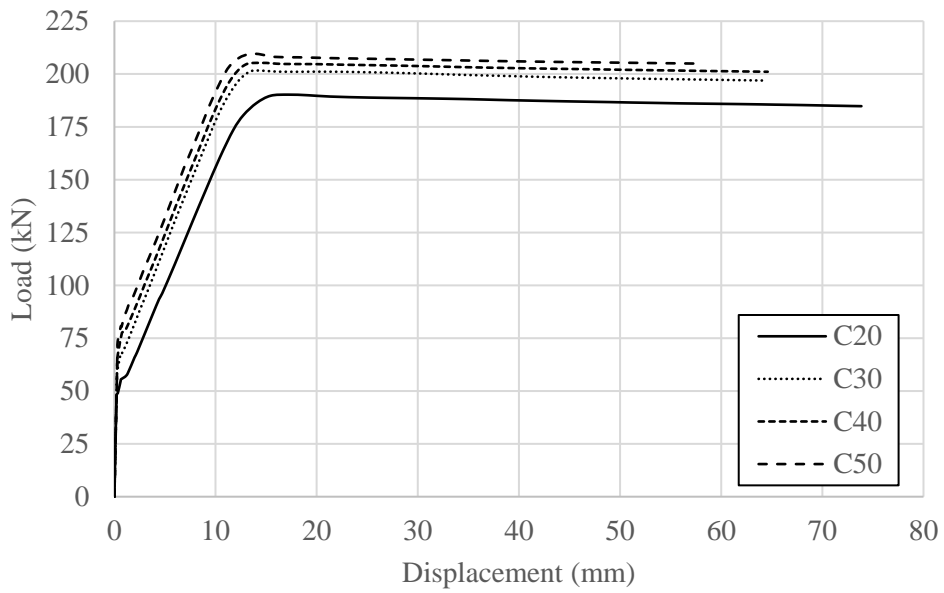
325 analytical model is 21.5%. Clearly, the ultimate bending moment calculated from the simplified
326 analytical model is more influenced by the strength of concrete compared with those obtained using the
327 numerical or the full analytical models. This is perhaps owing to the simplified bi-linear material
328 behaviour of the stainless steel employed in the simplified material model which, for beams made from
329 a relatively higher concrete strength, enables the reinforcement to carry further tensile forces prior
330 concrete crushing failure. Despite this, all the predictions of the simplified method are currently lower
331 than the numerical values, considering the new proposed values for the C_2 parameter.

332 The effect of concrete strength on the load-displacement response is illustrated in Figs. 9, 10 and 11 for
333 beams made using stainless steel reinforcement in grade 1.4311, 1.4162 and 1.4307, respectively. The
334 section used in this analysis is 300 mm in width and 545 mm in height (i.e. the b/h ratio is 0.55). The
335 concrete strength is varied between 20 and 50 MPa. It is clear that as expected, the initial bending
336 stiffness, crack load (i.e. identified as the load in which the slope of the load-displacement curve begins
337 to change) and ultimate load of the beam is improved by increasing the strength of concrete, for all
338 cases. For example, increasing the strength of concrete from 20 MPa to 50 MPa enhances the cracking
339 load and the ultimate load by around 43% and 11% on average, respectively. Beams with C20 concrete
340 exhibit a softer bending stiffness, lower cracking load and ultimate load compared with the responses
341 obtained using the other concrete strengths. This is most likely because the lower tensile strength of
342 C20 leads to greater cracking in the specimen which affects the overall load-displacement response.



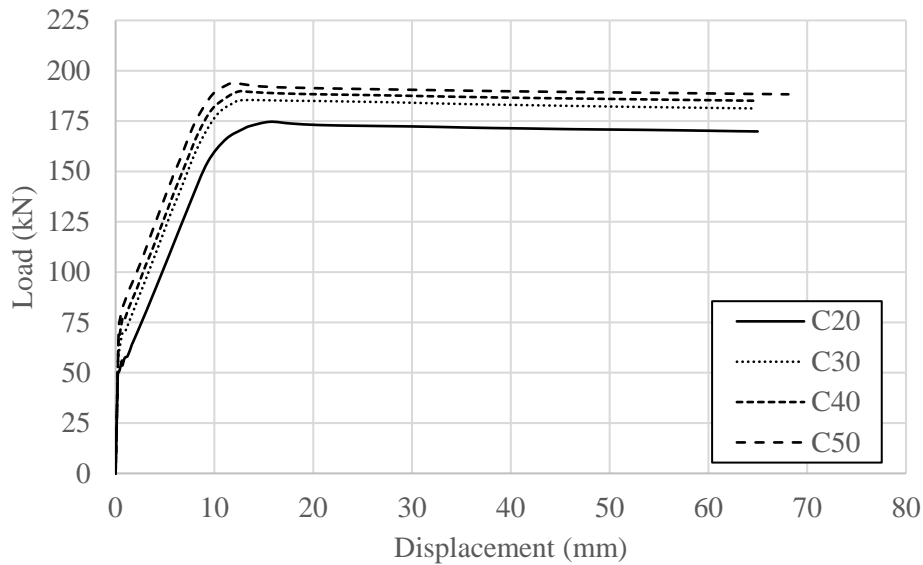
343

344 Fig. 9: Load-displacement curves obtained numerically using various concrete strength for beams
 345 with stainless steel grade 1.4311.



346

347 Fig. 10: Load-displacement curves obtained numerically using various concrete strength for beams
 348 with stainless steel grade 1.4162.



349

350 Fig. 11: Load-displacement curves obtained numerically using various concrete strength for beams
 351 with stainless steel grade 1.4307.

352 4.3. Stainless steel grade

353 The effect that stainless steel grade has on the load-displacement response is illustrated in Fig. 12. For
 354 illustrative purposes, a beam with C50 concrete is considered in this study which is 300 mm in width
 355 and 545 mm in height (i.e. b/h ratio of 0.55). It is evident from the figure that using different stainless
 356 steel grades shows no significant effect on the cracking load or the initial bending stiffness of the beams
 357 mainly owing to having similar modulus of elasticity. However, using stainless steel grades 1.4162 and
 358 1.4307 improves the ultimate load capacity by around 13% and 4%, respectively, compared to grade
 359 1.4311. It is noteworthy that grade 1.4162 has the highest yield strength of the grades examined in this
 360 study, and therefore the beam with reinforcement made from this material is expected to reach a higher
 361 load capacity.

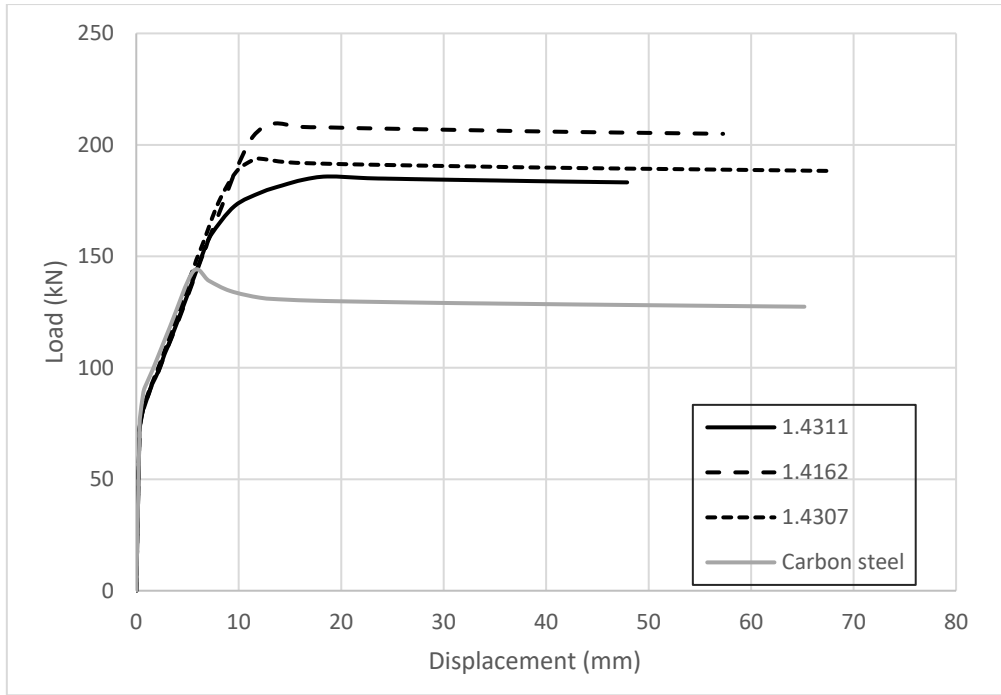
362 Fig. 12 also shows the load-displacement response for a similar beam with carbon steel reinforcement.
 363 It is assumed that the carbon steel material model is elastic-perfectly plastic, in accordance with the
 364 guidance given in Eurocode 2 [6]. Although there are likely to be some deviations between the real
 365 stress-strain behaviour of carbon steel reinforcement and this bilinear model, the model is generally a
 366 good representation of the carbon steel constitutive response, as shown in Fig. 2. The modulus of

367 elasticity and yield strength are taken as 200 GPa and 500 N/mm², respectively. The figure illustrates
368 that using carbon steel reinforcement shows no considerable difference in terms of the cracking load or
369 the initial bending stiffness of the beams, compared with the stainless steel reinforced concrete
370 members. However, it is clearly observed that the ultimate load capacity for the beam with carbon steel
371 rebars is significantly lower, by around 27% on average, compared with that of stainless steel beams.
372 Additionally, it is evident from Table 3 that beams with carbon steel reinforcement develop lower
373 ultimate bending moment capacities compared with those of stainless steel beams.

374 The other important observation is that the deflection at the ultimate load of the beam is influenced by
375 the grade of stainless steel, as shown in Fig. 12. For instance, the beam with grade 1.4311 stainless steel
376 reinforcement deflects to 18.6 mm at the ultimate load whereas the corresponding deflections for beams
377 with grades 1.4162 and 1.4307 are 13.4 and 12 mm, respectively. Given that grade 1.4311 has the
378 highest strain hardening capacity of the stainless steels examined herein, it is clearly intuitive to
379 conclude that the ductility of the section is improved by using reinforcement with a greater ultimate
380 strain.

381 In order to analyse the accuracy of the full and simplified analytical models when different stainless
382 steel grades are used, Table 3 shows a comparison of the bending moment predictions obtained
383 numerically and analytically with reference to the predictions of Eurocode 2. The results are obtained
384 for two different sections with width to height (b/h) ratios of 0.55 and 0.70. The results demonstrate
385 that both the full and simplified models as well as the Eurocode 2 tend to provide less conservative
386 bending moment predictions compared with the numerical values when a grade of stainless steel with
387 a relatively higher strength is used.

388



389

390 Fig. 12: Load-displacement curves obtained numerically for different reinforcement grades.

391 Table 3: Comparison between the ultimate bending moment predictions obtained numerically and
 392 analytically for different reinforcement grades.

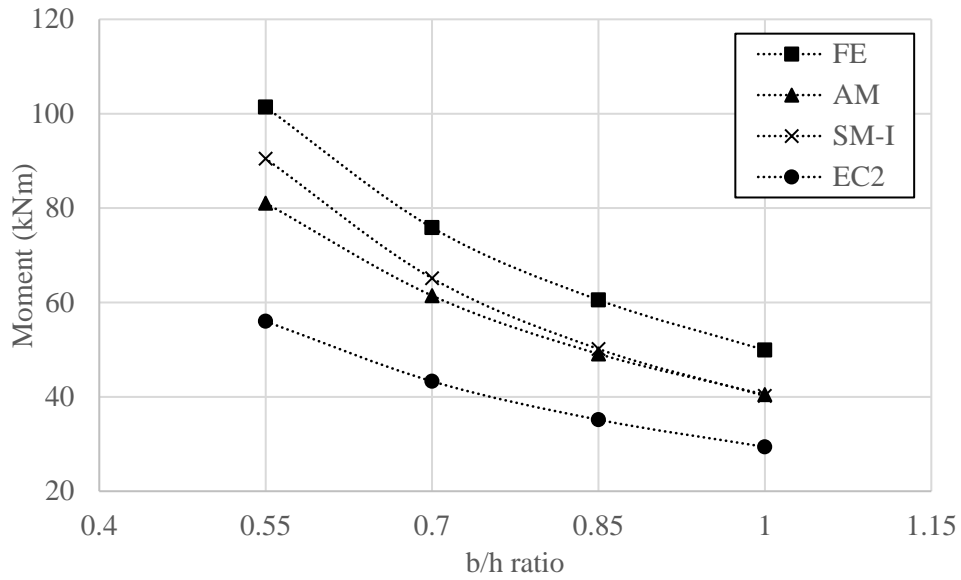
b/h ratio	Grade	FE (kNm)	AM (kNm)	SM-I (kNm)	EC2 (kNm)	AM/FE (%)	SM-I/FE (%)	EC2/FE (%)
0.55	1.4311	101.4	81.0	90.5	56.0	-20.1	-10.8	-44.8
	1.4162	113.8	97.8	109.5	79.3	-14.1	-3.7	-30.3
	1.4307	104.9	85.8	98.3	65.5	-18.2	-6.3	-37.6
	B500b	78.9	-	-	58.3	-	-	-26.1
0.7	1.4311	75.9	61.4	65.1	43.3	-19.0	-14.1	-42.9
	1.4162	85.8	74.5	80.0	61.2	-13.2	-6.8	-28.6
	1.4307	78.7	66.1	71.2	50.6	-16.0	-9.5	-35.7
	B500b	56.4	-	-	45.14	-	-	-20

393

394 4.4. Geometry

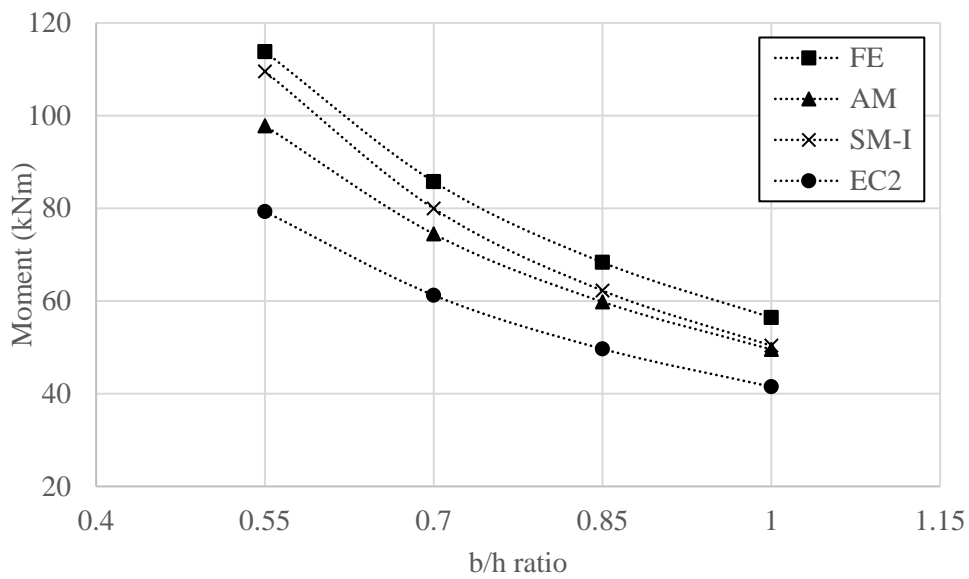
395 In order to investigate the effect that the geometry of the section has on the behaviour of stainless steel
396 RC beams, beams with different b/h ratios ranging from 1.00 to 0.55 are considered in the current
397 section. The results presented are obtained for beams made from C50 concrete. Figs. 13, 14 and 15
398 illustrate the relationship between the bending moment predictions obtained from the numerical and
399 analytical models, and b/h ratios for beams with stainless steel grades 1.4311, 1.4162 and 1.4307,
400 respectively. It is clear that the ultimate bending moment significantly increases for beams with a
401 relatively lower b/h ratio, as expected since these beams would have a greater second moment of area.
402 The simplified analytical model tends to provide a higher prediction compared with the full analytical
403 model for beams with a lower b/h ratio. However, the bending moment predictions obtained from the
404 simplified analytical model are lower than those obtained numerically in all cases, therefore providing
405 a conservative prediction. It is noteworthy that the full analytical method improves the accuracy of the
406 bending capacity of the section by around 41%, 21% and 32% on average, compared with the current
407 design approach in Eurocode 2, for the results presented in this section and obtained using stainless
408 steel grades 1.4311, 1.4162 and 1.4307, respectively.

409 Fig. 16 presents the relationship between the beam geometry and the ability of the section to exploit the
410 strain hardening capabilities of the stainless steel, using the full analytical model. It is shown that the
411 geometry of the beam has a relatively small influence on the exploitation of strain hardening. For
412 example, a beam with a b/h ratio of 0.55 develops around 4.2%, 2.9% and 2.2% more stress in the
413 reinforcement for grades 1.4311, 1.4162 and 1.4307, respectively, compared with members with a b/h
414 ratio of 1.00. In general, it is observed that beams reinforced with 1.4162 grade lean duplex stainless
415 steel reinforcement exhibit greater exploitation of the strain hardening capacity in the stainless steel,
416 compared with beams reinforced with the austenitic grades 1.4307 and 1.4311.



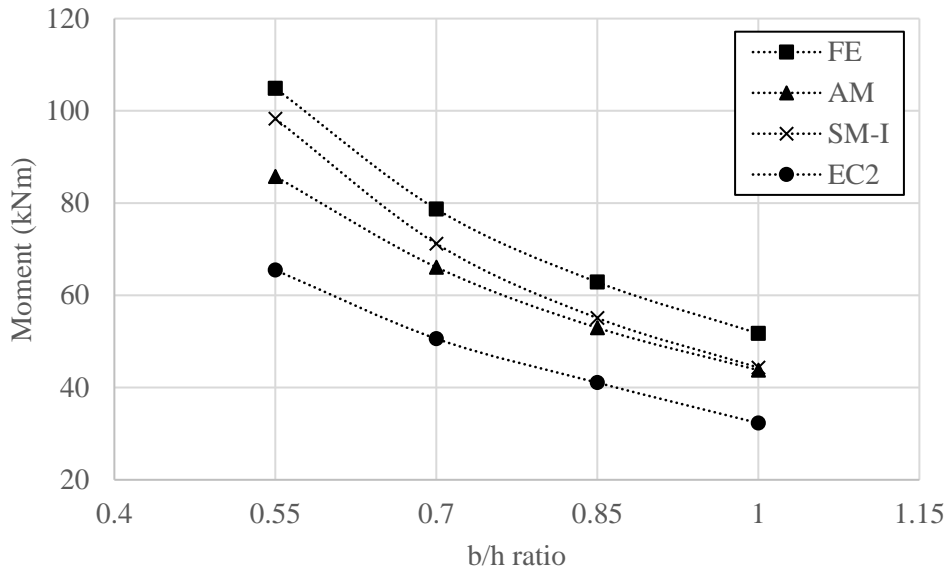
417

418 Fig. 13: Effect of the beam geometry on the bending moment predictions for beams with austenitic
 419 stainless steel grade 1.4311.



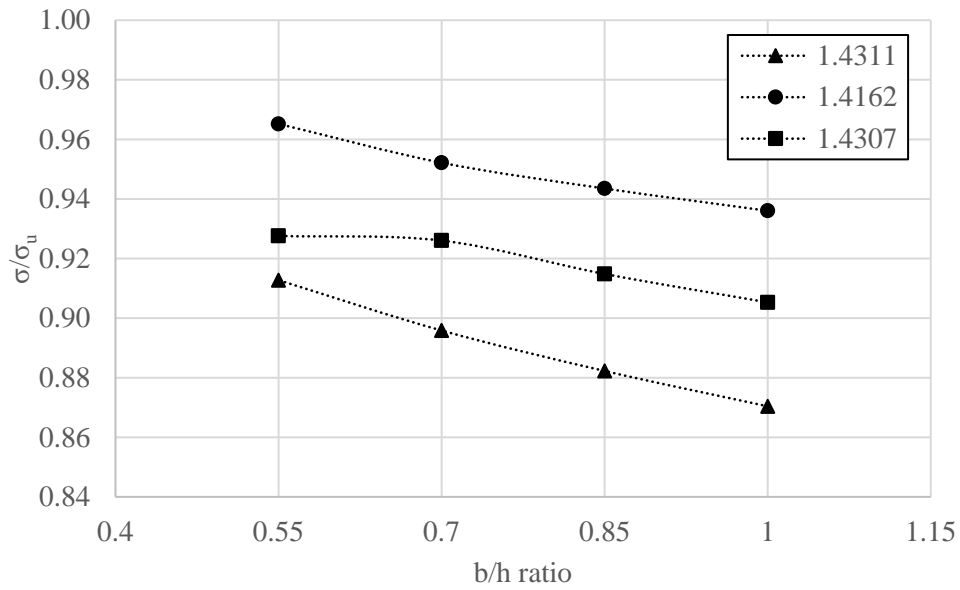
420

421 Fig. 14: Effect of the beam geometry on the bending moment predictions for beams with lean duplex
 422 stainless steel grade 1.4162



423

424 Fig. 15: Effect of the beam geometry on the bending moment predictions for beams with austenitic
 425 stainless steel grade 1.4307.



426

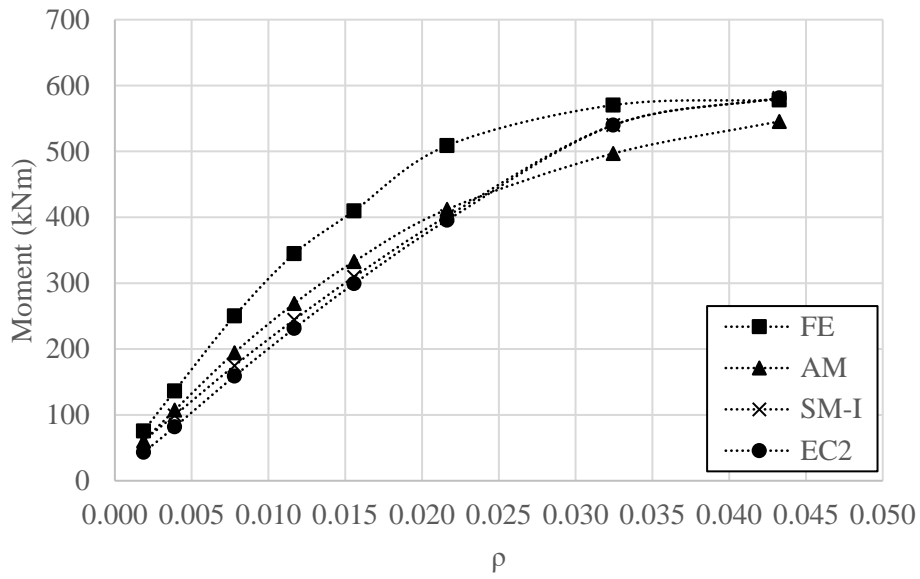
427 Fig. 16: Effect of the beam geometry on the exploitation of strain hardening.

428 **4.5. Reinforcement ratio**

429 Reinforcement ratio is an important parameter in the design of reinforced concrete sections as it dictates
 430 not only the load carrying capacity but also the failure mode. In this section, the influence of
 431 reinforcement ratio on the behaviour of stainless steel RC beams, in particular the exploitation of strain

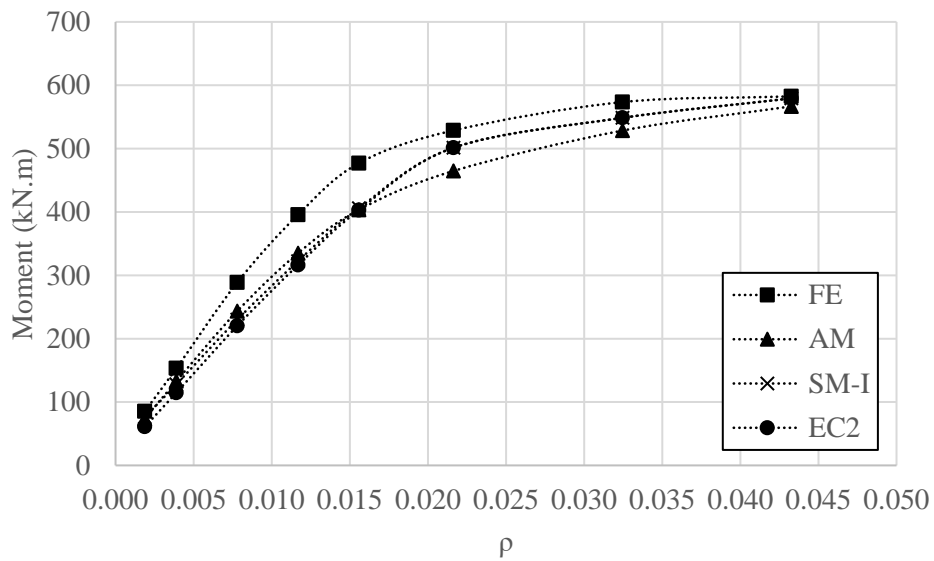
432 hardening in the reinforcement, is assessed. The results presented are obtained for beams with concrete
433 strength C40 and a b/h ratio of 0.70.

434 Figs. 17, 18 and 19 illustrate the effect that reinforcement ratio (ρ) has on the bending moment capacity
435 values obtained numerically and analytically for beams made using stainless steel reinforcement in
436 grades 1.4311, 1.4162 and 1.4307, respectively. The results demonstrate that both the full and simplified
437 analytical models underestimate the bending moment capacities obtained numerically in almost all
438 cases, which is conservative and in line with previous findings. The numerical analyses show that the
439 bending moment capacity improves as the reinforcement ratio increases until it reaches a specific ratio
440 (i.e. around 0.032 in the cases presented herein) after which no further improvement in the bending
441 capacity is observed. The reason for this is most likely due to the greater depth of the neutral axis when
442 a higher reinforcement ratio is employed which increases the compressive stress in the concrete until it
443 crushes, and no further improvement can be achieved. Moreover, both the simplified analytical model
444 and the Eurocode 2 design rules provide identical predictions, as expected, when a higher reinforcement
445 ratio is used since both models are based on the same constitutive behaviour for the stainless steel in
446 the elastic range. It is also observed that for beams with a relatively higher reinforcement ratio, the
447 moment capacities predicted by the full analytical model are below those from the simplified analytical
448 model and also Eurocode 2. This is owing to the nonlinearity of the material model which starts from
449 an early stage.



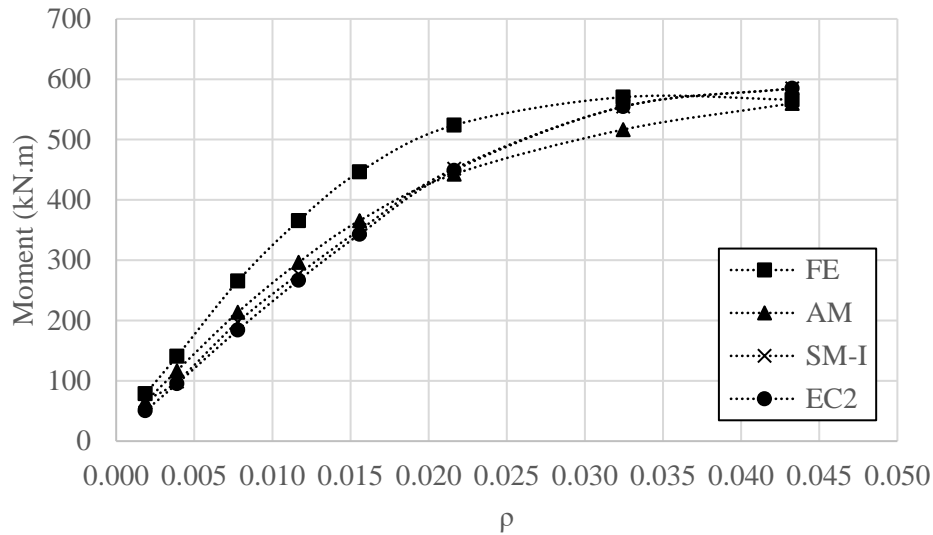
450

451 Fig. 17: Effect of the reinforcement ratio (ρ) on the bending moment capacity for beams made using
 452 grade 1.4311 austenitic stainless steel.



453

454 Fig. 18: Effect of the reinforcement ratio (ρ) on the bending moment capacity for beams made using
 455 grade 1.4162 lean duplex stainless steel.

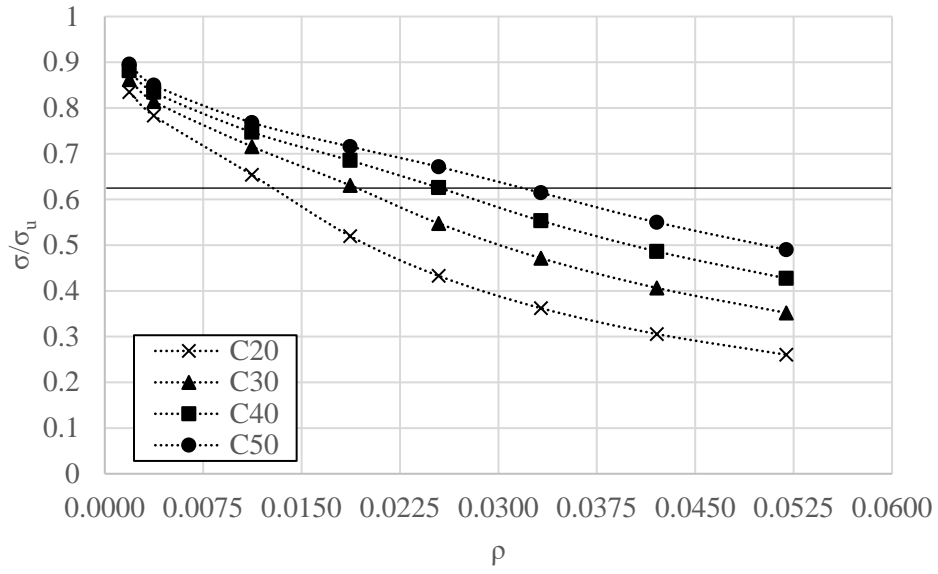


456

457 Fig. 19: Effect of the reinforcement ratio (ρ) on the bending moment capacity for beams made using
 458 grade 1.4307 austenitic stainless steel.

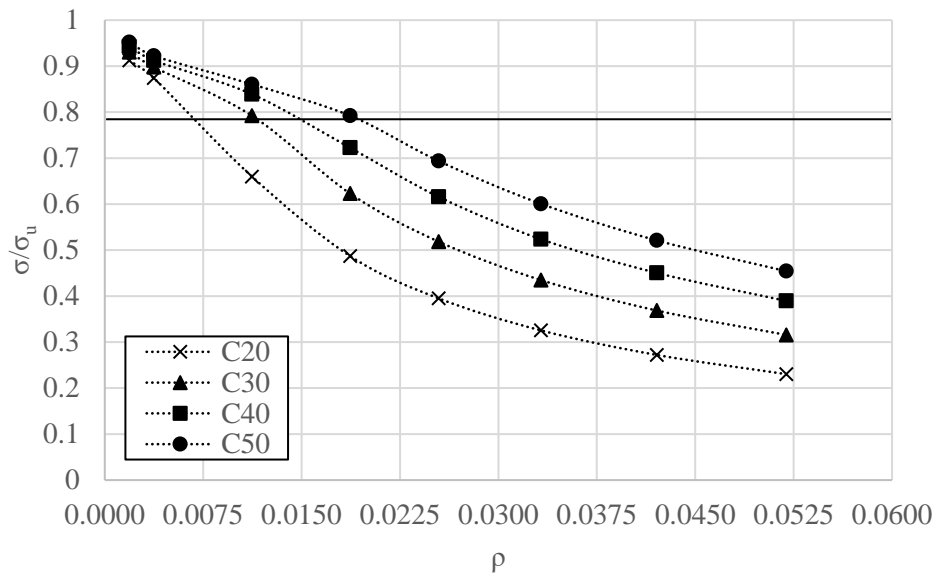
459 Figs. 20, 21 and 22 demonstrate the influence of reinforcement ratio on the exploitation of strain
 460 hardening in the rebar for beams with stainless steel reinforcement in grades 1.4311, 1.4162 and 1.4307,
 461 respectively. These results are obtained using the full analytical model, for a range of different concrete
 462 strengths. The figures illustrate the amount of stress in the rebars that can be exploited when calculating
 463 the ultimate bending moment capacity of the section. The horizontal solid line in each of the figures
 464 represents the yield limit for that particular grade of stainless steel (i.e. $\sigma_{0.2}/\sigma_u$).

465 It is shown in the figures that further exploitation of the strain hardening capacity in the reinforcement
 466 is achieved when a relatively higher grade of concrete is employed. This is mainly because the higher
 467 strength concrete can carry greater compressive forces allowing the rebar to reach greater levels of
 468 stress. In all cases, it is observed that the level of stress in the stainless steel is relatively lower when a
 469 higher reinforcement ratio is employed. This is because an increase in the steel cross-sectional area
 470 generally reduces the levels of stress and strain in the reinforcement and increases the depth of the
 471 neutral axis, which causes a relative increase in the levels of applied stress and strain in the concrete
 472 resulting in crushing of the concrete. Accordingly, lower exploitation of the tensile strength in the
 473 reinforcement is achieved.



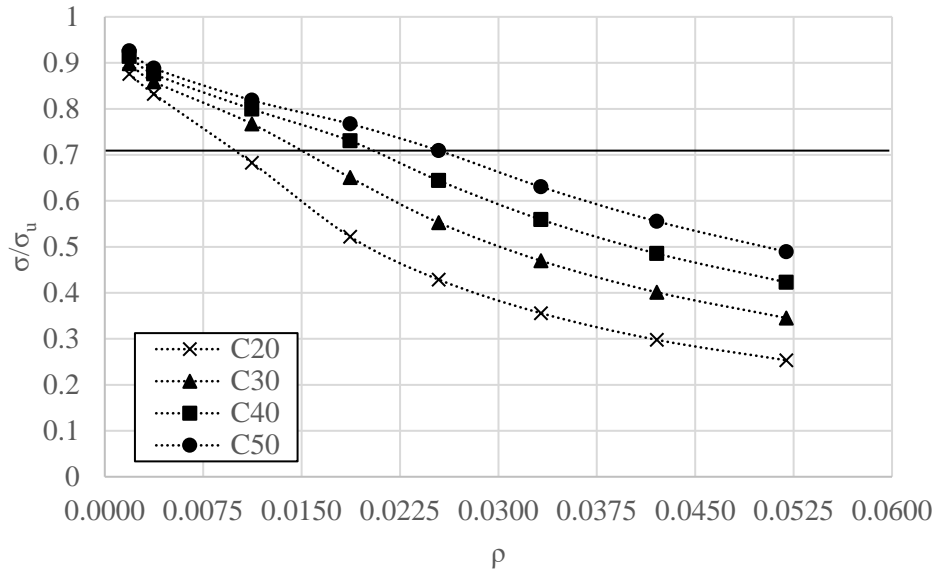
474

475 Fig. 20: Effect of reinforcement ratio on the exploitation of strain hardening for beams reinforced with
 476 grade 1.4311 austenitic stainless steel.



477

478 Fig. 21: Effect of reinforcement ratio on the exploitation of strain hardening for beams reinforced with
 479 grade 1.4162 lean duplex stainless steel.



480

481 Fig. 22: Effect of reinforcement ratio on the exploitation of strain hardening for beams reinforced with
 482 grade 1.4307 austenitic stainless steel.

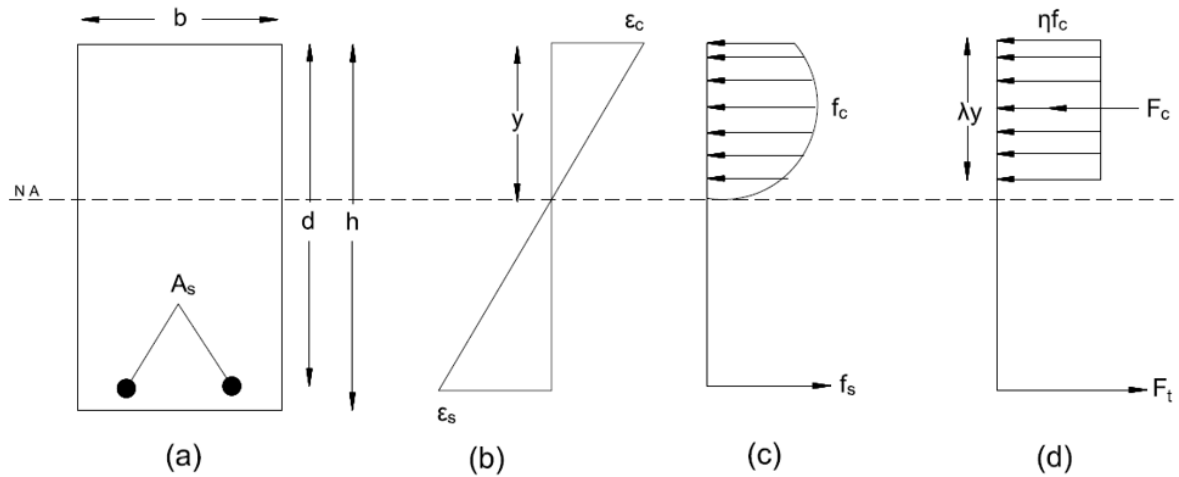
483 A balanced reinforcement ratio (ρ_{bal}) is defined in this paper as the ratio where concrete crushing and
 484 reinforcement yielding occur simultaneously in the cross section. In order to utilize and exploit the
 485 positive strain hardening properties of stainless steel reinforcement in the design of reinforced concrete
 486 beams, it is necessary to design the section to be under-reinforced. An under-reinforced section is when
 487 the reinforcement ratio is lower than the balanced ratio (i.e. $\rho < \rho_{bal}$). This allows the reinforcement to
 488 yield first and then develop some strain hardening before the section fails due to crushing of concrete.
 489 It ensures enough ductility in the section to avoid sudden catastrophic failure of the reinforced concrete
 490 member. On the other hand, if the beam is designed to be over-reinforced (i.e. $\rho > \rho_{bal}$), failure will
 491 occur by crushing of the concrete before the rebar yields, and the strain hardening characteristics of the
 492 stainless steel will not be exploited. This design case is neither desirable nor efficient, but could still be
 493 employed if a higher partial safety factor is considered.

494 A balanced reinforcement ratio (ρ_{bal}) can be identified for stainless steel reinforced concrete sections as
 495 the reinforcement ratio at which when the tensile strain in the rebar reaches to 0.2% strain ($\epsilon_{0.2}$)
 496 simultaneously with the concrete on the top surface reaching the ultimate crushing strain (ϵ_{cu}). This

497 requires obtaining the depth of the neutral axis (y) from the strain distribution in Fig. 23, as presented
 498 in Eq. 14:

$$y = \frac{d}{1 + \varepsilon_{0.2}/\varepsilon_{cu}} \quad (14)$$

499



500

501 Fig. 23: Strain and stress distribution diagrams for a reinforced concrete beam including (a) the cross-
 502 section (b) the strain distribution, (c) the stress distribution and (d) an equivalent stress distribution in
 503 the section.

504 The equilibrium of internal forces can be applied, as presented in Eq. 15, by assuming the depth of the
 505 compressive stress block of the concrete is $0.8y$ and the concrete compressive stress in the concrete
 506 stress block is $0.85f_c$:

$$0.68f_c y b - A_s \sigma_s = 0 \quad (15)$$

507 In this expression, the tensile stress (σ_s) is the 0.2% proof stress of the reinforcement ($\sigma_{0.2}$).

508 By substituting Eq. 14 into Eq. 15, Eq. 16 is obtained:

$$0.68f_c \left(\frac{d}{1 + \varepsilon_{0.2}/\varepsilon_{cu}} \right) b - A_s \sigma_{0.2} = 0 \quad (16)$$

509 The balanced reinforcement ratio (ρ_{bal}) is obtained by rearranging Eq. 16, as follows:

$$\rho_{\text{bal}} = \frac{A_s}{bd} = \frac{0.68}{\sigma_{0.2}} \left(\frac{f_c}{1 + \varepsilon_{0.2}/\varepsilon_{\text{cu}}} \right) \quad (17)$$

510 In the case of under-reinforced section, the reinforcement ratio must be greater than the minimum ratio
 511 required to prevent the rupture of the rebar which it can be obtained using Eq. 18.

$$\rho_{\text{min}} = \frac{0.68}{\sigma_u} \left(\frac{f_c}{1 + \varepsilon_u/\varepsilon_{\text{cu}}} \right) \quad (18)$$

512 4.6. Deflections

513 A realistic estimation of the levels of deflection that develop in a structure is imperative to ensure
 514 acceptable serviceability and the comfort of end-users. Thus, global design standards typically provide
 515 limiting values for deflections which should not be exceeded. In Eurocode 2, for example, the allowable
 516 deflection is limited to span/250 for members subjected to quasi-permanent loads [6]. Deflections are
 517 in important consideration for concrete members reinforced with stainless steel owing to the excellent
 518 ductility of the reinforcing material. In the deflection calculations for RC beams, using the elastic
 519 modulus of stainless steel may result in over-conservative predictions due to the non-linear behaviour
 520 of the stainless steel, even in the low-strain range. Therefore, this section aims to evaluate the deflection
 521 design approach in Eurocode 2 for stainless steels RC beams. The predicted results from Eurocode 2
 522 are compared with the corresponding values from the numerical model. The influences of implementing
 523 the secant modulus and the tangent modulus of stainless steel in the deflection calculations for RC
 524 beams are also explored.

525 In Eurocode 2, the deflection of a member is obtained based on the assumption that the concrete member
 526 comprises cracked and un-cracked sections, at the service load. Accordingly, the maximum deflection
 527 (δ_{EC2}) for RC members is calculated as follows:

$$\delta_{\text{EC2}} = (1 - \zeta)\delta_1 + \zeta\delta_2 \quad (19)$$

528 In this expression, ζ is a distribution coefficient representing the tension stiffening phenomenon in the
 529 section, and is taken as zero for the un-cracked portion of the section, otherwise it is calculated using
 530 Eq. 20:

$$\zeta = 1 - \beta \left(\frac{M_{cr}}{M_a} \right)^2 \quad (20)$$

531 where β is a coefficient that accounts for the effect of the duration of loading on the average strain, and
 532 is assumed to have a value of unity for a single short-term loading and 0.5 for sustained and cyclic
 533 loading. M_{cr} and M_a are the bending moment values calculated at the cracking and service loads,
 534 respectively. The cracking moment (M_{cr}) is determined as:

$$M_{cr} = \frac{f_t I_g}{y} \quad (21)$$

535 δ_1 and δ_2 are the deflection values obtained for the un-cracked section and cracked section, respectively,
 536 and are determined from Eqs. 22 and 23 for beams subjected to four point bending conditions:

$$\delta_1 = \frac{Pa}{24E_c I_g} (3L^2 - 4a^2) \quad (22)$$

$$\delta_2 = \frac{Pa}{24E_c I_{cr}} (3L^2 - 4a^2) \quad (23)$$

537 In these expressions, P is the applied load at each point, L is the clear span and a is the distance between
 538 the support and the nearest loading point. I_g and I_{cr} are the second moment of area calculated on the
 539 basis of the un-cracked and cracked sections, respectively, determined using the expressions in Eqs. 24
 540 and 25:

$$I_g = \frac{bh^3}{12} \quad (24)$$

$$I_{cr} = \frac{bd^3k^3}{3} + nA_s d^2 (1 - k)^2 \quad (25)$$

$$\text{where } k = \sqrt{2\rho n + (\rho n)^2} - \rho n$$

541 In Eq. 25, the term n refers to the modular ratio between the reinforcement and the concrete, given as
 542 the ratio of E to E_c .

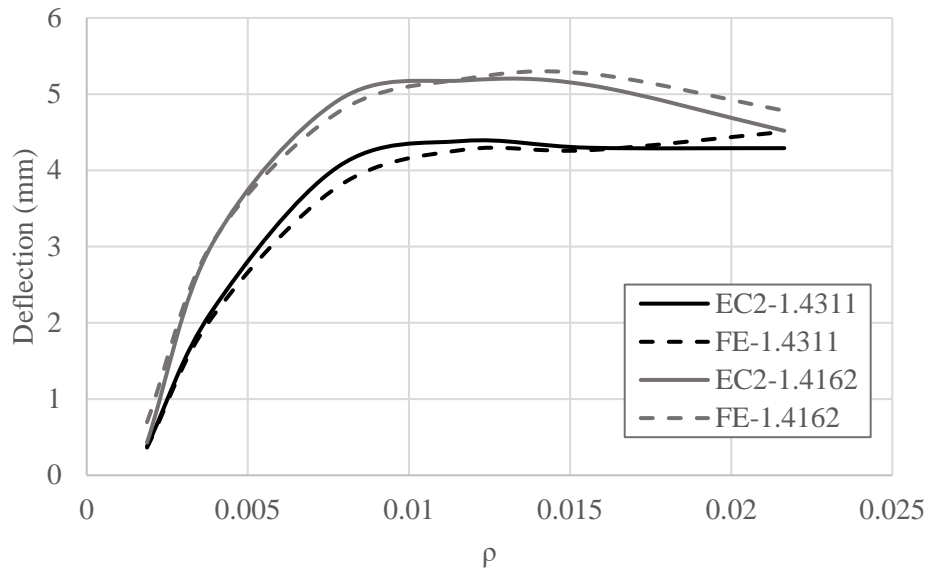
543 In the current analysis, the deflection of the beam is calculated at the mid-span of the member at the
544 service moment, which is 30% of the ultimate bending moment ($0.3M_u$), as well as at 67% of the
545 ultimate bending moment ($0.67M_u$). Table 4 presents a comparison between the measured deflections
546 from the numerical model (δ_{FE}) and the predicted values obtained using Eurocode 2 (δ_{EC2}), using the
547 expressions given in Eqs. 19-25. The results presented in the table are for beams made from C40
548 concrete which are 300 mm in width and 428 mm in depth, and employ the elastic modulus for the
549 stainless steel (E) in the calculations. In order to study the influence of the stainless steel constitutive
550 relationship on the deflection of RC beams, various reinforcement ratios (ρ) are considered to develop
551 different levels of stress in the reinforcement.

552 It is observed that the Eurocode 2 design deflections at $0.3M_u$ are in very good agreement with the
553 corresponding numerical values (δ_{EC2}/δ_{FE}) with the maximum and average differences being around -
554 38% and -2%, respectively. These same values at $0.67M_u$ are -28% and -15%, respectively. Figs. 24(a)
555 and (b) demonstrate the influence that the reinforcement ratio has on the beam deflections at $0.3M_u$ and
556 $0.67M_u$, respectively. It is clear that Eurocode 2 predictions are in very good agreement with the
557 corresponding measured values from the FE model in almost all cases for beams which are at the service
558 load, corresponding to a bending moment of $0.3M_u$. On the other hand, the code results in over-
559 conservative predictions for beams with relatively higher reinforcement ratios, when the beam is
560 subjected to $0.67M_u$. It is also observed that the deflections rise with an increase of reinforcement ratio
561 up to specific point (i.e. at a reinforcement ratio of around 1%) after which remains more or less
562 constant. This indicates that the deflection is more influenced by the reinforcement ratio for relatively
563 low values of ρ , where the stress level in the reinforcement is relatively greater.

564 Table. 4: Results of the predicted deflection obtained from Eurocode 2 in comparison with the measured
 565 values from the FE model.

Reinforcement ratio (ρ)	Grades	Bending moment		Deflections at $0.3M_u$			Deflections at $0.67M_u$		
		$0.3M_u$ (kNm)	$0.67M_u$ (kNm)	δ_{EC2} (mm)	δ_{FE} (mm)	δ_{EC2}/δ_{FE}	δ_{EC2} (mm)	δ_{FE} (mm)	δ_{EC2}/δ_{FE}
0.0019	1.4311	22.7	50.6	0.38	0.36	1.05	6.05	6.47	0.94
	1.4162	25.6	57.1	0.43	0.70	0.62	7.80	8.19	0.95
	1.4307	23.6	52.6	0.40	0.42	0.95	6.36	6.70	0.95
0.0039	1.4311	40.9	91.3	2.16	2.07	1.04	9.10	9.31	0.98
	1.4162	46.0	102.7	3.04	3.05	1.00	10.64	11.22	0.95
	1.4307	42.2	94.2	2.32	2.38	0.98	9.17	9.51	0.96
0.0078	1.4311	75.0	167.5	4.05	3.79	1.07	10.15	11.34	0.90
	1.4162	86.6	193.3	4.91	4.76	1.03	11.96	13.82	0.87
	1.4307	79.6	177.8	4.24	4.02	1.06	10.49	12.02	0.87
0.0117	1.4311	103.4	231.0	4.39	4.27	1.03	10.30	12.30	0.84
	1.4162	118.7	265.1	5.18	5.20	1.00	12.02	14.83	0.81
	1.4307	109.7	244.9	4.56	4.47	1.02	10.63	12.84	0.83
0.0156	1.4311	122.9	274.4	4.30	4.26	1.01	9.89	12.27	0.81
	1.4162	143.1	319.6	5.12	5.27	0.97	11.69	15.37	0.76
	1.4307	133.9	299.1	4.59	4.62	0.99	10.50	13.36	0.79
0.0216	1.4311	152.6	340.9	4.29	4.51	0.95	9.73	13.27	0.73
	1.4162	158.6	354.2	4.52	4.78	0.94	10.23	14.15	0.72
	1.4307	157.2	351.0	4.31	4.53	0.95	9.76	13.28	0.74

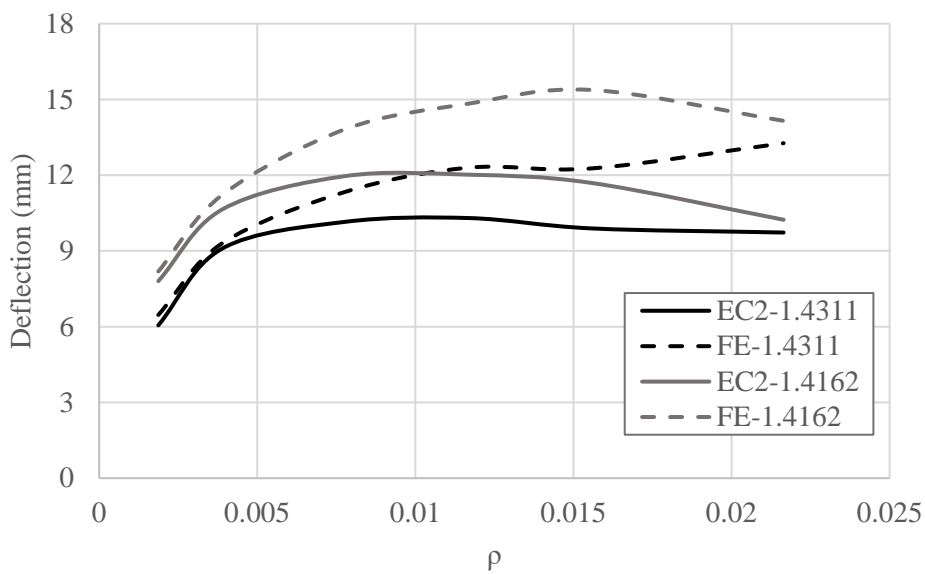
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(a)



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(b)

571 Fig. 24: Effect of reinforcement ratio on the deflection of a stainless steel reinforced concrete beam at

572 (a) $0.3M_u$ and (b) $0.67M_u$.

573 As stated before, the current design approach in Eurocode 2 [6] calculates the deflection on the basis of

574 the modulus of elasticity of the reinforcement. This assumption is acceptable in the case of carbon steel

575 reinforcement, however it may result in an over-conservative prediction in the case of stainless steel

576 reinforcement owing to its nonlinear behaviour. In the design of structural stainless steel sections, it is
 577 recommended to use the secant modulus in deflection calculations rather than the elastic modulus [37].
 578 In order to investigate this for reinforced concrete design, the predicted deflections calculated using
 579 secant modulus and also the tangent modulus of the stainless steel reinforcement are compared with
 580 their corresponding numerical values.

581 The secant modulus of elasticity (E_{sec}) for stainless steel is obtained from the modified Ramberg-
 582 Osgood material model presented earlier in Eqs. 1 and 2 according to:

$$E_{\text{sec}} = \frac{E}{1 + 0.002 \frac{E}{\sigma} \left(\frac{\sigma}{\sigma_{0.2}} \right)^n} \quad \text{for } \sigma \leq \sigma_{0.2} \quad (26)$$

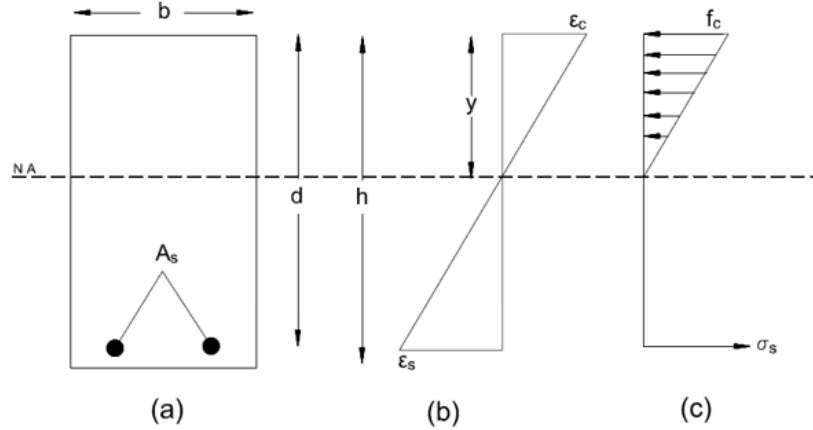
$$E_{\text{sec}} = \frac{\sigma}{\varepsilon_{0.2} + \frac{\sigma - \sigma_{0.2}}{E_2} + \left(\varepsilon_u - \varepsilon_{0.2} - \frac{\sigma_u - \sigma_{0.2}}{E_2} \right) \left(\frac{\sigma - \sigma_{0.2}}{\sigma_u - \sigma_{0.2}} \right)^m} \quad \text{for } \sigma_{0.2} < \sigma \leq \sigma_u \quad (27)$$

583 The tangent modulus of elasticity (E_{tan}) is the derivative of the secant modulus and is determined as
 584 follows:

$$E_{\text{tan}} = \frac{\sigma_{0.2} E}{\sigma_{0.2} + 0.002 n E \left(\frac{\sigma}{\sigma_{0.2}} \right)^{n-1}} \quad \text{for } \sigma < \sigma_{0.2} \quad (28)$$

$$E_{\text{tan}} = \frac{1}{\frac{1}{E_2} + \left(\varepsilon_u - \varepsilon_{0.2} - \frac{\sigma_u - \sigma_{0.2}}{E_2} \right) \left(\frac{m}{(\sigma_u - \sigma_{0.2})^m} \right) (\sigma - \sigma_{0.2})^{m-1}} \quad \text{for } \sigma_{0.2} < \sigma \leq \sigma_u \quad (29)$$

585 The deflection of elastic beams (i.e. those not containing a plastic hinge) may be estimated by standard
 586 structural theory. In order to obtain the secant modulus and the tangent modulus of the reinforcement
 587 at $0.3M_u$ and $0.67M_u$, the stress in the reinforcement must first be determined. An elastic analysis of the
 588 section is conducted to obtain the depth of the neutral axis (y) and the stress in the reinforcement,
 589 according to the stress and strain distributions presented in Fig. 25.



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591 Fig. 25: Elastic analysis of a reinforced concrete beam including (a) the cross-section (b) the strain
 592 distribution, (c) the stress distribution in the section.

593 The location of the neutral axis can be obtained from Eq. 30:

$$y = d \left(\sqrt{2\rho n + \rho^2 n^2} - \rho n \right) \quad (30)$$

594 where n is the modular ratio between the reinforcement and concrete:

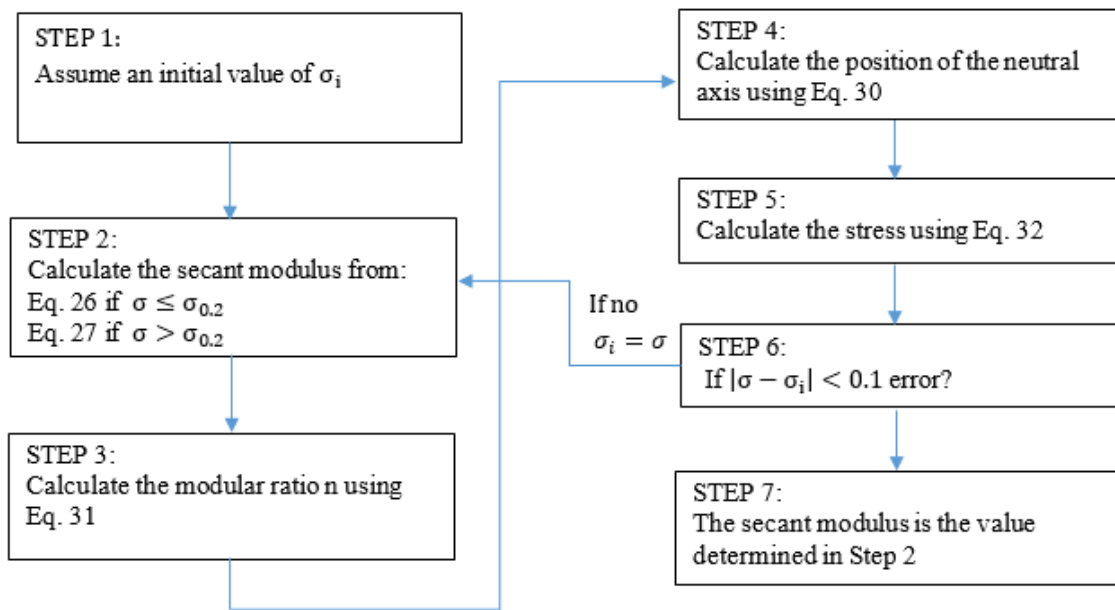
$$n = \frac{E_{sec}}{E_c} \quad \text{for secant modulus} \quad (31)$$

$$n = \frac{E_{tan}}{E_c} \quad \text{for tangent modulus}$$

595 Once the neutral axis depth is located, the stress in the reinforcement is calculated from the stress
 596 distribution in Fig. 25(c), as follows:

$$\sigma_s = \frac{M_a}{A_s(d - y/3)} \quad (32)$$

597 Since the secant and tangent moduli are functions of the stress in the reinforcement, an iterative
 598 technique is required to obtain the solution of Eq. 32. A flow chart describing the solution procedure
 599 for determining the secant modulus is given in Fig. 26. The same solution procedure can be followed
 600 to determine the tangent modulus. Then, the deflections of the beam for load levels corresponding to
 601 $0.3M_u$ and $0.67M_u$ are calculated using secant modulus and the tangent modulus.



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Fig. 26: Flow chart of the solution procedure.

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The predicted deflections obtained using the elastic modulus (δ_{EC2}), secant modulus ($\delta_{EC2(Esec)}$) and tangent modulus ($\delta_{EC2(Etan)}$) for the stainless steel grades considered herein, are presented in Table 5 in comparison with the corresponding numerical values (δ_{FE}). The results show that implementing the secant modulus in the calculations of deflection provides quite accurate predictions at $0.3M_u$ with maximum and average $\delta_{EC2(Esec)}/\delta_{FE}$ values of -38% and 0%, respectively. However, these results are quite similar in terms of accuracy as the corresponding deflections obtained using the elastic modulus of stainless steel, as presented earlier, which gave maximum and average δ_{EC2}/δ_{FE} values of -38% and -2%, respectively. On the other hand, at $0.67M_u$, using the secant modulus in deflection calculations results in un-conservative predictions with maximum and average $\delta_{EC2(Esec)}/\delta_{FE}$ values of 55% and 18%, respectively. The corresponding values when the elastic modulus is used in the calculations are -28% and -15%, respectively, as previously presented.

Using the tangent modulus in deflection calculations at load levels corresponding to $0.3M_u$ results in maximum and average $\delta_{EC2(Etan)}/\delta_{FE}$ values of -38% and 6%, respectively, whilst at $0.67M_u$ the maximum and average $\delta_{EC2(Etan)}/\delta_{FE}$ values are 1130% and 205%, respectively. It is clear that the using the tangent

618 modulus to calculate the deflections results in a significant overestimation of the deflections compared
619 with the numerical model values, especially at higher load levels.

620 In summary, the results presented in this analysis show that there is only a minor improvement in the
621 deflection predictions by adopting the secant modulus rather than the elastic modulus in the
622 calculations, and in all cases at load levels corresponding to $0.3M_u$, conservative predictions are
623 achieved. The predictions obtained using the tangent modulus were significantly less accurate than
624 when the elastic modulus or the secant modulus is employed. Therefore, it is recommended to use the
625 elastic modulus in the calculation of deflections for stainless steel RC beams. It is noteworthy that the
626 predicted deflections for beams with a reinforcement ratio 0.187% at loads corresponding to $0.3M_u$ are
627 typically the same for each stainless steel grade considered herein. After a careful examination of these
628 cases, it was found that applied load is lower than the cracking moment and therefore the deflection is
629 calculated only on the basis of an un-cracked section. In this scenario, the second moment of area is
630 calculated based on the gross area of the section which is the same irrespective of the reinforcement
631 modulus of elasticity.

632 Table. 5: Deflection results obtained using the initial modulus, secant modulus and the tangent modulus
 633 of stainless steel in comparison with the measured values from the FE model.

Reinforcement ratio	Grade	Bending moment (kNm)		Deflections at 0.3M _u			Deflections at 0.67M _u		
		0.3M _u	0.67M _u	δ _{EC2}	δ _{EC2(Esec)}	δ _{EC2(Etan)}	δ _{EC2}	δ _{EC2(Esec)}	δ _{EC2(Etan)}
				/δ _{FE}	/δ _{FE}	/δ _{FE}	/δ _{FE}	/δ _{FE}	/δ _{FE}
0.00187	1.4311	22.7	50.6	1.05	1.05	1.05	0.94	1.36	12.30
	1.4162	25.6	57.1	0.62	0.62	0.62	0.95	1.35	2.89
	1.4307	23.6	52.6	0.95	0.95	0.95	0.95	1.46	4.02
0.00390	1.4311	40.9	91.3	1.04	1.09	1.29	0.98	1.48	5.91
	1.4162	46.0	102.7	1.00	1.01	1.05	0.95	1.26	2.45
	1.4307	42.2	94.2	0.98	1.01	1.11	0.96	1.55	3.60
0.00779	1.4311	75.0	167.5	1.07	1.12	1.29	0.90	1.41	3.60
	1.4162	86.6	193.3	1.03	1.04	1.08	0.87	1.09	1.94
	1.4307	79.6	177.8	1.06	1.08	1.19	0.87	1.33	2.79
0.01169	1.4311	103.4	231.0	1.03	1.06	1.19	0.84	1.35	2.94
	1.4162	118.7	265.1	1.00	1.00	1.03	0.81	0.96	1.52
	1.4307	109.7	244.9	1.02	1.04	1.12	0.83	1.15	2.17
0.01559	1.4311	122.9	274.4	1.01	1.03	1.11	0.81	1.14	2.16
	1.4162	143.1	319.6	0.97	0.98	0.99	0.76	0.85	1.21
	1.4307	133.9	299.1	0.99	1.01	1.06	0.79	1.01	1.72
0.02165	1.4311	152.6	340.9	0.95	0.97	1.02	0.73	0.94	1.57
	1.4162	158.6	354.2	0.94	0.95	0.95	0.72	0.76	0.90
	1.4307	157.2	351.0	0.95	0.96	0.99	0.74	0.85	1.23

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5. Conclusions

This paper has presented a detailed investigation into the behaviour of stainless steel reinforced concrete beams. A full and simplified version of a deformation-based design method for the analysis of these elements has been proposed and examined in comparison with predictions of the current design rules in Eurocode 2. A comprehensive parametric study was conducted to study the influence that various geometric and material properties have on the capacity of the members. Moreover, the paper provides guidance for selecting an appropriate reinforcement ratio in order to allow for an evaluation of the strain hardening properties of the stainless steel reinforcement being included in the design. In the final section of the paper, the serviceability limit state for stainless steel reinforced concrete beams has been explored through a detailed analysis of the deflection behaviour. Overall, the results and analysis presented in this paper have provided an excellent basis for engineers to specify stainless steel reinforcement in reinforced concrete beams in an efficient and sustainable manner, with minimal wastage of materials. Following this detailed study, the following key findings and recommendations for international codes of practice are presented:

1. The proposed full and simplified analytical approach is shown to be an effective design tool that exploits the distinctive characteristics of stainless steel reinforcement in an efficient and reliable manner.
2. For the range of data examined here, the average and maximum full analytical-to-numerical bending moment values are -14.9% and -22.3% whilst these same values obtained using the Eurocode 2 design rules are -28.3% and -44.7%, respectively.
3. The predictions of the simplified proposed analytical model are in excellent agreement with the predictions of the full analytical model with the average and maximum full-to-simplified bending moment values are -2.8% and -17.2%, respectively
4. In general, it is shown that further exploitation of the strain hardening capacity in the rebar is achieved when a relatively higher grade of concrete is employed.
5. It is also found that the b/h ratio of the beam has a relatively small influence on the exploitation of strain hardening.

- 662 6. It is observed that the levels of stress in the rebar are relatively lower when a higher
663 reinforcement ratio is employed.
- 664 7. It is recommended that the elastic modulus is employed in the calculation of deflections for
665 stainless steel RC beams rather than the secant modulus or the tangent modulus.
- 666 8. Finally, although the results presented herein are very promising in terms of improving the
667 efficiency of designing stainless steel reinforced concrete beams, it is important that the shear
668 resistance is studied in future work, including how the revised flexural capacities determined
669 herein are likely to affect the design shear resistance.

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