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1 **Non-linear and mixed regression models in predicting sustainable**
2 **concrete strength**

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11

12 **Abstract**

13 Most previous research adopting the regression analysis to capture the relationship
14 between concrete properties and mixture-design-related variables was based on the
15 linear approach with limited accuracy. This study applies non-linear and mixed regression
16 analysis to model properties of environmentally friendly concrete based on a
17 comprehensive set of variables containing alternative or waste materials. It was found
18 that best-fit non-linear and mixed models achieved similar accuracies and superior R^2
19 values compared to the linear approach when using both the numerical and relative input
20 methods. Individual materials' effects on concrete strength were statistically quantified at
21 different curing ages using the best-fit models.

22 **Keywords**

23 [Sustainable concrete](#); concrete mixture design; [cementitious materials](#); concrete strength;
24 statistical modeling; [non-linear](#) regression analysis; [mixed model](#) [curing age](#);
25 [sustainability](#)

26 1. Introduction

27 As the most widely consumed construction material worldwide, concrete has recently
28 caught a lot of attention from researchers who are interested in finding out how its sustainability
29 could be improved by replacing conventional cementitious and aggregate materials with
30 alternative or waste materials. In their studies [1, 2, 3], one main focus is to understand how
31 these materials affect concrete properties. Although some understanding has been generated
32 based on limited experimental data, it is not adequate to stimulate wider application of
33 sustainable concrete in the construction industry. To fill this gap, the authors selected Portland
34 limestone cement (PLC), Haydite® lightweight aggregate (LWA), and fly ash (FA) Class F as
35 alternative materials in their sustainable concrete research based on the industry feedback
36 collected from a market survey they conducted earlier [4].

37 Mathematical modeling has been adopted by some researchers [1, 5, 6, 7] to capture the
38 relationships between properties of sustainable concrete and mixture-design-based
39 independent variables. So far limited studies such as Omran et al. [7] have included a
40 comprehensive list of concrete-mixture-design-based inputs (especially the different
41 replacement rates of alternative or waste materials) in the quantitative methods to predict
42 concrete properties. Also, the independent variables from concrete mixture design can be
43 numeric-based (e.g., Omran et al. [7] and Chithra et al. [8]) or relative-based (e.g., Topçu and
44 Saridemir [9]; Omran et al. [10]). There is very limited research comparing the prediction
45 performance between the two input systems.

46 Previous research (e.g., Atici [6]; Chithra et al. [8]) found that the regression analysis was
47 reliable in predicting concrete strength, but less accurate than Artificial Neural Network (ANN).
48 However, the multivariate regression analysis approach has its advantages by not requiring
49 programming or additional time for model training, being able to generate easy-to-use
50 regression constants, and capable of estimating the significance of input variables. So far, the
51 regression analysis has not been thoroughly explored in concrete mixture design, particularly in
52 the use of non-linear or mixed models, which could be a better-fit [11].

53 The contributions of this research lie in: 1) to propose and test non-linear and mixed
54 regression models as an alternative approach to the traditionally linear method in predicting
55 concrete strength; 2) to adopt a complete set of mixture-design-related variables for modeling

56 environmentally friendly concrete; 3) to compare the prediction performance by using the
57 numerical and relative input methods in a comprehensive set of statistical models; and 4) to
58 provide a statistical guide on studying the effects of alternative/waste materials on concrete
59 strength at different curing ages. This research also compares the performance of non-linear
60 and mixed methods with existing approaches including ANN and other data mining methods.

61 The remainder of this paper is organized as follows. Section 2 provides the background
62 information on the study area. Section 3 describes materials used in the experiment,
63 experimental design, and the proposed statistical models. Section 4 presents the prediction
64 performance of the tested models and other statistical analysis results. Section 5 discusses the
65 robustness of non-linear and mixed models in predicting sustainable concrete strength, and
66 Section 6 concludes this paper.

67 **2. Background**

68 *2.1. Concrete mixture design*

69 Concrete contains four basic ingredients: cement, water, fine aggregate, and coarse
70 aggregate. Chemical admixtures such as air-entraining admixture (AEA) could also be added
71 into concrete to achieve varied properties. In the concrete industry, guidelines are usually used
72 for designing concrete mixtures and the overdesign factor is statistically determined by
73 experimental data or calculated based on some formulas when no sufficient data is available
74 [12]. Internationally, the concrete mixture design approach can be divided into two major
75 systems: numerical and relative systems. Examples of numerically featured mixture design
76 include the Absolute Volume Method introduced in ACI 211 [13] and the Design of Normal
77 Concrete Mixes described in Building Research Establishment [14]. The relative system-based
78 mixture design includes the Equal Paste Volume method [15], which considers the mix
79 proportion of concrete including the water to binder ratio, paste to aggregate ratio, and sand to
80 coarse aggregate ratio.

81 The early market survey [4] of U.S. concrete suppliers and prefabricators nationwide
82 confirmed that most of industry practitioners (81% of totally 39 survey respondents) used
83 industry guidelines and standards for concrete mixture design. In addition, using companies'
84 historical data and other methods such as trial batches were mentioned by 68% and 19% of
85 respondents, respectively. Among various methods applied by the industry, there are limited

86 applications of quantitative methods (e.g., statistical tools) in modeling or predicting how the
87 mixture design affects concrete properties. According to some existing studies [6, 16, 17],
88 quantitative methods have great potential to be used in the concrete mixture design. This will
89 benefit concrete companies that may have limited budgets but need to investigate mix
90 proportions to obtain the desired concrete strength [6, 18]. In addition, the compressive strength
91 (CS) of concrete during the early curing age is usually unknown, but this information is of great
92 importance to the structure to be built as well as site operations [6].

93 2.2. Sustainable concrete

94 Producing conventional concrete utilizes huge amounts of natural resources (e.g., sand and
95 rock) while generating significant energy and environmental impacts from manufacturing of
96 Portland cement (PC) [4]. Environmentally friendly or sustainable concrete refers to concrete
97 with lowered life cycle environmental impact by having conventional ingredients replaced with
98 recycled waste materials, locally available materials, or alternative materials associated with
99 lower greenhouse gas emissions or having concrete properties (e.g., durability) improved. In the
100 U.S. concrete industry, the top three most commonly used supplementary cementitious
101 materials (SCMs) had been identified as FA, silica fume, and ground-granulated blast-furnace
102 slag (BFS) based on the market surveys of both Jin et al. [4] and Obla [19]. The applied
103 alternative aggregates were limited to LWA and recycled concrete aggregate (RCA) [4].
104 Although various other waste or alternative concrete materials (e.g., Berry et al. [20], Binici [21],
105 Topçu and Boğa [1]) had been studied, they are limited in their industry application due to
106 various reasons such as the lack of abundance of material source or regional availability.

107 Many researchers have performed experimental tests to study the effects of waste or
108 alternative materials on concrete properties, such as the studies of oyster shell [22], RCA [23],
109 and the research of FA Class C and furnace slag [24]. In concrete research, simple linear plots
110 were commonly used (e.g., Basri et al. [25]; Berry et al. [20]; Bondar et al. [26]) to relate the
111 concrete properties (e.g., CS) to a given independent variable (e.g., age). Although there were
112 some limited studies attempting to link concrete properties to multiple independent variables in
113 concrete mixture design with various substitution rates of waste or alternative materials, how the
114 different substitution rates of such materials impact concrete properties was not sufficiently
115 quantified. In addition, the study of concrete properties in relation to an alternative material

116 usually requires a large amount of experimental data, which is not only time-consuming but also
 117 cost-prohibitive. Therefore, most previous studies on environmentally friendly concrete rarely
 118 investigated more than one alternative concrete material (e.g., Bondar [26]; Topçu and Boğa [1];
 119 Yang et al., [22]).

120 *2.3. Prediction methods linking concrete mixture design to strength*

121 It is not new to apply statistical and mathematical models in the research of
 122 cement/concrete related construction materials. Aderibigbe et al. [16] described the relationship
 123 between CS and optimum water to cement ratio (w/c) using a power curve equation for
 124 cement/clay soil mixed blocks. Similarly, some other studies, for example, Topçu and Saridemir
 125 [9], adopted statistical analysis to describe the relationships between concrete properties (i.e.,
 126 strength) and aggregate proportion by using a linear regression equation. In these studies, only
 127 one variable was considered, e.g., w/c or percentage of supplementary aggregate.
 128 Nevertheless, concrete mixture design involves multiple interrelated factors (e.g., w/c and
 129 substitution rate of SCMs). It would be necessary to study how the concrete properties can be
 130 affected at the presence of these factors, i.e., joint effects from the mixture design.

131 Table 1 provides details for a few representative studies that have adopted the linear
 132 regression approach to model the relationship between concrete strength and mixture-design-
 133 related variables. It can be seen that the regression models adopted in these studies had
 134 relatively low determination coefficient (i.e., R^2 value). This level of accuracy appears to be
 135 lower than that achieved by some machine learning techniques [6, 7]. As pointed out by St-
 136 Pierre [11], the traditional simple regression methods are likely to generate biased statistical
 137 results and the mixed model methodologies could be applied to provide more accurate
 138 prediction. So far, the non-linear and mixed models have been tried in fields such as biological
 139 engineering [11, 27], but their application in the concrete-materials-related studies is still sparse.

140 **Table 1**
 141 Existing regression models used to predict concrete strength.
 142

Reference	Independent variables	Adopted model	Achieved R^2
Yeh [28]	Cement, FA, BFS, water, superplasticizer, coarse and fine aggregates, and curing age	Linear regression	0.574
Deepa et al. [29]	Cement, BFS, FA, water, superplasticizer, coarse and fine aggregates, and curing age	Linear regression	0.491
Atici [6]	Proportion of BFS, FA, curing age, rebound number	Multiple linear regression analysis (MRA)	0.899
Chou et al. [30]	Cement, FA, BFS, water, superplasticizer,	MRA	0.611

Chithra et al. [8]	coarse and fine aggregate, and curing age Cement, fine and coarse aggregate, silica, slag, superplasticizer	MRA	0.672
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143

144 In literature review, ANN was found to be the most widely used modeling approach in
 145 predicting concrete properties [18, 28, 31, 32, 33, 34, 35, 36]. ANN can automatically build the
 146 relationships between inputs and outputs through a learning algorithm. However, it depends on
 147 software applications and requires larger and more varied training dataset(s) [6]. A few concrete
 148 property studies [37, 38, 39] used fuzzy logic (FL). This method mimics the way of human
 149 thinking to deal with problems caused by the imprecision of source(s) in consideration of
 150 linguistic uncertainties [5, 38]. The use of ANN in predicting concrete properties could be
 151 complicated by the large number of variables [31]. The same problem also applies to FL due to
 152 its characteristics of human-like manner and linguistic rules [38]. Also, statistical models can
 153 handle the inverse problem within concrete mixture design while ANN faces difficulties in
 154 solving such problems [6].

155 3. Materials and Methods

156 3.1. Materials used

157 In this study, PC Type I/II with 28-day CS at 38 MPa, brown sand (fine aggregate), and pea
 158 gravel with maximum size at 9.5 mm (coarse aggregate) were selected as conventional
 159 concrete materials used in the control group of the experimental tests. While PC Type I/II (for
 160 general use) and brown sand are widely used in concrete production, pea gravel, rather than
 161 crushed stones, is more often adopted in lab-based experimental studies. These materials are
 162 locally available in many parts of the world. Unconventional concrete materials used in this
 163 study include PLC Type GUL (General Use Limestone Cement), FA Class F, and Haydite LWA
 164 (Size B, similar to the size of pea gravel). PLC, FA, and LWA were defined as alternative or
 165 waste materials that improve concrete sustainability or environmental friendliness according to
 166 Jin et al. [4] and Omran et al. [7], as they would either reduce the cement carbon footprint, save
 167 materials, or achieve other environmental benefits. In this study, Micro Air was chosen as the
 168 AEA to increase air content in concrete batches.

169 Suppliers provided the Mill Test Reports for PC Type I/II, PLC (GUL), and FA Class F.
 170 Table 2 lists the major elements of these materials. Other minor ingredients such as K₂O in FA

171 and C₃A in PC are not listed. PLC can be produced by intergrinding or blending PC with
 172 limestone, which reduces the carbon footprint of cement manufacturing. The PLC used in this
 173 study was interground with 12% limestone as calculated based on the CO₂ content. The
 174 calculation method was defined in ASTM C150 Standard Specification for Portland Cement [40].

175 **Table 2**
 176 Mill Test Reports of cementitious materials in this study (percentage by weight).
 177

Cementitious material	SiO ₂ (%)	Al ₂ O ₃ (%)	Fe ₂ O ₃ (%)	CaO (%)	MgO (%)	SO ₃ (%)	Alkalis (%)	Loss on ignition (%)	Autoclave expansion (%)
PC	20.1	5.0	3.3	63.2	2.4	2.6	0.56	2.0	0.02
PLC	18.4	4.6	3.0	59.9	2.9	3.6	0.65	5.2	0.08
FA	43.7	21.0	23.8	5.0	1.0	1.7	1.97	1.5	0.00

178 The chemical analysis of oven dry Haydite is shown in Table 3. The density information of
 179 the three aggregate materials was listed in Table 4. While the loose bulk dry density
 180 information was provided by the suppliers, the oven dry density and specific gravity were
 181 obtained by following the standard test methods described in ASTM C127 for coarse aggregate
 182 [41] and C128 for fine aggregate [42].
 183

184 **Table 3**
 185 Chemical analysis of Haydite (provided by the supplier).
 186

Item	SiO ₂	Al ₂ O ₃	Fe ₂ O ₃	CaO	MgO	SO ₃	Na ₂ O	K ₂ O	TiO ₂	P ₂ O ₅	Mn ₂ O ₃	SrO	Cr ₂ O ₃	ZnO
Weight (%)	60.36	19.95	8.09	2.41	2.40	0.13	0.92	4.58	0.96	0.11	0.15	0.01	0.03	0.04

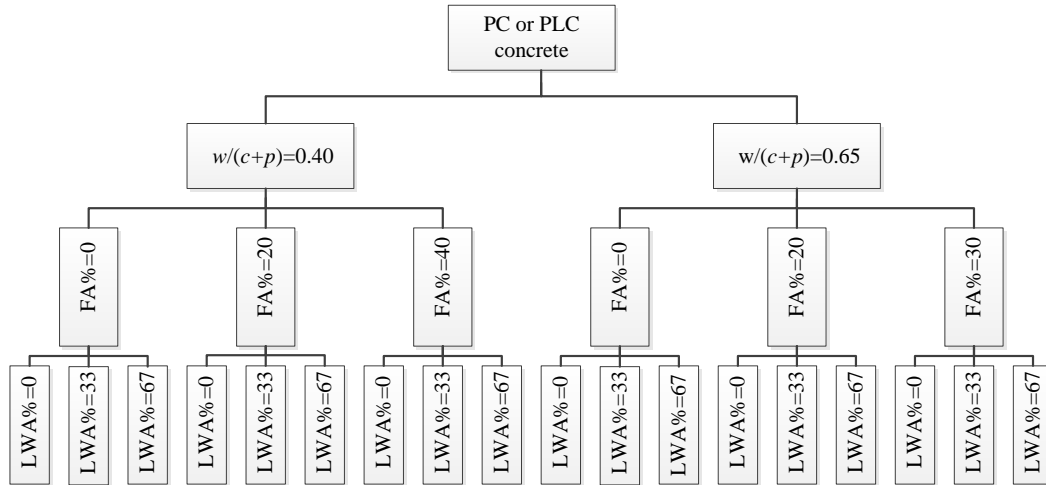
187 **Table 4**
 188 Dry densities of aggregates used in this study.
 189
 190

Type of aggregate	Loose bulk dry density ^a (kg/m ³)	Oven dry density ^b (kg/m ³)	Specific gravity ^c	Fineness modulus
Pea gravel	1602	2643	2.64	6.01
Haydite Size B	673	1298	1.30	5.39
Brown sand	1602	2611	2.61	2.48

191 ^aLoose bulk dry density is the mass of dry aggregate per unit volume of aggregate particles, including the
 192 volume of impermeable pores and water-filled voids within the particles, and the pores between the
 193 particles.
 194 ^bOven dry density is defined by ASTM C127 and C128 as the mass of oven dry aggregate per unit volume
 195 of aggregate, including the volume of impermeable pores and water-filled voids within the particles but
 196 excluding pores between particles.
 197 ^cSpecific gravity (or relative density), according to ASTM C127 and C128, is the ratio of the oven dry
 198 density of the material to the density of distilled water (assuming 1000 kg/m³).
 199

200 3.2. Experimental design

201 The mixture design incorporating different proportions of waste or alternative materials is
 202 displayed in Fig. 1.



203
204
205
206

Fig. 1. Mixture design (36 batches).

207
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219

The 36 batches represent combinations of different cement types (i.e., PC or PLC), $w/(c+p)$ (water to cementitious material weight) ratios, substitution rates of FA Class F (FA%) by weight of the cementitious material, and replacement rates of Haydite to pea gravel by volume. This study implemented both a lower $w/(c+p)$ ratio (0.40) and a higher $w/(c+p)$ ratio (0.65), which are typically used in concrete mixture design to meet different quality requirements (e.g., strength and durability). Having at least two different ratios was also necessary for the statistical analysis as $w/(c+p)$ is one of the key independent variables in the relative system. The making, pouring, and curing of concrete followed the guideline of ASTM C31/C31M-06 [43]. Strength tests were based on 10 mm by 20 mm cylinders casted in single used plastic molds, cured at room temperature (23 °C), and tested at different ages including 3, 7, 28 and 90 days. CS and split tensile strength (TS) tests followed ASTM C39/C39–05 [44] and ASTM C 496/C496M-11 [45], respectively. The mixture design details can be found in Table 5.

220 **Table 5**
 221 Design of concrete mixture proportions.
 222

Cement type	Mixture batch			Ingredients per cubic meter of concrete							
	w/(c+p) ratio	FA (%)	Haydite (%)	Water (kg)	Cement (kg)	FA (kg)	Sand (kg)	Pea gravel (kg)	Haydite (kg)	Micro air (ml)	
PC	0.4	0	0	211	528	0	742	750	0	135	
			33	211	528	0	742	504	121	135	
			67	211	528	0	742	247	247	135	
		20	0	211	422	106	742	750	0	135	
			33	211	422	106	742	504	121	135	
			67	211	422	106	742	247	247	135	
		40	0	211	317	211	742	750	0	135	
			33	211	317	211	742	504	121	135	
			67	211	317	211	742	247	247	135	
	0.65	0	0	211	324	0	902	750	0	112	
			33	211	324	0	902	504	121	112	
			67	211	324	0	902	247	247	112	
		20	0	211	259	65	742	750	0	112	
			33	211	259	65	742	504	121	112	
			67	211	259	65	742	247	247	112	
		30	0	211	227	97	742	750	0	112	
			33	211	227	97	742	504	121	112	
			67	211	227	97	742	247	247	112	
	PLC	0.4	0	0	211	528	0	742	750	0	135
				33	211	528	0	742	504	121	135
				67	211	528	0	742	247	247	135
			20	0	211	422	106	742	750	0	135
				33	211	422	106	742	504	121	135
				67	211	422	106	742	247	247	135
40			0	211	317	211	742	750	0	135	
			33	211	317	211	742	504	121	135	
			67	211	317	211	742	247	247	135	
0.65		0	0	211	324	0	902	750	0	112	
			33	211	324	0	902	504	121	112	
			67	211	324	0	902	247	247	112	
		20	0	211	259	65	742	750	0	112	
			33	211	259	65	742	504	121	112	
			67	211	259	65	742	247	247	112	
		30	0	211	227	97	742	750	0	112	
			33	211	227	97	742	504	121	112	
			67	211	227	97	742	247	247	112	

223

224 *3.3 Non-linear and mixed regression models in predicting concrete strength*

225 This research aimed to explore the potential relationship between sustainable concrete strength
 226 and input variables (i.e., concrete mixture-based variables and curing age) by applying
 227 statistical models. Besides the conventional linear regression model, introduced as Model 1 in
 228 Eq. (1), this research proposed alternative non-linear and mixed models to improve the
 229 determination coefficient when predicting concrete strength based on the mixture-design-related
 230 variables. These models range from Model 2 to Model (2k + 3) in Eqs. (2)-(5), where k denotes
 231 the number of independent predictor variables (IPVs) in the regression model (it is 9 and 8 for
 232 the numerical and relative input methods, respectively). The equations for all of these models
 233 are displayed below:

234 *Model 1: Multi-linear regression analysis*

$$Y_i = \alpha + \sum_{j=1}^k \beta_j X_{ij}, \quad i = 1, \dots, n \quad (1)$$

235

236 *Model 2: A non-linear model involving natural logarithms*

$$\ln Y_i = \alpha + \sum_{j=1}^k \beta_j X_{ij}, \quad i = 1, \dots, n \quad (2)$$

237

238 *Model 3: A second type of non-linear model involving natural logarithms*

$$\ln Y_i = \alpha + \sum_{j=1}^k \beta_j \ln X_{ij}, \quad i = 1, \dots, n \quad (3)$$

239

240 *Mixed models from (4) to (k+3)*

$$\frac{X_{ij}}{Y_i} = \alpha + \sum_{l=1}^k \beta_l X_{il}, \quad i = 1, \dots, n, \quad j = 1, \dots, k \quad (4)$$

241

242 *k mixed models with natural logarithm*

$$\frac{\ln X_{ij}}{Y_i} = \alpha + \sum_{l=1}^k \beta_l \ln X_{il}, \quad i = 1, \dots, n, \quad j = 1, \dots, k \quad (5)$$

243

244 **In these models, X_{ij} represents k IPVs such as curing age, Y_i is the response random**
245 **variable (RRV) referring to CS or TS, and $\alpha, \beta_1, \dots, \beta_k$ denote constants.** Only Model 1 from the
246 above $(2k+3)$ models is linear, and all the remaining non-linear or mixed relationships were
247 converted into linear formats. The statistics software, Minitab, was used to analyze these $(2k+3)$
248 models. The values of R^2 and residual standard deviation were generated to compare the
249 accuracy of these models in predicting each target RRV. The F and p values generated from
250 Analysis of Variance (ANOVA) were used to test the significance of the selected regression
251 model (at 95% level of significance) in describing the data samples. The null hypothesis is that
252 the target RRV cannot be predicted by using the selected model with the chosen IPVs. A p
253 value less than 0.05 from ANOVA would reject the null hypothesis and indicate that the selected
254 regression model fits the data. Residual analysis was also conducted in Minitab to study the
255 distribution and values of residuals, which were the differences between predicted RRV and

256 experimental data. The Durbin-Watson statistical test is based on the null hypothesis that
 257 residuals from a least-square regression are not autocorrelated [46]. The Durbin-Watson value
 258 ranges from 0 to 4, and a value near 2 indicates non-autocorrelation. The ideal Durbin-Watson
 259 value would fall between 1.5 and 2.5 [6, 8].

260 Among the k IPVs, some may have more significant effects on the target RRV than others.
 261 The t -test of correlation analysis was used to determine the significance regarding the effect of
 262 each IPV on RRV . There is a p value corresponding to each t value for an IPV. At the 95%
 263 confidence level, a p value lower than 0.05 would indicate that this selected IPV has significant
 264 contribution to RRV . In contrast, IPVs with p values higher than 0.05 are those without
 265 significant contributions. The reason that some IPVs had higher significance than others could
 266 be due to the strong internal correlation among IPVs, which caused redundancy of IPVs.
 267 Therefore, the regression analysis could be redone by removing the insignificant IPVs so that
 268 the equation can be shortened with only significant IPVs. Target $RRVs$ (CS and TS) and various
 269 IPVs using both numerical and relative input systems are defined in Table 6.

270 **Table 6**
 271 Definitions of $RRVs$ and IPVs in the numeric and relative systems.
 272

Variables	Definitions	
	Numeric system	Relative system
Y_i	Concrete CS (MPa) or TS (MPa)	Concrete CS (MPa) or TS (MPa)
X_{i1}	Concrete age (days)	Concrete age (days)
X_{i2}	W (kg): Amount of water used in the mixture of per m^3 of concrete	$w/(c+p)$: Water-cementitious material ratio
X_{i3}	PC (kg): Amount of PC used in the mixture of per m^3 of concrete	PLC%: Replacement of PLC to PC*
X_{i4}	PLC (kg): Amount of PLC used in the mixture of per m^3 of concrete	FA%: FA substitution rate in cementitious material
X_{i5}	FA (kg): Amount of FA used in the mixture of per m^3 of concrete	LWA%: Haydite LWA substitution rate in coarse aggregate
X_{i6}	S (kg): Amount of sand used in the mixture of per m^3 of concrete	$S/(c+p)$: Weight ratio of sand to cementitious material
X_{i7}	CA (kg): Amount of coarse aggregate used in the mixture of per m^3 of concrete	S/CA : Volume ratio of sand to coarse aggregate
X_{i8}	LWA (kg): Amount of Haydite used in the mixture of per m^3 of concrete	Unit AEA (ml): Amount of air entrainment (ml) per 100 kg of cement (AEA)
X_{i9}	AEA (ml): Amount of air entrainment used in the mixture of per m^3 of concrete	N.A.

273 *: X_{i3} in the relative system is a binary value, with its value at 0 when using PC and 1 when PLC is used.
 274

275 4. Results

276 In this study, the two major input systems within concrete mixture design (i.e., numerical and
 277 relative input systems) were compared for their accuracy in predicting concrete strength. The
 278 best-fit models were identified under each input system. By removing significantly correlated

279 IPV within each input system, the regression modeling process was rerun by shortlisting.
 280 Finally, the whole data sample was divided by different curing ages to study the effects of each
 281 IPV on concrete strength at various ages.

282 *4.1. Comparison between the numerical and relative input systems*

283 The regression analysis for both CS and TS was conducted based on the trial of 21 and 19
 284 proposed models for numerical and relative input systems, respectively. The reliability of these
 285 models was compared, and the best-fit model was identified for each of the four scenarios, i.e.,
 286 concrete CS and TS in these two input systems. Table 7 displays the corresponding R^2 values
 287 for all CS and TS prediction using both systems.

288 **Table 7**
 289 Statistical modeling results in the numerical and relative systems.
 290

Statistical approach	Model no.	Predication of CS				Predication of TS			
		Numerical system		Relative system		Numerical system		Relative system	
		RRV	R^2	RRV	R^2	RRV	R^2	RRV	R^2
Linear	1	CS	0.907	CS	0.901	TS	0.764	TS	0.775
Non-linear	2	ln(CS)	0.876	ln(CS)	0.878	ln(TS)	0.732	ln(TS)	0.748
	3	ln(CS)	0.953*	ln(CS)	0.934*	ln(TS)	0.866	ln(TS)	0.836
Mixed models	4	Age/CS	0.932	Age/CS	0.933	Age/TS	0.952*	Age/TS	0.955*
	5	W/CS	0.740	(w/(c+p))/CS	0.807	W/TS	0.626	(w/(c+p))/TS	0.774
	6	PC/CS	0.823	PLC%/CS	0.823	PC/TS	0.899	PLC%/TS	0.859
	7	PLC/CS	0.813	FA%/CS	0.832	PLC/TS	0.878	FA%/TS	0.873
	8	FA/CS	0.839	LWA%/CS	0.816	FA/TS	0.890	LWA%/TS	0.868
	9	S/CS	0.788	(S/(c+p))/CS	0.830	S/TS	0.726	(S/(c+p))/TS	0.814
	10	CA/CS	0.822	(S/CA)/CS	0.793	CA/TS	0.818	(S/CA)/TS	0.736
	11	LWA/CS	0.874	Unit AEA/CS	0.772	LWA/TS	0.874	Unit AEA/TS	0.694
	12	AEA/CS	0.698	ln(Age)/CS	0.906	AEA/TS	0.632	ln(Age)/TS	0.884
	13	ln(Age)/CS	0.914	ln(w/(c+p))/CS	0.839	ln(Age)/TS	0.900	ln(w/(c+p))/TS	0.804
	14	ln(W)/CS	0.859	ln(PLC%)/CS	0.841	ln(W)/TS	0.798	ln(PLC%)/TS	0.902
	15	ln(PC)/CS	0.838	ln(FA%)/CS	0.822	ln(PC)/TS	0.904	ln(FA%)/TS	0.898
	16	ln(PLC)/CS	0.837	ln(LWA%)/CS	0.862	ln(PLC)/TS	0.901	ln(LWA%)/TS	0.890
17	ln(FA)/CS	0.862	ln(S/(c+p))/CS	0.879	ln(FA)/TS	0.911	ln(S/(c+p))/TS	0.878	
18	ln(S)/CS	0.861	ln(S/CA)/CS	0.884	ln(S)/TS	0.804	ln(S/CA)/TS	0.898	
19	ln(CA)/CS	0.881	ln(Unit AEA)/CS	0.846	ln(CA)/TS	0.881	ln(Unit AEA)/TS	0.771	
20	ln(LWA)/CS	0.841	N/A	N/A	ln(LWA)/TS	0.895	N/A	N/A	
21	ln(AEA)/CS	0.857	N/A	N/A	ln(AEA)/TS	0.782	N/A	N/A	

291 *Model that achieves the highest R^2 value for the given scenario.
 292

293 As shown in Table 7, both numerical and relative input systems led to highly consistent R^2
 294 values (similar prediction accuracy) from Models 1 to 4 for predicting CS. Model 4, the mixed
 295 model using *Age/Strength* as the RRV achieved the consistently high R^2 values for all the four
 296 scenarios. All the corresponding Durbin-Watson values in the 16 scenarios are within the
 297 reasonable range (i.e., 1.5 to 2.5). Model 4 also achieved the highest R^2 value for the

298 predication of TS in both systems. In the CS-related RRV regression analysis, Model 3 (the
 299 non-linear approach) represents the best-fit model by achieving even higher accuracy than
 300 Model 4, the highest based on both input systems. The remaining mixed models had relatively
 301 lower R^2 values for both input systems. The R^2 values resulting from the best-fit non-linear and
 302 mixed regression models in this research (ranging from 0.934 to 0.955) are significantly higher
 303 than the values generated from previous studies adopting linear methods as shown in Table 1.
 304 The accuracy level of these regression models is also comparable to that achieved by data
 305 mining techniques in Omran et al. [7] when the same dataset for CS was used.

306 4.2. Regression analysis using the best-fit models

307 Although both numerical and relative input systems had highly consistent R^2 values for the
 308 best-fit models, the former is deemed more practical for field applications due to the wide
 309 adoption of the numerically featured ACI method of mix design [13] in North America and many
 310 parts of the world. Due to space limitations, this section only showcases the best-fit models for
 311 predicting CS and TS based on the numerical input system. However, the modeling process
 312 and outcomes of the best-fit models based on the relative input system are expected to be
 313 similar.

314 Compared to the R^2 values (0.907 and 0.763 for CS and TS, respectively) associated with the
 315 linear approach (Model 1), the best-fit non-linear (i.e., Model 3) and mixed (i.e. Model 4) models
 316 performed superiorly. Model 3 in the regression analysis for CS provided the highest correlation
 317 with R^2 value at 0.953 (followed by Model 4 with R^2 value at 0.932) while Model 4 achieved the
 318 highest accuracy with R^2 value at 0.952 for predicting TS. The two equations generated from
 319 Models 3 and 4 are listed below:

320 For predicting CS

$$321 \ln Y_i = 6.520 + 0.212 \ln X_{i1} - 0.056 \ln X_{i2} + 0.808 \ln X_{i3} + 0.817 \ln X_{i4} \\ + 0.006 \ln X_{i5} - 0.775 \ln X_{i6} + 0.014 \ln X_{i7} - 0.009 \ln X_{i8} + 0.177 \ln X_{i9} \quad (6)$$

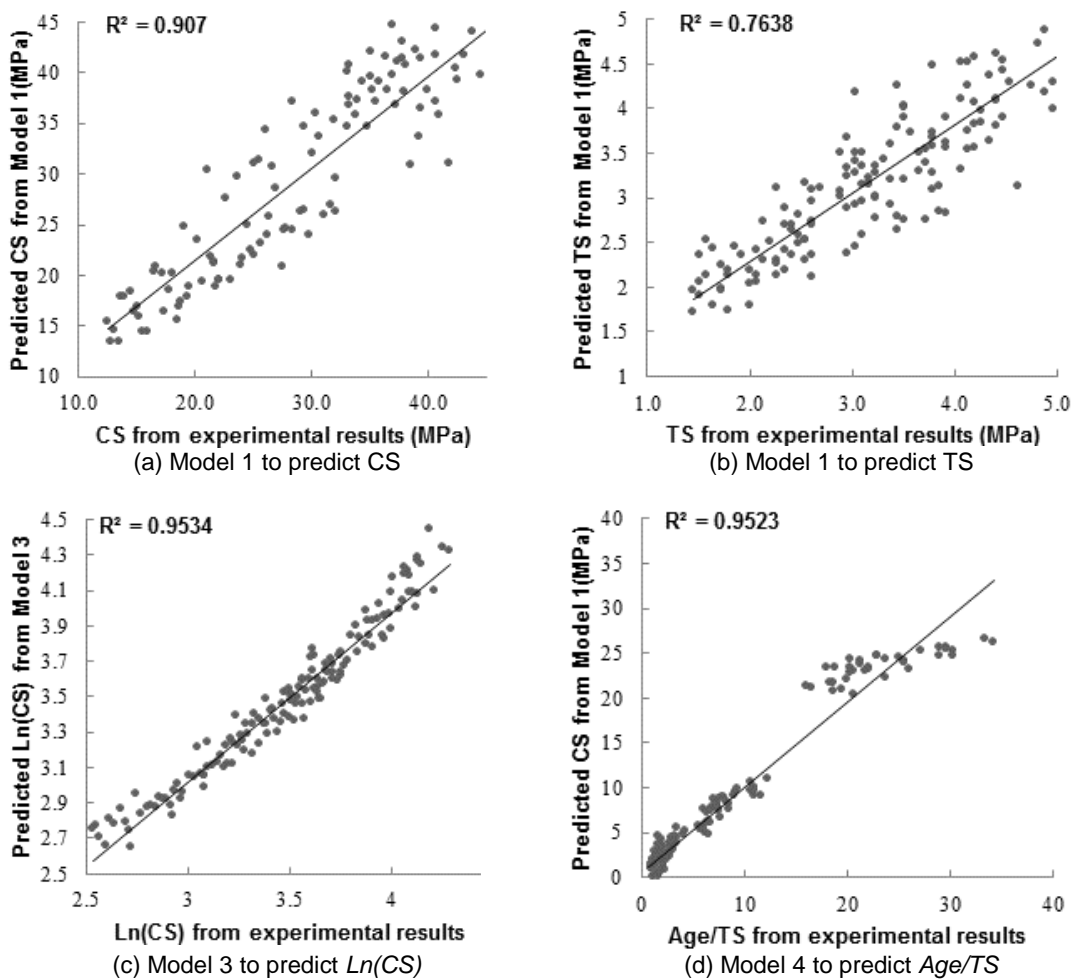
322 For predicting TS

$$323 X_{i1}/Y_i = -12.500 + 0.252 X_{i1} + 0.012 X_{i2} - 0.003 X_{i3} - 0.008 X_{i4} - 0.001 X_{i5} + 0.010 X_{i6} \\ + 0.007 X_{i7} + 0.016 X_{i8} - 0.005 X_{i9} \quad (7)$$

324 Fig. 2 shows the comparison between the predicted RRVs and experimental results. The R^2
 325 values over 0.950 in Figs. 2(c) and 2(d) indicate the high accuracy of the identified best-fit

326 models (i.e., Model 3 for the CS-related RRV and Model 4 for the TS-related RRV) in predicting
 327 concrete strength-related RRVs. Model 4, which sets Age/TS as the RRV, tends to be non-
 328 continuous as compared to Model 3 due to the large variation of curing age (i.e., Day 3, 7, 28
 329 and 90) involved in the RRV. The discontinuous nature of RRV in the mixed model would also
 330 affect the residual distribution. As a comparison, the R^2 performance of Model 1, the linear
 331 regression approach, is also displayed in Figs. 2(a) and 2(b). It can be observed that compared
 332 to the linear approach, non-linear and mixed methods improved the prediction accuracy of
 333 concrete strength-based RRVs.

334



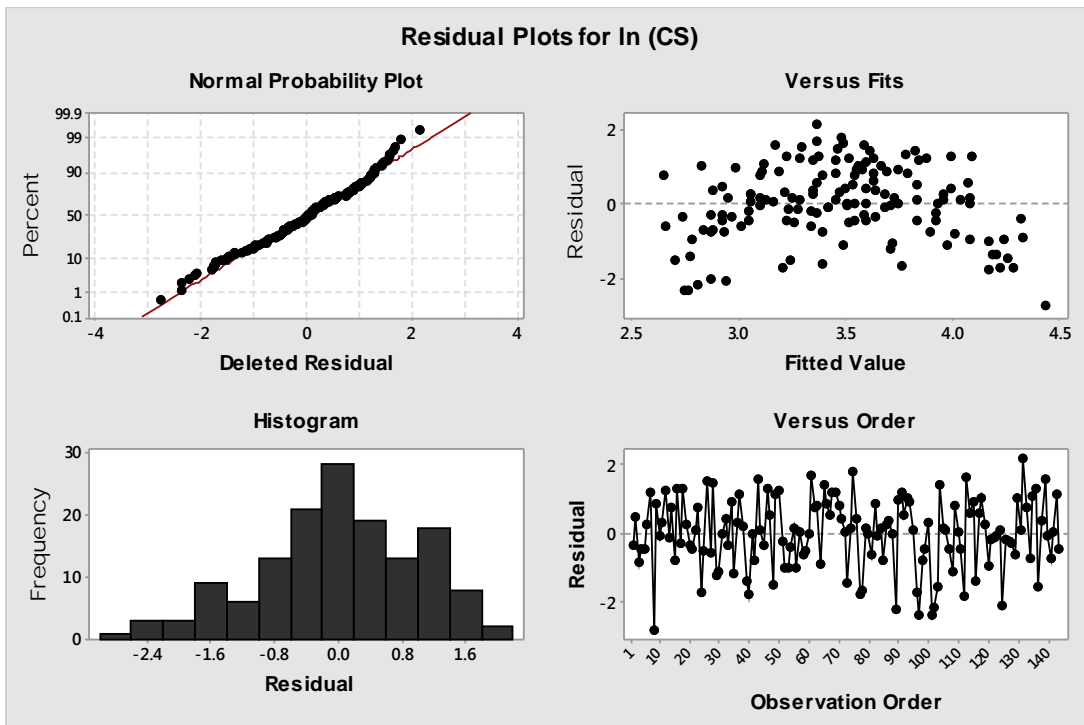
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Fig. 2. Comparison between predicted RRV and experimental data using linear regression analysis and best-fit models.

340 Residual analysis for the best-fit models was conducted in Minitab. Fig. 3 illustrates the
 341 residual analysis results for $ln(CS)$ from Model 3. The residual values of Model 3 applied in

342 $\ln(\text{CS})$ analysis presented satisfactory trends of normal distribution as shown in both the normal
 343 probability plot and histogram. The residual values appeared symmetrically distributed along the
 344 neutral horizontal line (when the residual is 0) and were not affected by the increase of fitted
 345 values. The observation order in Fig. 3 is corresponding to the growth of concrete age; there
 346 were 36 observations for each of the four concrete ages (i.e., Day 3, 7, 28, and 90). Generally,
 347 the residual was not affected by curing age as well. Similar distribution of residual values in
 348 Model 3 could be found when applied in the relative system.

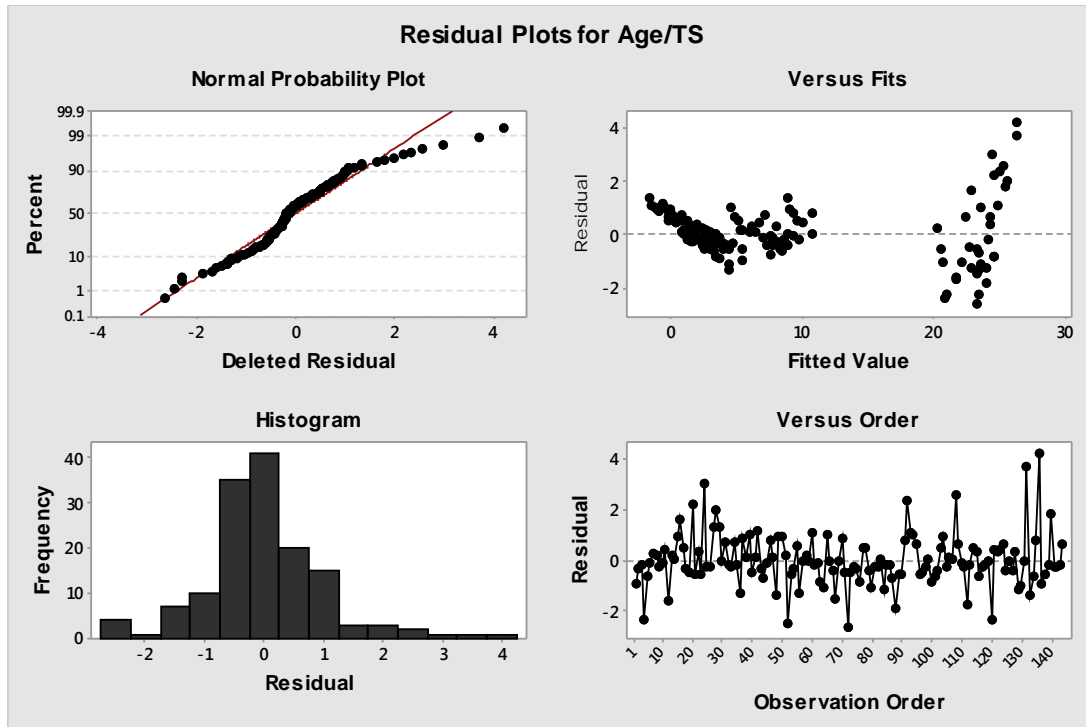
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Fig. 3. Residual analysis of Model 3 in predicting $\ln(\text{CS})$.

355 For Model 4 applied in TS, the residual distribution displayed in Fig. 4 shows less symmetry
 356 along the neutral line. Corresponding to the larger variation nature of Age involved in the RRV,
 the residual value in Model 4 tends to grow with the RRV value.



357

358 **Fig. 4.** Residual analysis of Model 4 in predicting *Age/TS*.

359

360 *4.3. Internal correlation analysis of IPVs based on the best-fit model*

361

This section uses Model 3 in CS to demonstrate the internal correlation analysis of IPVs and regression analysis with shortened IPVs. Pearson correlations and corresponding *p* values displayed in Table 8 indicate the correlations among mixture-design-related IPVs. Curing age was found independent of any other mixture-based IPVs, and sand amount had significantly negative correlation with CA amount. Therefore, only one IPV between sand and CA amounts needs to be kept for the shortened input variables. This study purposely kept IPVs related to the studied alternative or waste materials to capture their effects on concrete properties, which fits the research goals.

368

369

Table 8.

370

Pearson correlations among nine IPVs.

371

		1	2	3	4	5	6	7	8	9
1. ln(Age)	Correlation	1.000								
	<i>p</i> value	0.000								
2. ln(W)	Correlation	0.000	1.000							
	<i>p</i> value	1.000	0.000							
3. ln(PC)	Correlation	0.000	-0.207	1.000						
	<i>p</i> value	1.000	0.013*	0.000						
4. ln(PLC)	Correlation	0.000	0.237	-0.999	1.000					
	<i>p</i> value	1.000	0.004*	0.000*	0.000					
5. ln(FA)	Correlation	0.000	-0.375	-0.013	-0.014	1.000				
	<i>p</i> value	1.000	0.000*	0.876	0.867	0.000				
6. ln(S)	Correlation	0.000	-0.597	0.033	-0.071	0.011	1.000			
	<i>p</i> value	1.000	0.000*	0.876	0.395	0.894	0.000			

7. ln(CA)	Correlation	0.000	-0.086	-0.010	0.012	0.321	-0.177	1.000		
	<i>p</i> value	1.000	0.307	0.905	0.891	0.000*	0.034*	0.000		
8. ln(LWA)	Correlation	0.000	0.081	0.007	-0.009	-0.008	-0.036	-0.347	1.000	
	<i>p</i> value	1.000	0.333	0.938	0.914	0.927	0.666	0.000*	0.000	
9. ln(AEA)	Correlation	0.000	0.522	-0.085	0.120	-0.028	-0.855	0.208	-0.103	1.000
	<i>p</i> value	1.000	0.000*	0.313	0.152	0.742	0.000*	0.012*	0.221	0.000

*Significant correlations between two IPVs with *p* values less than 0.05.

372
373

374 Table 9 displays the regression analysis results of Model 3 for both nine IPVs and
375 shortened IPVs. In the secondary run of Model 3, all the five kept IPVs showed significant
376 influences on RRV (i.e., ln(CS)), with age having the most significant contribution according to
377 its corresponding *t* value (24.28). The negative coefficient values corresponding to FA, sand,
378 and LWA indicate that these three materials would generally reduce concrete CS. In contrast,
379 PLC is indicated to increase concrete CS based on the positive coefficient value and low *p*
380 value at 0.001. It is also worth noting that the shortlisted IPVs in the secondary run of Model 3
381 resulted in only slightly lower *R*² at 0.907 and slightly higher residual standard deviation.
382 However, the Durbin-Watson value fell out of the ideal range between 1.5 and 2.5. In
383 comparison, the mixed model (i.e., Model 4) turns out to have a superior Durbin-Watson value
384 when keeping only the same five shortlisted input variables.

385 **Table 9.**
386 Non-linear regression analysis results from Model 3.
387

Response	Predictor	Coefficient analysis			Residual Standard Deviation	<i>R</i> ²	ANOVA		Durbin- Watson value
		Coefficient	<i>t</i> value	<i>p</i> value			<i>F</i> value	<i>p</i> value	
ln(CS)	Constant	6.520	3.13	0.002	0.098	0.953	304.69	0.000	1.906
	ln(Age)	0.212	33.94	0.000					
	ln(W)	-0.056	-0.43	0.669*					
	ln(PC)	0.808	9.00	0.000					
	ln(PLC)	0.817	9.07	0.000					
	ln(FA)	0.006	1.68	0.096*					
	ln(S)	-0.775	-3.37	0.001					
	ln(CA)	0.014	3.69	0.000					
	ln(LWA)	-0.009	-4.56	0.000					
	ln(AEA)	0.177	3.11	0.002					
ln(CS)	Constant	21.890	29.14	0.000	0.136	0.906	266.86	0.000	1.405
	ln(Age)	0.212	24.28	0.000					
	ln(PLC)	0.007	3.27	0.001					
	ln(FA)	-0.016	-6.47	0.000					
	ln(S)	-2.819	-25.23	0.000					
	ln(LWA)	-0.017	-6.92	0.000					

**p* value higher than 0.05 indicating less significant of the target predictor on concrete-strength-based response.

388
389
390

391 4.4. Subsamples at different curing ages

392 Continuing the work in Jin [47] where experimental observations were obtained on the
 393 waste or alternative materials' effects on concrete properties at different curing ages, this study
 394 provided the statistical approach to test these observations. Based on the shortened IPV list
 395 from Section 4.3, the totally 144 observations were divided into subsamples according to the
 396 curing age (i.e., Day 3, 7, 28, and 90) to analyze the effects of multiple alternative or waste
 397 materials on concrete strength as concrete ages. Table 10 displays the data analysis results by
 398 rerunning Model 3 as the example.

399 **Table 10.**
 400 Non-linear regression analysis results from Model 3.
 401

Response	Predictor	Coefficient analysis			Residual Standard Deviation	R^2	ANOVA		Durbin- Watson value
		Coefficient	t value	p value			F value	p value	
ln(CS) in Day 3	ln(PLC)	0.006	1.02	0.314*	0.170	0.843	41.5	0.000	1.784
	ln(FA)	-0.019	-2.96	0.006					
	ln(S)	-3.362	-12.08	0.000					
	ln(LWA)	-0.019	-3.09	0.004					
ln(CS) in Day 7	ln(PLC)	0.009	2.12	0.042	0.134	0.873	53.21	0.000	1.723
	ln(FA)	-0.022	-4.27	0.000					
	ln(S)	-2.871	-13.06	0.000					
	ln(LWA)	-0.020	-4.09	0.000					
ln(CS) in Day 28	ln(PLC)	0.009	2.61	0.014	0.110	0.895	65.8	0.000	1.625
	ln(FA)	-0.020	-4.88	0.000					
	ln(S)	-2.640	-14.65	0.000					
	ln(LWA)	-0.014	-3.60	0.001					
ln(CS) in Day 90	ln(PLC)	0.005	1.37	0.179*	0.170	0.873	53.33	0.000	2.056
	ln(FA)	-0.006	-1.44	0.160*					
	ln(S)	-2.402	-13.89	0.000					
	ln(LWA)	-0.015	-3.97	0.000					

402 * p value higher than 0.05 indicating less significant of the target predictor on concrete-strength-based
 403 response.

404
 405 The coefficient analysis in Table 10 conveys the information that the three adopted
 406 alternative or waste materials (i.e., PLC, FA, and LWA) tended to have significant effects on
 407 concrete strength at different curing ages with a few exceptions. Overall PLC increased
 408 concrete CS while FA and LWA decreasing CS. Consistent R^2 and ANOVA analysis results
 409 were also found in Model 3 when applied in the four different concrete ages. The Durbin-
 410 Watson values all fell into the ideal range. However, compared to early ages, the effects of FA
 411 and PLC in Day 90 tended to be less significant with corresponding p values higher than 0.05.
 412 This would indicate that FA and PLC tended to more strongly affect concrete strength in earlier
 413 ages (i.e., Day 7 and Day 28), but the long-term strength of sustainable concrete would be more
 414 comparable to that of conventional concrete. This statistical finding was consistent with and

415 supported by earlier studies [47] when comparing the concrete strength between sustainable
 416 concrete and conventional concrete using bar chart illustration. The TS-related numerical or
 417 relative system also led to consistent findings.

418 **5. Discussion**

419 Although only Model 3's statistical performance was demonstrated in this paper in detail,
 420 Model 4, when applied in either TS-related numerical or relative system, was also found to have
 421 consistent results following the procedures described in Sections 4.3 and 4.4. This suggests the
 422 robustness of non-linear and mixed models in predicting concrete mechanical properties based
 423 on both numerical and relative systems. Although non-linear models might not have ideal
 424 Durbin-Watson value when IPV was shortlisted, and mixed models might not have ideal
 425 distribution of residual values due to the scattering nature of the "mixed" RRV, these problems
 426 could be solved by identifying the appropriate list of IPV's and selecting the proper model from
 427 the 21 models defined in Table 7.

428 The non-linear and mixed models adopted in this study have the potential to serve as an
 429 alternative to existing methods in predicting concrete strength based on mixture design
 430 variables with alternative or waste materials involved. **Generally, the non-linear and mixed**
 431 **models achieved higher accuracy than the linear regression approach in predicting concrete**
 432 **strength as proved in this study and by the comparison with previous studies (Table 7 versus**
 433 **Table 1).** Also, as shown in Table 11, compared with ANN and other data mining methods, the
 434 best-fit non-linear and mixed models proposed in this research achieved similar prediction
 435 performance based on both the numerical and relative input systems while having advantages
 436 of being less time-consuming in model creation and allowing the analysis of individual materials'
 437 effects on concrete strength at different curing ages.

438 **Table 11**
 439 Existing studies that used advanced or non-linear models to predict concrete strength.
 440

Study	Independent variables	Adopted models	Sample size	R ² result	Findings
Saridemir et al. [5]	BFS, curing age, PC, water, and aggregate	ANN and FL	284	As high as 1.00 for ANN and 0.991 for FL	ANN and FL had strong potential in predicting the CS.
Atici [6]	Proportion of BFS, FA, curing age, rebound number	MRA and ANN	135	As high as 0.98 for ANN and 0.90 for MRA	ANN outperformed MRA in predicting CS. However, MRA has its advantages.

Omran et al. [7]	Amount of individual ingredients in concrete mixture design including PLC, FA, and LWA	Nine different data mining methods including ANN, M5P model tree, etc.	144	Highest R^2 value achieved (0.984) by the additive regression method	Four regression tree models improved the prediction accuracy. Other three advanced models achieved higher accuracy, but the time required for building and training these models may be a restraint.
Chithra et al. [8]	Amount of cement, fine and coarse aggregates, nano silica, slag, and superplasticizer	MRA and ANN	264	Around 0.670 for MRA and close to 1.0 for ANN	MRA was found with lower accuracy and less satisfactory in meeting other statistical requirements (Durbin-Watson value) compared to ANN.
This study	Concrete-mixture-design-based inputs in both numeric and relative systems	MRA including linear, non-linear, and mixed models	144	Over 0.950 achieved in both numerical and relative input systems	Both non-linear and mixed models achieved better performance than the linear approach using both input systems. They can also statistically quantify alternative or waste materials' effects on concrete properties at different curing ages.

441

442 6. Conclusions

443 The regression analysis in this study provided a quantitative tool to predict concrete strength
444 purely based on mixture-design-related variables and curing age. This statistical tool has
445 advantages of being easy-to-use and low-cost, not requiring extensive lab testing and huge
446 datasets, and achieving high degree of reliability. The non-linear and mixed models proposed in
447 this research enrich the existing statistical modeling approach, which was usually limited to the
448 linear regression method. The non-linear and mixed models could also serve as an alternative
449 approach to existing data mining methods (e.g., ANN). The major findings of this study are
450 summarized below:

- 451 ▪ The proposed non-linear and mixed regression models achieved higher accuracy
452 compared to the linear method in predicting concrete strength using the same concrete
453 mixture variables and datasets. The best-fit models reached comparably high R^2 values
454 (ranging from 0.934 to 0.955) as some data mining techniques. It is recommended to
455 apply these models to datasets in previous studies to examine their potential in improving
456 the prediction accuracy.
- 457 ▪ Using a comprehensive set of variables from the concrete mixture design including both
458 conventional and alternative/waste materials was found to be viable in predicting the
459 strength of sustainable concrete. It is expected that the list of IPVs could still be expanded

460 when more alternative materials from the cementitious or aggregate parts are added into
461 concrete mixture.

- 462 ▪ Using the two input systems (i.e., numerical and relative) yielded highly consistent R^2
463 values in predicting concrete strength when the same RRV was adopted in the regression
464 models. However, for practical reasons, the more straightforward numerical input system
465 would be preferable as it allows the direct use of variable values from concrete mixture
466 design. Conversion would be needed for the relative input system.
- 467 ▪ Shortening IPV's based on internal correlation analysis would only cause small
468 performance loss when using the best-fit models to predict concrete strength. The
469 corresponding statistical values (e.g., t , p , and coefficient) would better quantify the effect
470 of each remaining IPV on the target RRVs. This research recommends keeping IPV's
471 related to the studied material(s) (e.g., IPV's related to PLC, FA and LWA in this study) in
472 the shortlist. As a result, the effects of studied material(s) on concrete properties could be
473 properly quantified.
- 474 ▪ The non-linear and mixed statistical models could simplify the prediction of concrete
475 strength at certain curing age (e.g., Day 3, 7, or 90). They could also provide the
476 statistical guide on the effects of alternative or waste materials on concrete mechanical
477 properties as concrete age grows.

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482 **References**

- 483 [1] I.B. Topçu, A.R. Boğa, Effect of boron waste on the properties of mortar and concrete,
484 *Waste Manage. Res.* 28 (2010) 626-633.
- 485 [2] D. Bondar, C.J. Lynsdale, N.B. Milestone, N. Hassani, A.A. Ramezani-pour, Engineering
486 properties of alkali-activated natural pozzolan concrete, *ACI Mater. J.* 108 (2011) 64-72.
- 487 [3] M. Limbachiya, M.S. Meddah, Y. Ouchagour, Y. Performance of Portland/silica fume cement
488 concrete produced with recycled concrete aggregate, *ACI Mater. J.* 109 (2012) 91-100.
- 489 [4] R. Jin, Q. Chen., A. Soboyejo, Survey of the current status of sustainable concrete
490 production in the U.S., *Resour. Conserv. Recy.* 105 (PART A) (2015) 148-159.

- 491 [5] M. Saridemir, I.B. Topçu, F. Ozcan, M.H. Severcan, Prediction of long-term effects of
492 GGBFS on compressive strength of concrete by artificial neural networks and fuzzy logic,
493 *Constr. Build. Mater.* 23 (2009) 1279-1286.
- 494 [6] U. Atici, Prediction of the strength of mineral admixture concrete using multivariable
495 regression analysis and an artificial neural network, *Expert. Syst. Appl.* 38 (2011) 9609-9618.
- 496 [7] B.A. Omran, Q. Chen, R. Jin, Comparison of data mining techniques for predicting
497 compressive strength of environmentally friendly concrete, *J. Comput. Civil. Eng.* 30 (6)
498 (2016), DOI: 10.1061/(ASCE)CP.1943-5487.0000596.
- 499 [8] S. Chithra, S.R.R. Senthil Kumar, K. Chinnaraju, F. Alfin Ashmita, A comparative study on
500 the compressive strength prediction models for High Performance Concrete containing nano
501 silica and copper slag using regression analysis and Artificial Neural Networks, *Constr. Build.*
502 *Mater.* 114 (2016) 528-535.
- 503 [9] I.B. Topçu, M. Saridemir, Prediction of properties of waste AAC aggregate concrete using
504 artificial neural network, *Comp. Mater. Sci.* 41 (2007) 117-125.
- 505 [10] B.A. Omran, Q. Chen, R. Jin, 2014, Prediction of compressive strength of “green” concrete
506 using artificial neural networks, in: Proc. of the 50th Annual International Conference of the
507 Associated Schools of Construction, March 26-28, Washington, D.C., USA.
- 508 [11] N.R. St-Pierre, Invited review: Integrating quantitative findings from multiple studies using
509 mixed model methodology, *American Dairy Science Association* 84 (2001) 741-755.
- 510 [12] M. Pardi, PE, LEED GA, Central/SE Ohio Concrete, OCCA. Personal communication,
511 2012.
- 512 [13] American Concrete Institute (ACI) 211.1-91, Standard practice for selecting proportions for
513 normal, heavyweight, and mass concrete—procedure for mix design.
- 514 [14] Building Research Establishment, Design of normal concrete mixes, Second edition [M].
515 Watford, WD2 7JR. 1988.
- 516 [15] H. Lian, Y. Li, Discussion on method for selecting mix proportion of concrete (II), Proposal
517 on selection of factors and method for calculating mix proportion of current concrete,
518 *Concrete* 5 (2009), DOI:10.3969/j.issn.1002-3550.2009.05.001. in Chinese.
- 519 [16] D.A. Aderibigbe, T.A.I. Akeju, C.O. Orangun, Optimal water/cement ratios and strength
520 characteristics of some local clay soils stabilized with cement, *Mater. Constr.* 18 (2) (1985)
521 103-108.
- 522 [17] M.J. Simon, E.S., Lagergren, K.A. Snyder, 1997, Concrete mixture optimization using
523 statistical mixture design methods, in: Proc. of the PCI/FHWA, International Symposium on
524 High Performance Concrete, October 20-22, New Orleans, LA, USA.
- 525 [18] A. Oztas, M. Pala, E. Ozbay, E. Kanca, N. Caglar, M.A. Bhatti MA. Predicting the
526 compressive strength and slump of high strength concrete using neural network, *Constr.*
527 *Build. Mater.* 20 (9) (2006) 769–775.
- 528 [19] K.H., Obla, C.L. Lobo, H. Kim, The 2012 NRMCA supplementary cementitious materials
529 use survey, NRMCA Concrete InFocus Magazine, Fall 2012 edition.

- 530 [20] M. Berry, J. Stephens, D. Cross, D. Performance of 100% fly ash concrete with recycled
531 glass aggregate, *ACI Mater. J.* 108 (4) (2011) 378-384.
- 532 [21] H. Binici. Effect of crushed ceramic and basaltic pumice as fine aggregates on concrete
533 mortars properties, *Constr. Build. Mater.* 21 (6) (2007) 1191–1197.
- 534 [22] E.I. Yang, S.T. Yi, Y.M. Leem, Effect of oyster shell substituted for fine aggregate on
535 concrete characteristics: Part I. Fundamental properties, *Cem. Concr. Res.* 35 (2005) 2175-
536 2182.
- 537 [23] M. Etxeberria, E. Vázquez, A. Marí, M. Barra, Influence of amount of recycled coarse
538 aggregates and production process on properties of recycled aggregate concrete, *Cem.*
539 *Concr. Res.* 37 (2007) 735-742.
- 540 [24] J.T. Kevern, V.R. Schaefer, K. Wang, K. Mixture proportion development and performance
541 evaluation of pervious concrete for overlay applications, *ACI Mater. J.* 108 (4) (2011) 439-
542 448.
- 543 [25] H.B. Basri, M.A. Mannan, M.F.M. Zain, Concrete using waste oil palm shells as aggregate,
544 *Cem. Concr. Res.* 29 (4) (1999) 619–622.
- 545 [26] D. Bondar, C.J. Lynsdale, N.B. Milestone, N. Hassani, A.A. Ramezaniapour, Engineering
546 properties of alkali-activated natural pozzolan concrete, *ACI Mater. J.* 108 (1) (2011) 64-72.
- 547 [27] O.K. Nielsen, C. Ritz, J.C. Streibig, Nonlinear mixed-model regression to analyze herbicide
548 dose-response relationships, *Weed Technol.* 18 (2004) 30-37.
- 549 [28] I.C. Yeh, Modeling of strength of high performance concrete using artificial neural networks,
550 *Cem. Concr. Res.* 28 (1998) 1797-1808.
- 551 [29] C. Deepa, K. Sathiyakumari, V. Sudha, Prediction of the compressive strength of high
552 performance concrete mix using tree based modelling, *Int. J. Comput. Appl. Technol.* 6
553 (2010) 18–24.
- 554 [30] J.S. Chou, C.K. Chiu, M. Farfoura, I. Al-Taharwa I, Optimizing the prediction accuracy of
555 concrete compressive strength based on a comparison of data-mining techniques, *J.*
556 *Comput. Civil. Eng.* 25 (2011) 242–253, DOI:10.1061/(ASCE)CP.1943-5487.0000088.
- 557 [31] W.P.S Dias, S.P. Pooliyadda, Neural networks for predicting properties of concretes with
558 admixtures, *Constr. Build. Mater.* 15 (2001), 371–379.
- 559 [32] S. Lai, M. Sera, Concrete strength prediction by mean of neural networks, *Constr. Build.*
560 *Mater.* 11 (1997) 93–98.
- 561 [33] S.C. Lee, Prediction of concrete strength using artificial neural networks, *Eng. Struct.* 25
562 (2003) 849–857.
- 563 [34] A. Mukherjee, S.N. Biswas, Artificial neural networks in prediction of mechanical behavior of
564 concrete at high temperature, *Nucl. Eng. Des.* 178 (1997) 1–11.
- 565 [35] H. Ni, J. Wang, Prediction of compressive strength of concrete by neural networks, *Cem.*
566 *Concr. Res.* 30 (2000) 1245–1250.
- 567 [36] M. Pala, E. Ozbay, A. Oztas, M.I. Yuce, Appraisal of long-term effects of fly ash and silica
568 fume on compressive strength of concrete by neural networks, *Constr. Build. Mater.* 21
569 (2007), 384–394.

- 570 [37] S. Akkurt, G. Tayfur, S. Can, Fuzzy logic model for the prediction of cement compressive
571 strength, *Cem. Concr. Res.*, 34 (2004), 1429–1433.
- 572 [38] F. Demir, A new way of prediction elastic modulus of normal and high strength concrete-
573 fuzzy logic, *Cem. Concr. Res.* 35 (2005) 1531–1538.
- 574 [39] F.L. Gao, A new way of predicting cement strength-fuzzy logic, *Cem. Concr. Res.* 27 (1997)
575 883–888.
- 576 [40] ASTM, ASTM C150, Standard specification for Portland cement, ASTM International, West
577 Conshohocken, PA, USA, 2007, 3rd edition, 2-5.
- 578 [41] ASTM, ASTM C127, Standard test method for density, relative density (specific gravity),
579 and absorption of coarse aggregate, ASTM International, West Conshohocken, PA, USA,
580 2007, 1-6.
- 581 [42] ASTM, ASTM C128, Standard test method for density, relative density (specific gravity),
582 and absorption of fine aggregate, ASTM International, West Conshohocken, PA, USA, 2001,
583 1-6.
- 584 [43] ASTM, ASTM C 31/C 31M-06, Standard practice for making and curing concrete test
585 specimens in the field, ASTM International, West Conshohocken, PA, USA, 2007, 3rd
586 edition, 1-5.
- 587 [44] ASTM, ASTM C 39/ C 39-05, Standard test method for compressive strength of cylindrical
588 concrete specimens, ASTM International, West Conshohocken, PA, USA, 2007 3rd edition,
589 18-23.
- 590 [45] ASTM, ASTM C496/C496M-11, Standard test method for splitting tensile strength of
591 cylindrical concrete specimens, ASTM International, West Conshohocken, PA, USA. 2007.
- 592 [46] Ludwig-Maximilians-Universitat Munich, Durbin-Watson significance tables, Institute for
593 market-based management,
594 <[http://www.imm.bwl.unimuenchen.de/dateien/3_lehre/market_analysis/durbin_watson_table](http://www.imm.bwl.unimuenchen.de/dateien/3_lehre/market_analysis/durbin_watson_tables.pdf)
595 [s.pdf](http://www.imm.bwl.unimuenchen.de/dateien/3_lehre/market_analysis/durbin_watson_tables.pdf)> (assessed on August 29, 2016).
- 596 [47] R. Jin, A statistical modeling approach to studying the effects of alternative and waste
597 materials on green concrete properties, Ph.D. Dissertation, 2013, The Ohio State
598 University, Columbus, OH, USA.
599 <<http://rave.ohiolink.edu/etdc/view.cgi?acc%5Fnum=osu1372854071>>.