

Valorisation of high acid value waste cooking oil into biodiesel using supercritical methanolysis: Experimental assessment and statistical optimisation on typical Egyptian feedstock

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ABSTRACT

In this study, valorisation of high acid value waste cooking oil into biodiesel has been investigated. Non-catalytic transesterification using supercritical methanol has been used for biodiesel production. Four controllable independent process variables have been considered for analysis including methanol to oil (M:O) molar ratio, temperature, pressure and time. Uncommon effects of process variables on the reaction responses, e.g. biodiesel and glycerol yields, have been observed and extensively discussed. Response surface methodology (RSM) *via* Central Composite Design (CCD) has been used to analyse the effect of the process variables and their interactions on the reaction responses. A quadratic model for each response has been developed representing the interrelationships between process variables and responses. Analysis of Variance (ANOVA) has been used to verify the significance effect of each process variable and their interactions on reaction responses. Optimal reaction conditions have been predicted using RSM for 98% and 2.05% of biodiesel and glycerol yields, respectively at 25:1 M:O molar ratio, 265°C temperature, 110 bar pressure and 20 minutes reaction time. The predicted optimal conditions have been validated experimentally resulting in 98.82% biodiesel yield, representing 0.83% relative error. The quality of the produced biodiesel showed excellent agreement with the European biodiesel standard (EN14214).

KEYWORDS

Biodiesel, Biomass valorisation, Waste cooking oil, Supercritical methanolysis, Optimisation, Response Surface Methodology.

HIGHLIGHTS

- Successful valorisation of high acid value waste cooking oil into biodiesel.
- Effect of reaction parameters on responses has been comprehensively discussed.
- Reaction optimal conditions has been predicted using Response Surface Methodology.
- Excellent correlation between predicted and experimental optimal conditions.

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40 1. INTRODUCTION

41 The increasing demand of energy from the domestic and industrial sectors combined with
42 possible scarcity of petroleum based fuels in the near future have boosted the research for
43 alternative sustainable fuels [1]. Moreover, the growing concerns for the environment and
44 the critical need to reduce carbon emissions, which are the main cause of global warming,
45 have developed numerous agreements between countries aiming to control emissions and to
46 promote development of environmental benign fuels from renewable resources [2,3].

47 Petroleum diesel is a fuel with complex composition, which is widely used in different
48 sectors including transportation, industrial, agricultural and commercial sectors. It consists
49 of paraffinic, olefinic and aromatic hydrocarbons as main components along with different
50 impurities e.g. sulphur, nitrogen and metallic atoms [4]. Of the alternative fuels, biodiesel is
51 considered as a promising eco-friendly replacement for petroleum diesel fuel [5]. Recently,
52 biodiesel has attracted huge attention due to its biodegradability, non-toxicity, availability
53 from renewable sources and lesser emissions of CO₂ into the atmosphere than petroleum
54 diesel. This non-conventional fuel, composed of fatty acid alkyl esters (FAAEs), is derived
55 from biological renewable resources including vegetable oils, animal fats and microbial oils
56 [6].

57 Biodiesel has been considered as a promising alternative fuel because it has similar
58 physicochemical properties to petroleum diesel which can be used as substitute without the
59 need for engine modifications. The significant advantage of using biodiesel in diesel
60 engines is the decrease of hydrocarbons, polyaromatic, carbon oxides and sulphur
61 emissions leading to reduction of greenhouse gases while providing similar properties in
62 terms of fuel efficiency [7,8]. Biodiesel is mainly synthesised from oils extracted from
63 traditional oilseeds e.g. sunflower, soybean, and palm. Moreover, any matter containing
64 triglycerides could be considered as a potential feedstock for biodiesel including waste
65 cooking oil (WCO) and lipids derived from either fish or animals [9]

List of Abbreviations:

2

2FI: Two Factors Interactions; ANOVA: analysis of variance; CCD: Central Composite design; DOE: Design of Experiments; FAME: fatty acids methyl esters; FFA: Free Fatty Acid; FID: Flame Ionisation Detector; M:O: methanol to oil ratio; R²: Coefficient of Correlation; RSM: response surface methodology; TAN: total acid number; WCO: waste cooking oil; df: Degrees of freedom.

66 Currently, edible oils are the main resources for biodiesel production. However, the use of
67 edible oils has a strong influence on the global food security by reduction of food resources
68 and increasing the price of edible oils. Thus, focus has been shifted towards second
69 generation feedstock including non-edible oils and WCO [10].

70 Valorisation of bio-waste including agro-industrial, municipal and domestic waste into
71 biodiesel make the process eco-friendly and sustainable. It simultaneously assists waste
72 management while minimising the production cost. WCO, which is much cheaper than
73 fresh vegetable oils, is considered as promising replacement feedstock for edible oils.
74 Disposal of WCOs and fats have been reported as a major problem in many parts of the
75 world. Some developed countries have set some policies to prevent the disposal of WCO
76 through drainage [11].

77 Generally, the physicochemical properties of WCO is nearly similar to its fresh edible oil.
78 However, the main obstacles in WCO properties are high free fatty acids (FFAs) and water
79 contents due to frying process. During cooking process, edible oils are heated to high
80 temperature in the presence of air for relatively long time. Accordingly, FFAs concentration
81 increases in the oil because of hydrolysis of triglycerides. Moreover, some physical changes
82 occur for WCO including increase in viscosity and surface tension, change in colour and
83 higher tendency of fat formation. These changes are relative to the cooking process where
84 the more use of edible oils in frying results in higher FFA and water contents [12].

85 There are four basic techniques for biodiesel production including alkaline catalysed
86 transesterification, direct acid catalysed transesterification, enzymatic catalytic conversion
87 of oil to fatty acids and subsequently to biodiesel and non-catalytic transesterification using
88 supercritical technology. Among all these techniques, homogeneous alkaline
89 transesterification is considered as the most commonly used method for biodiesel
90 production. Moreover, methanol is the preferred alcohol in transesterification reaction due
91 to its lower molecular weight and cost [13,14].

92 Alkaline and acidic transesterification techniques require lower cost with less reaction time
93 in comparison with enzymatic technique [15]. Homogeneous alkaline technique produces
94 biodiesel with high purity and yield with moderate reaction temperature in reasonable
95 reaction time. However, this technique requires feedstock with low FFA content to avoid
96 saponification side reactions [16,17]. Accordingly, two-steps transesterification technique
97 has been developed to overcome the high FFA content in feedstock. Firstly, acid catalysed
98 esterification of FFA to FAAE occur as a pre-treatment step. This is followed by an
99 alkaline catalysed transesterification of triglycerides to FAAEs. Although, the long reaction
100 time and low recovery of catalyst were considered as main disadvantages of two-steps
101 proposed technique [12]. Lewis acid catalysed technique has been proposed to overcome

102 the disadvantages of two-steps transesterification technique. However, it requires high
103 reaction temperature with relatively low production yield [18]. Heterogeneous alkaline
104 catalysed technique has been developed to overcome the feedstock restriction and to ease
105 the catalyst separation complications. Many researchers reported successful biodiesel
106 production using heterogeneous catalysts with high product yield. However, the high
107 preparation cost of catalysts including very high temperatures for calcination processes
108 (800-900°C) is considered as the main disadvantages of heterogeneous catalysed technique
109 [10,19].

110 Previous works have been reported for biodiesel production from WCO using various
111 transesterification techniques. El-Gendy et al. [20] have studied the optimisation of
112 biodiesel production from waste cooking oil using CaO obtained from calcination of
113 eggshells. They have obtained 96% yield of biodiesel at 6:1, 3 wt%, 60 min and 200 rpm
114 for M:O molar ratio, catalyst weight percentage reaction time and stirring rate, respectively.
115 Wang et al. [21] achieved have 90% conversion of WCO to biodiesel using 4 wt% of
116 H₂SO₄ with M:O molar ratio of 1:20 after 10 h reaction time. El-Gendy et al [14] have used
117 KOH as an alkaline catalyst for biodiesel production from WCO. They have optimised the
118 process variables to achieve 99% biodiesel yield at M:O molar of 7.5:1, KOH weight of
119 0.0875 wt%, temperature of 52°C in 1.17 h and 200 rpm stirring rate.

120 Recently, alternative methods have been reported for biodiesel production including
121 supercritical technology [13], ultrasonic reactor [22], microwave radiation [23] and
122 membrane reactor [24]. Specifically, supercritical methanol transesterification has been
123 developed as an alternative technique for biodiesel production where biodiesel is produced
124 in high yield without any pre-treatment processes. Supercritical methanol transesterification
125 has a number of advantages, including elimination of wastewater generation resulted from
126 catalyst recovery and leading to high purity biodiesel. It also eliminates saponification side
127 reactions resulted from alkaline homogenised technique. Accordingly, supercritical
128 methanol transesterification is considered as an ideal technique for biodiesel production
129 from WCO with high FFAs content [25,26].

130 Aghbashlo et al [27] have optimised biodiesel production from WCO using ultrasonic
131 reactor in the presence of KOH as a catalyst. They have achieved 97% conversion of
132 triglycerides at M:O molar ratio of 6:1 and reaction temperature of 60°C within only 10
133 minutes. Milano et al [28] have studied conversion of mixture of WCO and *Calophyllum*
134 *inophyllum* oil using microwave irradiation-assisted alkaline catalysed method. They have
135 reported 97.65% yield of biodiesel within 7.15 minutes at M:O volumetric ratio, catalyst
136 concentration and stirring rate of 59.60% (v/v), 0.774 wt% and 600 rpm, respectively.
137 Ghoreishi and Moein [29] have optimised biodiesel production from WCO using
138 supercritical methanol. They reported 95% biodiesel optimum yield at 271.1°C, 23.1 MPa ,

139 M:O molar ratio of 33.8:1 within 20 minutes. Aboelazayem et al. [30] have reported
140 optimum conditions for biodiesel production from WCO using supercritical methanol. They
141 have achieved 91% biodiesel yield at 37:1 M:O molar ratio, 253.5 °C, 198.5 bar within 14.8
142 min. However, there is a gap in the literature regarding non-catalytic biodiesel production
143 from high acid value WCO as it is readily available from food industries (TAN varies based
144 on the duration of cooking process).

145 RSM is based on experimental design with a final goal of assessing the optimal variables
146 for specific target of the response, using minimum experiments. RSM investigates the
147 interaction effect between several illustrative variables on one or more response variables.
148 RSM is a collection of mathematical and statistical techniques that are useful for the
149 modelling and analysis of problems in which a response of interest is influenced by several
150 variables and the objective is to optimize this response [31,32].

151 The present study is focused on solving a real world problem for sustainable production of
152 bioenergy from very low quality feedstock. The main aim of this study is to investigate the
153 feasibility of supercritical methanolysis for biodiesel synthesis from very low quality WCO
154 with high acid value. As high acidity WCO requires pre-treatment esterification step prior
155 to transesterification reaction, the applicability of supercritical methanolysis to operate
156 simultaneous transesterification of triglycerides and esterification of FFAs of very low
157 quality WCO to FAME has been investigated. As per using very low quality WCO, this
158 work has highlighted unusual influence of different reaction parameters and their
159 interactions on biodiesel and glycerol yields. In addition, two quadratic models have been
160 developed representing response variables function in reaction parameters. RSM using
161 CCD has been used for designing the experiments, modelling and optimisation. Four
162 independent process variables have been considered in this study, i.e. M:O molar ratio,
163 temperature, pressure and time. ANOVA has been used to assess the adequacy of the
164 predicted models and the effect of each process variable and their interactions on reaction
165 responses. Optimisation of reaction variables has been carried out to maximise the
166 production of biodiesel. Finally, the predicted optimum conditions have been validated
167 experimentally.

168

169 **2. MATERIALS AND METHODS**

170

171 **2.1. Materials**

172

173 WCO was collected from Egyptian local restaurants and food industries. Methanol (99%
174 purity) was purchased from Fisher Scientific, UK. The standard methyl esters used for
175 preparing calibration curves and the heptadecanoic acid methyl ester used as an internal

176 standard were purchased from Merck, UK. The liquid CO₂ cylinder (99.9%) equipped with
177 a dip tube was purchased from BOC Ltd., UK.

178

179

180 **2.2. Experimental procedures**

181

182 **2.2.1. Supercritical methanolysis**

183 WCO was heated to 30°C using a hot plate for liquefaction and then filtered to remove any
184 residuals from cooking processes. The filtered WCO was used directly in the reactor
185 without any pre-treatment steps. The reaction was carried out in a 100 mL high pressure
186 reactor made of stainless steel (model 4590, Parr Instrument Company, USA) which is
187 fitted with a thermocouple (type J), heating mantle, controller (model 4848) and a
188 mechanical stirrer. A schematic of the experimental setup is shown in Figure 1. WCO was
189 weighed and mixed with methanol (based on specific molar ratio). Then, the mixture was
190 fed to the reactor and heated to the target temperature with continuous stirring at a constant
191 rate of 300 rpm. After reaching the target temperature, vaporised methanol had already
192 built up pressure inside the reactor which was still below the targeted pressure. A
193 supercritical fluid pump (model SFT-10, Analytix Ltd., U.K) was used to compress CO₂
194 from a cylinder to the reactor in order to achieve the targeted pressure. The time required
195 for reaching the desired temperature and pressure was approximately 15 min in all
196 experiments. Reaction residence time counts once reaching the desired reaction conditions.
197 After the specified residence time, the reactor was quenched using an ice bath to stop the
198 reaction and then the reactor was depressurised. Unreacted methanol was recovered using
199 simple distillation at 80°C for 30 minutes. The reaction products were separated using a
200 centrifuge (1500 rpm, 3 min per cycle) to biodiesel and glycerol. Finally, biodiesel and
201 glycerol contents were measured for yields calculations. Biodiesel and glycerol yields were
202 calculated using Equation (1) [29].

203

$$204 \text{ Yield (\%)} = \frac{\text{Total weight of pure product}}{\text{Total weight of waste cooking oil used}} \times 100 \quad (1)$$

205

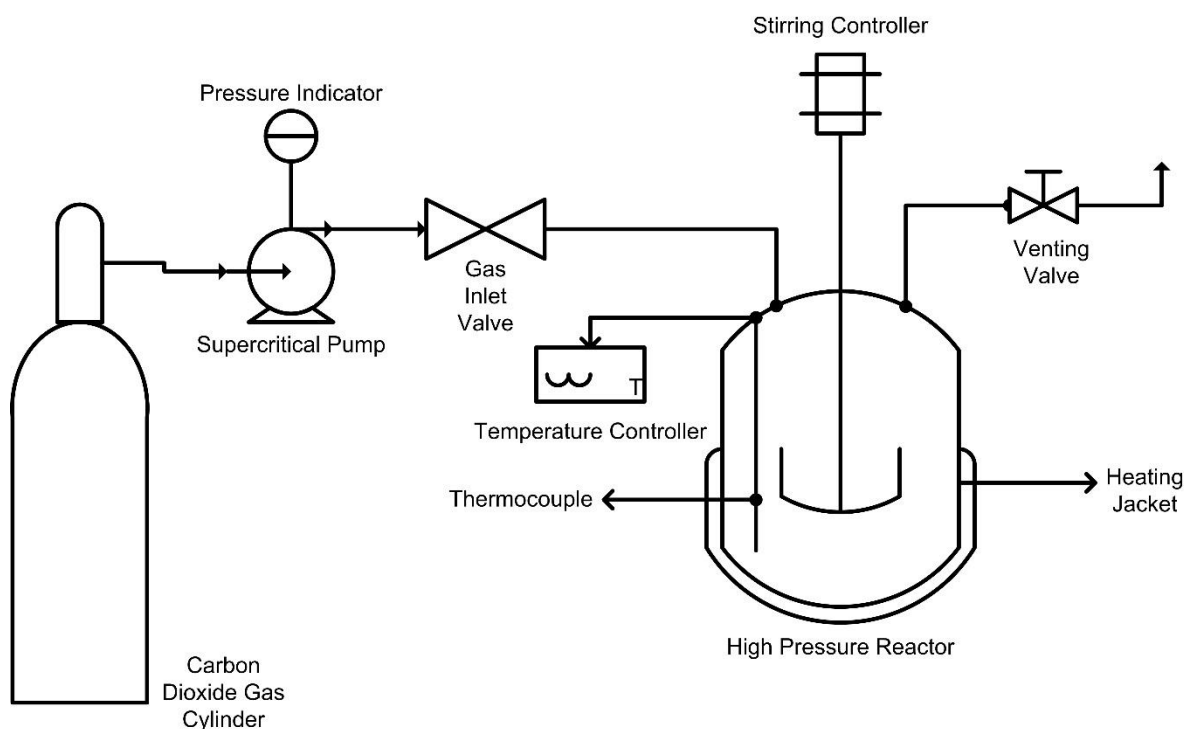


Figure 1. A schematic of the experimental setup

2.2.2. WCO and biodiesel characterisation

Standard procedures were followed to characterise properties of WCO and the produced biodiesel including ASTM D-974, ASTM D-445 and ASTM D-4052 for measuring total acid number (TAN), kinematic viscosity and density, respectively. The determined properties of biodiesel were compared with the European biodiesel standard (EN14214). The analysed properties were replicated twice and the final results were obtained as an average of the two results. Table 1 illustrates the main physicochemical properties of WCO used for the experimental analysis.

Compositions of fatty acids for WCO were analysed by converting them to methyl esters according to BS-EN-ISO-12966-2:2011. Methyl esters content for WCO and produced biodiesel were analysed using a gas chromatograph (GC) (Thermo- Scientific, Trace 1310) equipped with a capillary column (TR-BD 30 m × 0.25 mm × 0.25 μm) and flame ionisation detector (FID). Both injector and detector temperatures were adjusted at 250°C. Helium was used as the carrier gas. The temperature programme was started from 60°C and held for 2 min. Then it ramped with 10°C/min to 200°C and directly ramped with 1°C/min to 210°C. Finally, the temperature was increased to 240°C with a ramp rate of 20°C/min and remained for 7 minutes. Table 2 illustrates the fatty acids composition of WCO used for the experimental analysis.

229

Table 1. Physicochemical properties of WCO

Property	Calibration Method	Results
Kinematic viscosity	ASTM D-455	60.5 cSt
Density	ATM D-4052	0.931 g/cm ³
TAN	ASTM D-947	18 mg KOH/ g oil

230

231

Table 2. Composition of the fatty acids in WCO

Fatty Acid	Wt (%)
Palmitic acid	41.6
Oleic acid	48.2
Linoleic acid	9.3
Myristic acid	0.8

232

233 2.3. Experimental design

234

235 RSM was applied for the design of experiments (DOE) in order to optimise reaction
 236 parameters for higher biodiesel yield. The effect of four independent variables and their
 237 interactions on reaction responses (biodiesel and glycerol yields) were investigated using
 238 RSM based on four factors and five levels of CCD. The CCD method of RSM is the most
 239 popular optimisation tool for reaction conditions. It includes full or fractional designs with
 240 centre points that are integrated with a group of axial points, which allow better predictions
 241 of the curvature in the resulting model. In this study, the range of the selected independent
 242 variables was studied within five levels, which were coded as -2, -1, 0, 1, 2, as shown in
 243 Table 3.

244

245

Table 3. Experimental design variables and their coded levels

Factor	Code	Levels				
		-2	-1	0	+1	+2
M:O (molar ratio)	A	20	25	30	35	40
Temperature (°C)	B	240	250	260	270	280
Pressure (bar)	C	85	110	135	160	185
Time (min)	D	7	12	17	22	27

246

247 According to the CCD design, a 4 factors 5 levels CCD design was implemented and total
 248 30 experiments were carried out in this study as shown in Table 4. The total number of
 249 experiments was calculated based on Equation 2.

250

$$251 \text{ Total number of experiments} = 2^n + 2n + m \quad (2)$$

252 where n is the number of independent variables and m is number of replicated centre points.

253 This study included 4 independent variables and hence, enough information should be

254 provided to assist the prediction of second-order polynomial models for biodiesel and
255 glycerol yields as responses. Thus, 16 factorial points and 8 axial points developed 30
256 experiments that were performed randomly including 6 replicates at the centre point for
257 precise experimental error predictions. The experimental runs were performed in a
258 randomised order to minimise the effect of unexplained inconsistency in the responses [23].
259 The analysed reaction variables were M:O molar ratio (A), temperature (B, °C), pressure
260 (C, bar) and time (D, min) while reaction responses were biodiesel yield (Y_1 , wt%) and
261 glycerol yield (Y_2 , wt%).

262

263 **2.4 Statistical Analysis**

264

265 Regression analysis was performed using general quadratic polynomial equation to define
266 the model as shown in equation (3).

$$267 \quad Y = b_o + \sum_{i=1}^n b_i x_i + \sum_{i=1}^n b_{ii} x_i^2 + \sum_{i=1}^{n-1} \sum_{j>1}^n b_{ij} x_i x_j + \varepsilon \quad (3)$$

268 where Y is the predicted response (i.e. biodiesel and glycerol yields), b_o is the model
269 coefficient constant, b_i , b_{ii} , b_{ij} , are coefficients for intercept of linear, quadratic, interactive
270 terms respectively, while x_i , x_i are independent variables ($i \neq j$). n is number of independent
271 variables and ε is the random error.

272 Model accuracy was checked by coefficient of correlation (R^2), adjusted coefficient of
273 determination (R^2_{adj}) and the predicted coefficient of determination (R^2_{pred}). Investigation of
274 the statistical significance was analysed using ANOVA by calculating the Fisher's F-test at
275 95% confidence level. Design Expert 10 software (Stat-Ease Inc., Minneapolis, MN, USA)
276 was used to design the experiments, regression analysis, graphical analysis and numerical
277 optimisation.

278

279
280

Table 4. Experimental design matrix with the actual and predicted yields

Run	M:O ratio (A)	Temperature (°C) (B)	Pressure (bar) (C)	Time (min) (D)	Actual BD Yield %	Predicted BD Yield %	Actual GL Yield %	Predicted GL Yield %
1	30	260	135	17	89.21	88.63	10.82	11.50
2	35	250	160	22	92.12	92.63	7.92	7.82
3	35	250	110	22	94.00	93.91	7.10	6.21
4	35	270	160	22	83.00	83.51	17.72	16.61
5	35	270	110	12	89.70	90.01	10.50	9.37
6	35	250	160	12	96.95	96.44	3.20	3.45
7	25	270	160	22	94.50	94.22	4.37	5.36
8	30	260	135	17	88.40	88.63	11.60	11.50
9	25	250	110	22	94.10	94.57	5.96	5.31
10	25	250	160	22	94.20	93.98	5.70	6.01
11	30	260	85	17	99.00	98.84	0.52	1.32
12	25	270	110	12	94.40	93.88	4.50	5.34
13	25	250	160	12	91.40	91.63	8.40	7.97
14	30	260	135	17	88.60	88.63	11.63	11.50
15	35	250	110	12	94.00	94.27	5.82	5.57
16	30	240	135	17	92.00	91.90	8.15	8.83
17	30	260	185	17	96.20	96.25	4.30	3.55
18	35	270	160	12	88.50	88.02	9.50	10.89
19	30	260	135	17	88.40	88.63	11.5	11.50
20	30	260	135	27	95.00	94.40	4.36	4.98
21	30	260	135	7	92.60	93.10	5.50	4.95
22	25	270	160	12	92.40	92.57	5.90	5.97
23	20	260	135	17	90.50	90.51	9.32	9.09
24	25	250	110	12	89.20	88.77	10.70	10.99
25	30	280	135	17	87.90	87.89	12.60	11.97
26	30	260	135	17	88.60	88.63	11.68	11.50
27	40	260	135	17	85.40	85.29	14.65	14.93
28	25	270	110	22	98.40	98.99	2.08	1.01
29	30	260	135	17	88.60	88.63	11.80	11.55
30	35	270	110	22	89.20	88.96	10.20	11.37

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282

283 3. RESULTS AND DISCUSSION

284

285 3.1. Development of regression model equation

286

287 Design Expert software has fitted four models for each response including; linear, two
288 factors interactions (2FI), quadratic and cubic polynomials. Among the fitted models of
289 each response, one model has been selected based on different statistical tests including;
290 lack of fit analysis, adjusted coefficient of determination (R^2_{adj}), predicted coefficient of
291 determination (R^2_{pred}) and associated aliased coefficients. The software suggested the
292 quadratic model for both biodiesel and glycerol yield responses. Equations 4 and 5
293 represent the developed quadratic models with empirical relationships between responses
294 and reaction variables within specific levels in terms of coded factors shown in Table 3.

295

$$296 Y_1 = 88.64 - 1.31 A - B - 0.65 C + 0.32 D - 2.34 AB - 0.17 AC - 1.54 AD - 1.04 BC -$$
$$297 0.17 BD - 0.86 CD - 0.18 A^2 + 0.32 B^2 + 2.23 C^2 + 1.28 D^2 \quad (4)$$

298

$$299 Y_2 = 11.51 + 1.46 A + 0.79 B + 0.56 C + 0.01 D + 2.36 AB + 0.22 AC + 1.58 AD + 0.91$$
$$300 BC + 0.34 BD + 0.93 CD + 0.13 A^2 - 0.27 B^2 - 2.27 C^2 - 1.64 D^2 \quad (5)$$

301 where Y_1 and Y_2 represent biodiesel and glycerol yields, respectively. While, A, B, C and D
302 represent the process variables including M:O molar ratio, temperature, pressure and time,
303 respectively.

304 The regression equations illustrate the effect of the reaction variables on each the response.
305 The positive sign of each term indicates synergetic effect while the negative sign indicated
306 antagonistic effect [14]. The linear coefficient represents the effect of the reaction variable
307 on the response while the coefficient of variables interaction represents the interactive
308 effect of the process variables. Finally, the quadratic coefficient represents the effect of
309 variable excess on the response.

310 As shown in Equation 4, M:O molar ratio, temperature and pressure have negative effect on
311 biodiesel yield with negative sign coefficients where the increase of these variables have
312 decreasingly effect of biodiesel yield. However, in Equation 5 all the linear coefficients
313 have positive signs, which indicate that while increasing any of the process variables, e.g.
314 M:O molar ratio, temperature, pressure and time, glycerol yield increases. It can be seen in
315 Equations 4 and 5 that variation of M:O molar ratio (A) has the highest effect of both
316 biodiesel and glycerol yields, where it has the largest coefficient among other variables.

317

318

319

320 **3.2. Model adequacy checking**

321

322 The adequacies of the predicted models have been investigated to report any error
323 associated with the normality assumptions. Various analyses have been applied to check the
324 adequacy of the predicted model. The coefficient of correlation (R^2) evaluates the accuracy
325 of the predicted model whereas value of R^2 gets closer to unity indicates the high similarity
326 between predicted values of the model and the actual experimental value. The values of R^2 ,
327 R^2_{adj} , R^2_{pred} have been evaluated for biodiesel yield predicted model as 0.9913, 0.9831 and
328 0.9543, respectively. In addition, they have been assessed for glycerol's yield model as
329 0.99, 0.981 and 0.941, respectively. These results indicate that 99.13% and 99% of the total
330 variation is qualified to the experimental variables for both biodiesel and glycerol yields,
331 respectively. Adequacy precision value is a measure of the range for the predicted response
332 value in comparison with its relative error (signal to noise ratio) where a value greater than
333 4 is desirable. The value of adequacy precision has been evaluated as 44.77 and 22.79 for
334 models representing biodiesel and glycerol yields, respectively. These results verify that the
335 predicted models could be used to navigate the design space.

336 Statistical data obtained through variance analysis have been used to determine the
337 significance of the predicted models. Moreover, the significance effect of reaction
338 parameters and their interactions were determined. The parameter values from ANOVA are
339 tabulated in Tables 5 and 6.

340

341

Table 5. Analysis of variance for biodiesel yield for the developed model

Source	Sum of Squares	df	Mean Square	F-value	P-value	Significance
Model	406.8013	14	29.05723	121.5205	7.94E-13	HS
A-MeOH:Oil	40.8987	1	40.8987	171.0428	1.32E-09	HS
B-Temperature	24.1402	1	24.1402	100.9569	4.69E-08	HS
C-Pressure	10.0492	1	10.0492	42.02685	1.03E-05	HS
D-Time	2.515538	1	2.515538	10.52025	0.005456	S
AB	87.75006	1	87.75006	366.9802	5.88E-12	HS
AC	0.465806	1	0.465806	1.948052	0.183115	NS
AD	37.91481	1	37.91481	158.5638	2.23E-09	HS
BC	17.36806	1	17.36806	72.63508	3.92E-07	HS
BD	0.479556	1	0.479556	2.005556	0.177154	NS
CD	11.95431	1	11.95431	49.99419	3.81E-06	HS
A ²	0.918765	1	0.918765	3.842372	0.068819	NS
B ²	2.755907	1	2.755907	11.5255	0.003999	S
C ²	136.3358	1	136.3358	570.1711	2.39E-13	HS
D ²	44.90241	1	44.90241	187.7867	6.91E-10	HS
Residual	3.586708	15	0.239114			
Lack of Fit	3.141958	10	0.314196	3.532275	0.088105	NS
Pure Error	0.44475	5	0.08895			
Cor Total	410.388	29				

343 According to Tables 5-6, the significance of each model has been evaluated based on both
344 p-value and F-test at 95% confidence level. The smaller the p-value than 0.05, the more
345 significance of the corresponding parameter. It has been observed that both models are
346 highly significant with p-values of <0.0001. These values have ensured the significance of
347 the models in representing the experimental results. Lack-of-fit analysis is one of the
348 ANOVA techniques which measure the failure of the regression model in representing the
349 experimental data points. The non-significant value for lack-of-fit test indicates a high
350 fitting model. Lack-of-fit values for both models have been observed as 0.088 and 0.22 for
351 both biodiesel and glycerol yields models, respectively. The non-significance of the test
352 illustrated that the models have represented most of the experimental data successfully.
353 Moreover, Figure 2 (a and b) illustrated a graphical representation for experimental actual
354 values *versus* predicted values using the developed models for both biodiesel and glycerol

355 yields, respectively. The similarity between actual and predicted values has ensured the
 356 accuracy of the model in predicting the response variable.

357

358 Table 6. Analysis of variance for glycerol yield for the developed model

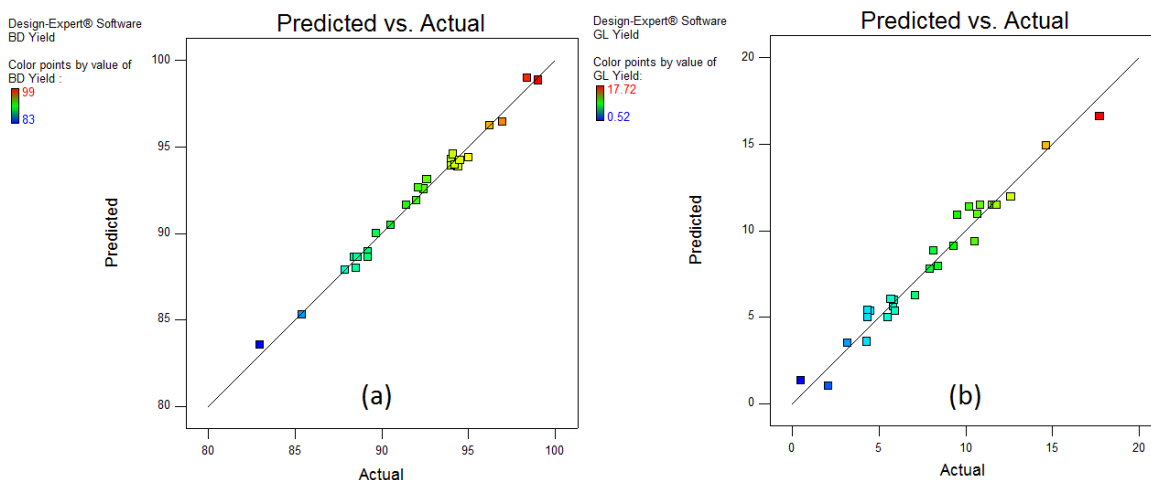
359

Source	Sum of Squares	df	Mean Square	F-Value	P-value	Significance
Model	432.8486	14	30.91776	33.51097	9.33E-09	HS
A-MeOH:Oil	51.07084	1	51.07084	55.35437	2.08E-06	HS
B-Temperature	14.83654	1	14.83654	16.08094	0.001136	HS
C-Pressure	7.492838	1	7.492838	8.121295	0.012172	S
D-Time	0.002604	1	0.002604	0.002823	0.958331	NS
AB	89.25526	1	89.25526	96.74149	6.21E-08	HS
AC	0.805506	1	0.805506	0.873068	0.364906	NS
AD	40.03726	1	40.03726	43.39536	8.62E-06	HS
BC	13.26781	1	13.26781	14.38064	0.001771	HS
BD	1.829256	1	1.829256	1.982684	0.179495	NS
CD	13.85701	1	13.85701	15.01925	0.001494	HS
A ²	0.449536	1	0.449536	0.487241	0.49584	NS
B ²	2.066436	1	2.066436	2.239757	0.155246	NS
C ²	140.8054	1	140.8054	152.6153	2.9E-09	HS
D ²	73.38816	1	73.38816	79.54355	2.2E-07	HS
Residual	13.83924	15	0.922616			
Lack of Fit	13.22769	10	1.322769	2.81489	0.22476	NS
Pure Error	0.61155	5	0.12231			
Cor Total	446.69	29				

360

361 where HS: highly significant, S: significant and NS: not significant

362



363
364 Figure 2. Predicted *versus* actual values for biodiesel yield model (a) and glycerol yield model (b)
365

366 Table 5 shows that all studied factors have significant individual (linear) effect on biodiesel
367 yield where reaction time variable has showed the least significance effect than other
368 variables with p-value of 0.005. The analysis also showed that there is a significant effect
369 on biodiesel yield for variables interaction of M:O molar ratio - temperature (AB), M:O
370 molar ratio - time (AD), temperature - pressure (BC) and pressure – time (CD). Moreover,
371 it has been observed that both pressure and time showed significant quadratic effect on
372 biodiesel yield.

373
374 According to Table 6, temperature, pressure and time showed significant individual effect
375 on glycerol yield while reaction time showed insignificant effect on glycerol yield. Only
376 temperature and pressure showed significant quadratic effect on glycerol yield. Although,
377 analysis showed that there is a significant effect on glycerol yield between variables
378 interactions of M:O molar ratio - temperature (AB), M:O molar ratio - time (AD),
379 temperature - pressure (BC) and pressure – time (CD).

380
381 In an attempt to simplify the developed models, the insignificant variables have been
382 excluded. According to ANOVA results presented in Tables 5 and 6 for the predicted
383 models (Equations 4 and 5), the insignificant parameters, with p-values higher than 0.05
384 have been highlighted. It is shown in Table 5 that there is insignificant interactive effect on
385 the response for both parameters AC and BD. In addition, the excess of M:O molar ratio
386 (A) has statistical insignificant effect on biodiesel yield. On the other hand, reaction time
387 (D) has insignificant effect on glycerol yield as shown in Table 6, however, it cannot be
388 excluded to maintain the model hierarchal structure [33]. Additionally, the interactions
389 between AC and BD along with the excess of two variables including M:O molar ratio and
390 temperature showed statistically insignificant effect on glycerol yield. Consequently,

391 simplified reduced models have been developed for both biodiesel and glycerol yields by
 392 excluding the mentioned insignificant parameters as shown in Equations 6 and 7.

393

$$394 \quad Y_1 = 88.43 - 1.31 A - B - 0.65 C + 0.32 D - 2.34 AB - 1.54 AD - 1.04 BC - 0.86 CD$$

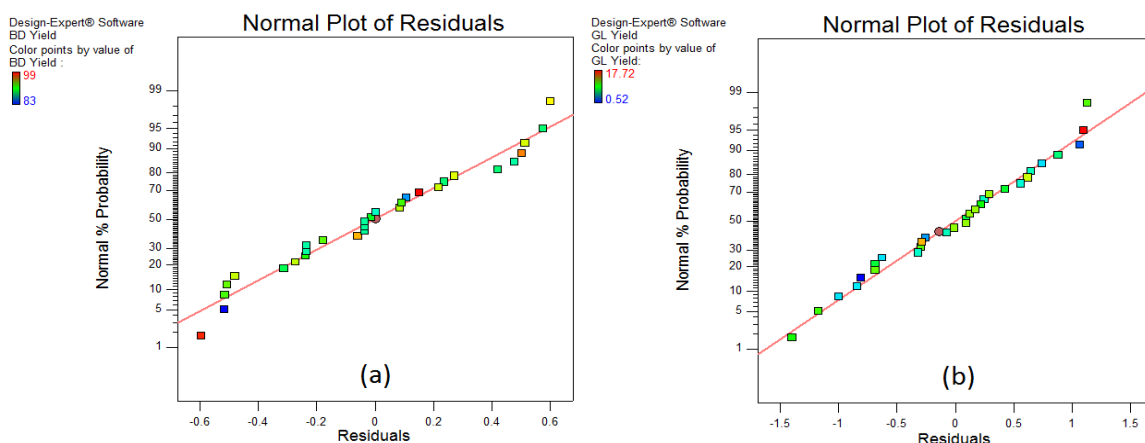
$$395 \quad + 0.34 B^2 + 2.26 C^2 + 1.31 D^2 \quad (6)$$

396

$$397 \quad Y_2 = 11.36 + 1.46 A + 0.79 B + 0.56 C + 0.01 D + 2.36 AB + 1.58 AD + 0.91 BC$$

$$398 \quad + 0.93 CD - 2.25 C^2 - 1.62 D^2 \quad (7)$$

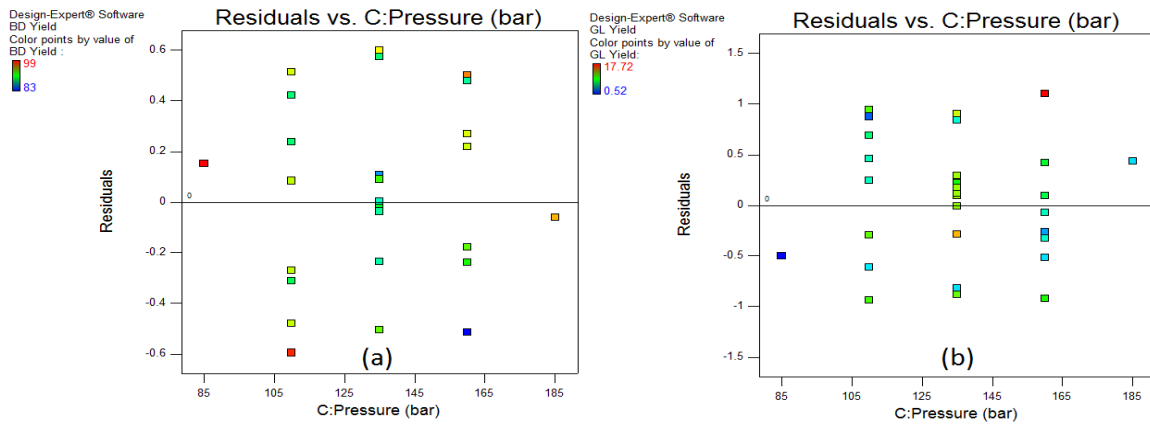
399 It is necessary to check ANOVA assumptions as it has been used to validate the predicted
 400 models. ANOVA assumptions summarised in; normality of residuals, homoscedasticity
 401 (equal variance) of residuals and random errors [33]. Normality of residuals has been
 402 investigated using normal plot where they approximately form straight line as shown in
 403 Figure 3. This test ensures the validity of the first assumption where residuals are normally
 404 distributed for both biodiesel and glycerol models. Secondly, the homoscedasticity has been
 405 investigated where pressure variable (C) has been chosen as a variable sample representing
 406 the variance equality at different levels. The homoscedasticity has been examined using
 407 residuals *versus* predicted values plot. The equal range of residuals at each level concluding
 408 the homoscedasticity of the variable results as shown in Figure 4. Finally, the
 409 randomisation of errors has been investigated using the plot of residuals *versus* actual
 410 responses values. As shown in Figure 5, residuals were distributed randomly where they do
 411 not follow any specific trend. These randomised distributions validate the third assumption
 412 of ANOVA.



413

414

Figure 3. Normal plot of residuals for (a) biodiesel yield model and (b) glycerol yield model

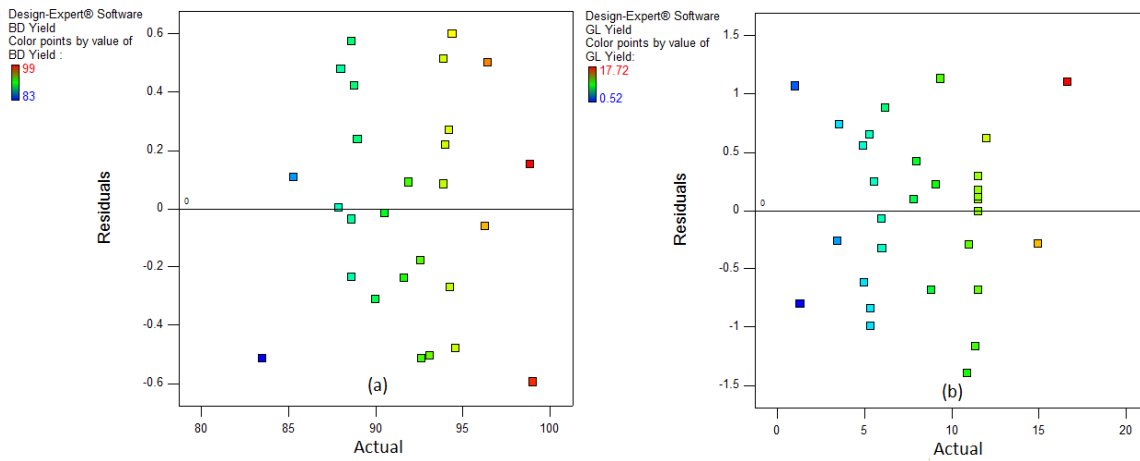


415

416 Figure 4. Plot of residuals *versus* predicted values of pressure variable for (a) biodiesel yield
 417 model and (b) glycerol yield model

418

419



420

421 Figure 5. Plot of residuals *versus* actual response for (a) biodiesel yield model and (b) glycerol yield
 422 model

423

424 **3.3. Effect of process variables and their interactions**

425

426 The effects of individual parameters and their interactions have been studied to analyse and
427 investigate the influence of parameters variation on the responses.

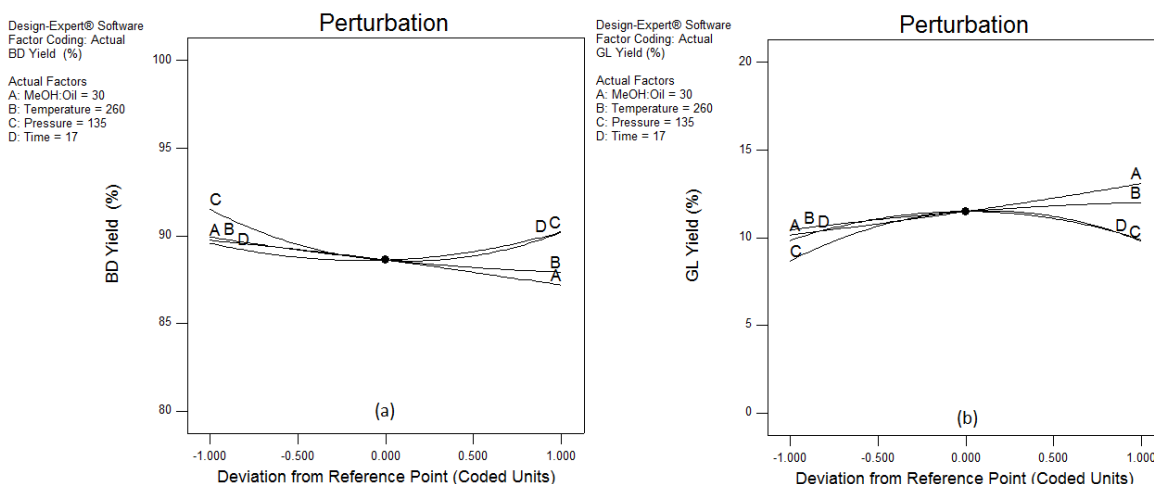
428

429 **3.3.1. Effect of individual variables on responses**

430

431 Perturbation plot is used to compare the influence of reaction variables at particular point in
432 space. In this study, centre point of all variables has been selected as a constant point of
433 comparison between variables. The influence of individual reaction variables on biodiesel
434 and glycerol yields have been presented in Figures 6a and 6b, respectively.

435



436

437 Figure 6. Perturbation plot showing the effect of individual variables on (a) biodiesel yield and (b)
438 glycerol yield

439

440 One of the drawbacks of using supercritical methanol technique for biodiesel production is
441 the usage of large excess of methanol, where it is very important to investigate its effect on
442 the biodiesel yield for optimisation considerations. It is clearly shown in Figure 6a that
443 M:O molar ratio (A) has negative effect on biodiesel yield, where increasing M:O molar
444 ratio has decreasing effect on biodiesel yield. These findings are in agreement with
445 previous study by Rade et al. [34] on high acidity soybean oil, where they have reported a
446 negative influence of alcohol to oil molar ratio on biodiesel yield. Varma et al. [25] have
447 reported that increasing M:O molar ratio for supercritical synthesis of biodiesel does not
448 have significant effect on biodiesel yield. They have explained these results as the
449 formation of homogenous reaction phase only requires lower molar ratios. Accordingly,
450 increasing methanol to oil ratio does not have a significant effect on the homogeneity of the
451 solution. However, these results contradicts previous studies for biodiesel production from

452 WCO using supercritical methanol [29,30]. The different properties of the utilised
453 feedstocks (acid value) is considered as the main reason for these contradicting results. It
454 also attributes to the esterification reaction rate of FFA that exists in the feedstock where it
455 has been reported that increasing M:O molar ratio has negatively effect on FFA conversion
456 for high acidity feedstock [35]. On the other hand, M:O molar ratio has positive effect on
457 glycerol yield as shown in Figure 6b. This is an expected result as it has been reported
458 previously that M:O ratio enhance transesterification reaction of which glycerol is produced
459 [29].

460

461 Reaction temperature is an important parameter for supercritical production of biodiesel. It
462 has been reported that at reaction temperature higher than 280°C, thermal degradation of
463 FAME occurs [36]. Since the critical temperature of methanol is 240°C, the studied
464 temperatures ranges have been chosen between 240°C and 280°C. In the present study,
465 reaction temperature has negative effect on biodiesel yield as shown in Figure 6a. This
466 result contradicts previous studies where it has been reported positive impact of increasing
467 temperature on biodiesel yield [37,38]. The effect of temperature varies at different levels
468 of M:O molar ratio. Hence, this is comprehensively discussed in section 3.3.2.1. However,
469 glycerol yield has been positively affected by increasing reaction temperature as shown in
470 Figure 6b.

471

472 Reaction pressure is one of the most important factors for supercritical transesterification
473 reactions. It has a very high impact on the properties of the solution including density and
474 hydrogen bond intensity [39]. It has been reported that the effect of reaction pressure on
475 biodiesel yield is not highly significant. In the present study, reaction pressure showed
476 significant effect on biodiesel yield. However, the variation in biodiesel yield reported 6%
477 while varying pressure from 85-185 bar. Moreover, slightly negative impact is shown at
478 Equation 4 with very small coefficient. These results are in agreement with Ting et al. [40]
479 who have reported about 7% variation in biodiesel yield when varying pressure from 10-25
480 MPa. Hence, they have considered constant pressure for their optimisation procedures.
481 Nevertheless, reaction pressure showed insignificant effect on glycerol yield as shown in
482 Table 6. Increasing reaction pressure from 110 to 140 bar, resulted in 4% increase in
483 glycerol yield. However, higher values of pressure have slightly decreasing effect on
484 glycerol yield.

485

486 Reaction time is one of the advantageous factors for supercritical transesterification over
487 catalysed processes as it recorded much shorter reaction time. The studied time interval has
488 been chosen between 12 and 22 min as it has been recommended previously [30]. In this
489 study, reaction time has been reported to have very limited effect on biodiesel yield.

490 Biodiesel variation has been reported to be 3% by varying time from 12-22 min. On the
491 other hand, reaction time has been found to be insignificant on glycerol yield.

492

493 **3.3.2. Effect of variables interactions on responses**

494

495 The interaction effect of each pair of variables has been observed from both interaction
496 plots and ANOVA results. Moreover, 3D-surface and contour plots for biodiesel and
497 glycerol yields *versus* interaction of two independent variables have been used to illustrate
498 the effect of interaction. In each plot the two remaining independent variables have been
499 kept constant at their centre points. For simplicity, this analysis only includes biodiesel
500 yield response.

501

502 *3.3.2.1 Interactive effect of methanol:oil molar ratio and temperature*

503

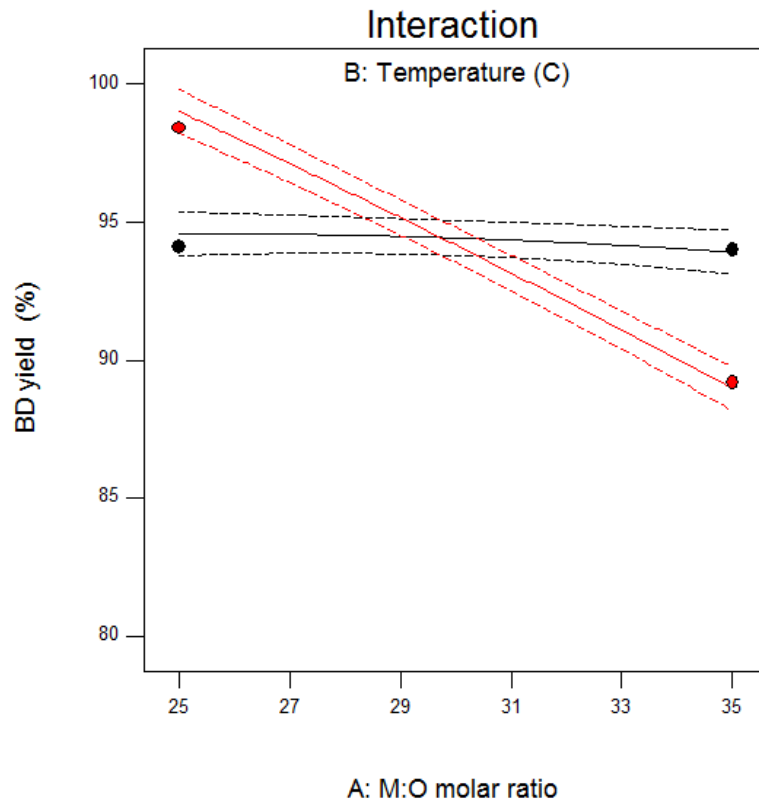
504 As reported in ANOVA results shown in Table 5, interactive effect of M:O molar ratio and
505 temperature has recorded a significant effect on biodiesel yield. Figure 7 illustrates an
506 interaction plot between M:O molar ratio and temperature where antagonistic interaction is
507 clearly observed which confirms ANOVA results. Figure 8 represents a response surface
508 and contour plots for M:O molar ratio and temperature interactive effect on biodiesel yield.
509 It can be seen from Figure 8 that at low temperature the effect of M:O molar ratio is
510 approximately neglected, however at higher temperatures, M:O molar ratio has negative
511 effect on biodiesel yield. Additionally, at low M:O molar ratio, increasing reaction
512 temperature shows positive influence on biodiesel yield. However, at high levels of M:O
513 molar ratio, biodiesel yield decreases with an increase in temperature. These results showed
514 the importance of studying the variables interactive effect. Figueroa et al. [37] have studied
515 the individual yields of different FAMES from high acidity raw castor oil using
516 supercritical methanol. They have reported decreasing effect of methyl oleate and methyl
517 palmitate (which are the main components of the WCO used in the present study) yields
518 while increasing temperature starting from 250°C at a constant M:O molar ratio of 1:40.
519 They explained this phenomenon to the increasing rate of thermal degradation of both
520 FAMES and FFAs. Interaction effect of M:O molar ratio and temperature for high acidity
521 feedstock was not reported widely. Aboelazayem et al. [32] have reported insignificant
522 interaction effect between M:O molar ratio and temperature for low acidity WCO. Hence,
523 FFA content attributes strongly to the effect of both M:O molar ratio and temperature.

Design-Expert® Software
Factor Coding: Actual
BD yield (%)
◆ Design Points
— 95% CI Bands

X1 = A: M:O molar ratio
X2 = B: Temperature

Actual Factors
C: Pressure = 110
D: Time = 22

B- 250
B+ 270



524
525
526
527
528

Figure 7. Interaction plot showing interactive effect of methanol ratio and temperature on biodiesel yield

Design-Expert® Software

Factor Coding: Actual

BD yield (%)

◆ Design points above predicted value

◇ Design points below predicted value

99

83

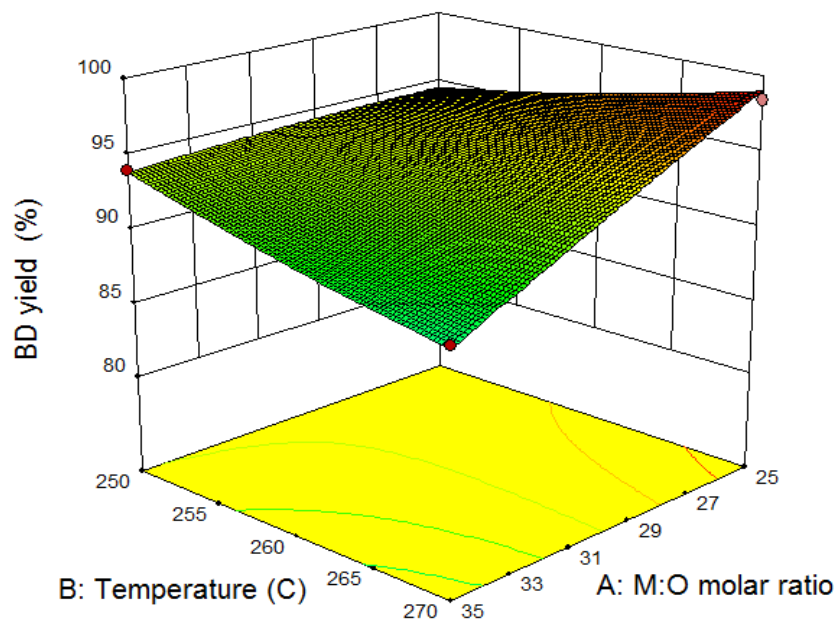
X1 = A: M:O molar ratio

X2 = B: Temperature

Actual Factors

C: Pressure = 110

D: Time = 22



Design-Expert® Software

Factor Coding: Actual

BD yield (%)

◆ Design Points

99

83

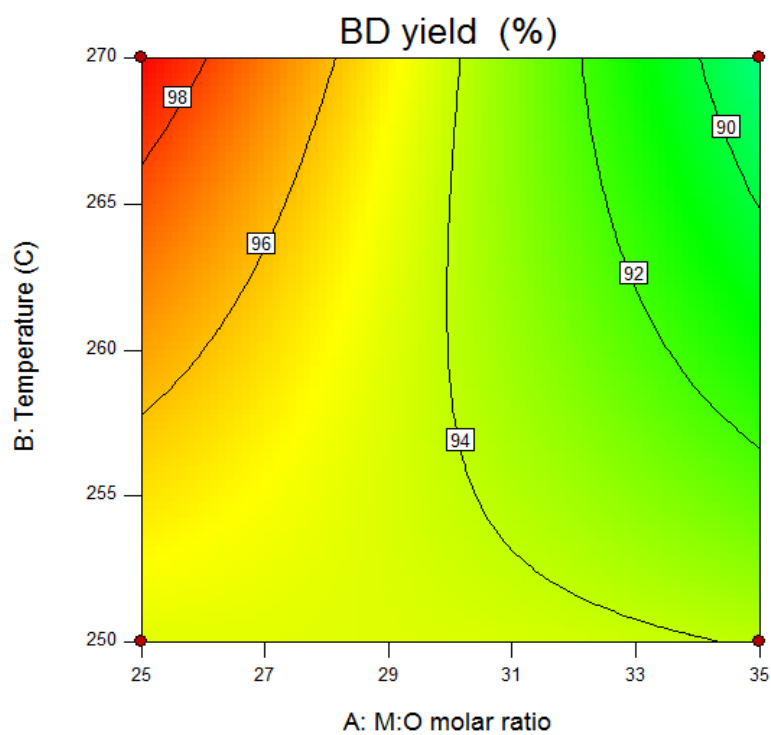
X1 = A: M:O molar ratio

X2 = B: Temperature

Actual Factors

C: Pressure = 110

D: Time = 22



529

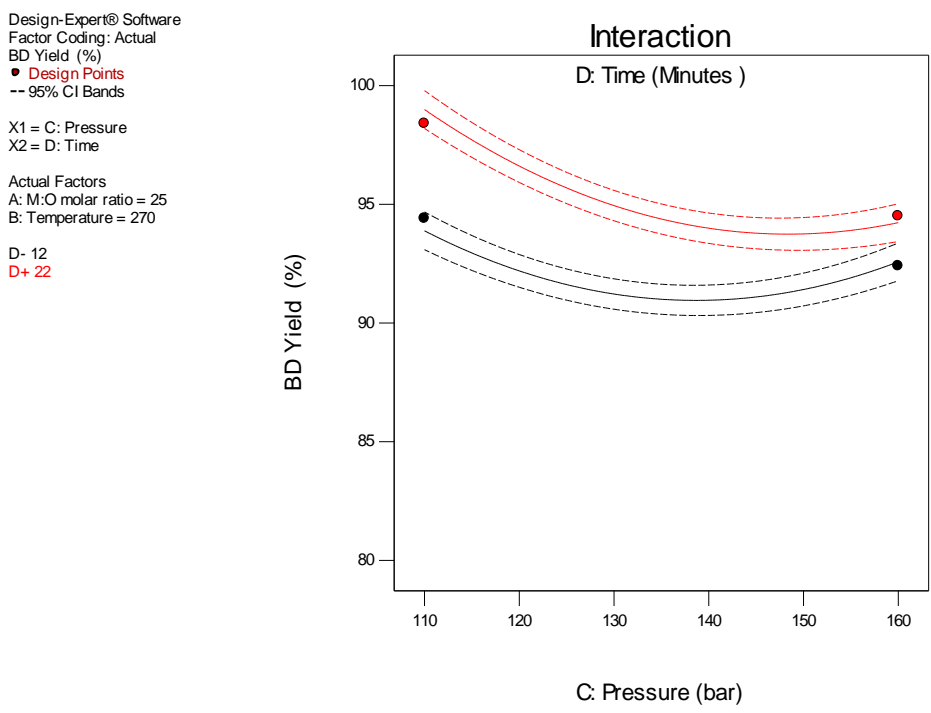
530

531

Figure 8. 3D response surface and contour plot for M:O molar ratio and reaction temperature *versus* biodiesel yield

532 3.3.2.2 Interactive effect of reaction pressure and time

533 Carbon dioxide (CO₂) gas has been used to pressurise the reaction to the desired pressure
534 using a high-pressure pump. In addition, carbon dioxide acts as a co-solvent, where it
535 enhances the solubility of methanol in oil [41]. The exponential interactive effect of
536 reaction pressure and time on biodiesel yield is shown in Figure 9, which confirms the
537 significant effect of their interaction as reported in ANOVA in Table 5. As shown in Figure
538 10, reaction pressure showed negligible effect on biodiesel yield at shorter reaction times.
539 However, slightly negative effect of reaction pressure observed at longer reaction times. It
540 has been reported by Ong et al. [42] that the increasing effect of pressure is not crucial as it
541 exceeds the critical pressure of methanol. They have explained that both transesterification
542 and esterification have the same number of moles of reactants and products. Hence, change
543 in pressure would not affect the chemical equilibrium of reaction according to Le
544 Chatelier's principle. While the negative effect of increasing pressure might be resulted
545 from FAME degradation as addition the CO₂ decrease the critical point of the system and
546 hence requires milder temperature [41].



547
548

Figure 9. Interaction plot showing interactive effect of reaction pressure and time on biodiesel yield

Design-Expert® Software

Factor Coding: Actual

BD yield (%)

● Design points above predicted value

○ Design points below predicted value



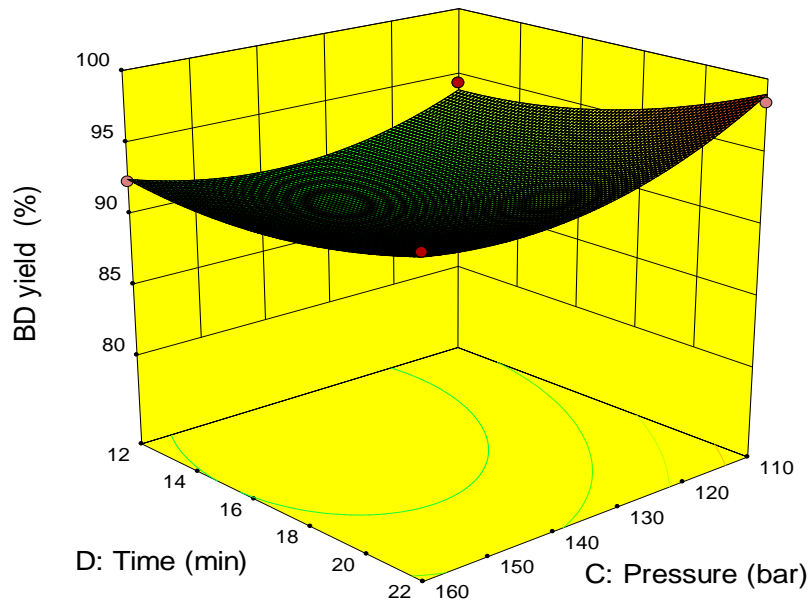
X1 = C: Pressure

X2 = D: Time

Actual Factors

A: M:O molar ratio = 25

B: Temperature = 270



549

Design-Expert® Software

Factor Coding: Actual

BD yield (%)

● Design Points



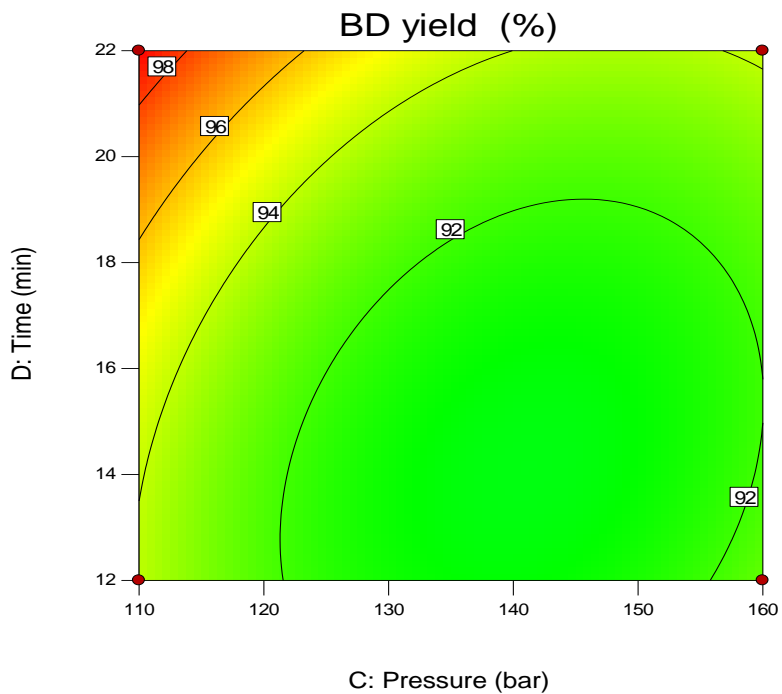
X1 = C: Pressure

X2 = D: Time

Actual Factors

A: M:O molar ratio = 25

B: Temperature = 270



550

551

552

553

554

555

Figure 10. 3D response surface and contour plot for reaction pressure and time *versus* biodiesel yield

3.4. Process optimisation and experimental validation

The application of RSM to optimise the reaction variables affecting biodiesel production have been reported in previous studies [38,43–45]. In order to optimise both reaction responses (i.e. biodiesel and glycerol yields), numerical feature using Design Expert 10 software has been implemented to evaluate the best combination of conditions for achieving the desired target. Biodiesel yield response has been set to a maximum target while minimum target of glycerol has been adjusted. The independent variables have been set to a minimum level as shown in Table 7. Subsequently, 40 solutions for optimum conditions have been generated by the software where the solution with highest desirability has been selected. The resulting optimum conditions achieved 98% and 2.05% for biodiesel and glycerol yield, respectively at 25:1 M:O molar ratio, 265°C, 110 bar pressure in 20 minutes reaction time.

In order to validate the predicted optimum conditions, three experiments have been conducted at these conditions, where the average result has been considered as the experimental outcome. The experimental validation has resulted biodiesel yield of 98.82%, which shows the adequacy of the predicted optimum conditions within 0.83% relative error from the experimental results.

Table 7. Optimisation constrains used to predict optimum conditions for biodiesel production

Factor	Code	Goal	Limits	
			Lower	Upper
M:O (molar ratio)	A	Minimise	25	35
Temperature (°C)	B	Minimise	250	270
Pressure (bar)	C	Minimise	110	160
Time (min)	D	Minimise	12	22
Biodiesel yield	Y ₁	Maximise	95	99
Glycerol yield	Y ₂	Minimise	0.52	17.72

575

The purified biodiesel produced at the optimum condition has been analysed and compared with the European Biodiesel Standard, EN14214. All the main measured physicochemical properties are within the range of the European standard as shown in Table 8.

579

580

Table 8. Comparison between produced biodiesel properties and European biodiesel standard EN14214

Test	Unit	Produced biodiesel	Biodiesel (EN14214)
Density at 15°C	kg/m ³	884	860 - 900
Kinematic viscosity at 40°C	cSt	4.6	3.5 - 5
TAN	mg KOH/ g oil	0.3	< 0.5

581

582 It is recommended to perform techno-economic study for supercritical production of
583 biodiesel from very low quality WCO. FFA conversion and intermediate conversions of
584 triglycerides could be considered as dependant responses for future studies. Exergy analysis
585 is also recommended to be studied for such a typical process. Finally, integrated process
586 simulation could be designed as a first step for scaling-up the process for industrial scale.

587

588 **4. CONCLUSIONS**

589 Valorisation of a typical Egyptian WCO with high acid value into biodiesel at very high
590 yield has been achieved. Both esterification and transesterification reactions have taken
591 place simultaneously throughout the reaction. High acidity feedstock behaves differently
592 with different reaction variables. Highly significant interactive effect of M:O molar ratio
593 and temperature has been observed. The optimum biodiesel yield has been predicted with
594 98% at M:O molar ratio of 25:1, reaction temperature of 265°C and reaction pressure of
595 110 bar in 20 minutes. The optimal conditions have been validated experimentally resulting
596 in biodiesel yield of 98.82%, which shows the adequacy of the predicted optimum
597 conditions within 0.83% relative error from the experimental results. The quality of the
598 produced biodiesel has been compared with the European biodiesel standard (EN14214)
599 showing excellent agreement with the standard biodiesel properties. This study has
600 provided an appropriate pathway for solving a real world problem for sustainable
601 production of biofuel from typically very low quality feedstock in Egypt.

602

603 **ACKNOWLEDGEMENT**

604

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608

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