Spectrum and Energy Efficiency in Dynamic UAV-Powered Millimeter Wave Networks

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Abstract—This letter investigates a dynamic scheme to analyze and optimize unmanned-aerial-vehicle-(UAV)-to-ground millimeter-wave (MMW) networks. First, a downlink energy transfer is proposed, followed by the uplink information transfer process between the UAV base stations (BSs) and a ground Internet of things (IoT) network. The UAVs fly above the ground IoT network in the energy transfer phase with the dynamic regulation to minimize the path loss fading. Afterwards, the ground-based IoT devices use the received energy to transmit the uplink information using vertical links. The UAV BSs are modeled with gain from multiple three-dimensional uniform linear antenna arrays. After deriving new statistical properties, we analyze the spectrum efficiency and energy efficiency for the system. Our numerical results have shown that the dynamic scheme in UAV-to-ground IoT networks provides great advantages than a traditional static deployment.

Index Terms—Unmanned aerial vehicles, millimeter wave, wireless power transfer, energy efficiency.

I. INTRODUCTION

In the next-generation Internet of Things (IoT) scenarios, the use of low-altitude platforms (LAPs) in aerial wireless communications has become increasingly popular, which has attracted huge attention from both academia and industry. Unmanned Aerial Vehicles (UAVs) benefit from mobility and could act as servers for various IoT devices and networks, for example, data collection, temporary base stations, or energy power beacons [1]. Enhancing the energy performance of UAV systems is becoming the most critical challenge in UAV networks, because UAV wireless networks are limited by the aircrafts’ flying speed and weight constraints. The author in [2] has shown that energy-efficient networking schemes in UAV will bring significant benefit when multiple small and mini drones are working with terrestrial networks. Energy harvesting in millimeter-wave (MMW)-based dense networks has been considered in [3]. The energy efficiency in UAV-enabled wireless networks has been studied in [4, 5]. [6] have proposed a UAV-assisted mobile network and analyzed an efficient trade-off between data collection and energy harvesting to ground devices. The authors in [7] have proposed the harvest-then-transmit protocol in UAV-enabled mobile networks.

The existing literature in [8,9] have focused on moving UAV acting as a wireless charging station in order to serve a limited number of ground IoT devices. Minimization of the total energy consumption in UAV mobile edge computing network with energy harvesting has been investigated in [10]. However, little is known about the wireless communication between multiple UAVs and ground IoT devices in cellular networks, based on the harvest-then-transmit protocol.

In order to tackle this new challenge, stochastic geometry approach has been considered to optimize the effect of multiple MMW antennas on the Spectrum Efficiency (SE) and Energy Efficiency (EE) of UAV-BSs and ground IoT networks, where the UAV-BSs first transfer energy and then collect data from the ground IoT devices. We can apply this network architecture to particular scenarios such as those pertaining to disasters and precision agriculture. To the best of our knowledge, this has not been investigated in the existing literature.

Our main contribution is to investigate a novel dynamic adaptive flight scheme for the wireless power transfer phase along with its detailed mathematical derivation. The proposed scheme can enable UAVs to move above the ground IoT devices and transfer the information, which significantly improves the efficiency of the harvested energy and overcomes the blockage effects to reduce the path loss fading. Moreover, this approach can help the desired UAVs by hovering at an ideal location to achieve better performance at MMW bands due to large path loss. We have also designed a realistic Three-Dimensional (3D) Uniform Linear Array (ULA) beamforming approach to model the UAV-to-ground MMW links after considering the moving elevation and depression angles for typical and interfering UAVs, respectively. From the simulation, we conclude that the proposed scheme is superior to the existing hovering scheme, and the optimal time allocation will maximize both SE and EE.

II. NETWORK MODEL

We consider a time-division UAV-to-ground network, which includes multiple UAV BSs having $M_r$ antennas in the air and multiple single-antenna IoT devices deployed on the ground.
The locations of all the UAV BSs and ground IoT devices are modeled as a Poisson point process (PPP) configuration in $\Phi_U$ and $\Phi_S$ with densities $\lambda_U$ and $\lambda_S$, respectively, where $\lambda_S$ is far larger than $\lambda_U$. We make the assumption that all the UAV-BSs fly at the same height $H$.

We define $T$ as the duration of a total communication slot, and $\tau \in (0, 1)$ as the allocation factor of time. In the first duration, $\tau T$ is allocated to the UAV-to-ground wireless power transfer phase, which includes the time taken for the serving UAV to move to the desired location for that ground IoT device. Typical ground IoT devices first associate with the nearest UAV-BS. Afterwards, the UAV-BS flies towards the typical ground IoT device, with a constant heading rate and altitude, as shown in Fig. 1. During the dynamic adaptive flight process, energy is transmitted to the typical ground IoT device. The next duration of $(1 - \tau) T$ is allocated to the ground-to-UAV wireless information communication phase $^1$. A ground IoT device uses the received energy as the transmit power to transmit information back to the associated UAV BSs $^2$.

A. Uniform Linear Array

All the antenna elements are placed along the propagation plane with $\Delta \kappa$ spacing, and we formulate the 3D array steering and response vector $^{[11, 12]}$ for the UAV BS as

$$\mathbf{u}_u^{(\theta_\theta, \varphi_\theta, M_o)} = \left[1, e^{-j \psi_o \sin \theta^p \sin \varphi^p}, \ldots, e^{-j \psi_{M_o-1} \sin \theta^p \sin \varphi^p}\right]^T$$

where $\theta^\theta \sim U(0, 2\pi)$ is the azimuth Angle of Departure (AoD) and $\varphi^\theta \sim U(0, \pi)$ is the angle of depression for AoD, respectively, and $\psi = 2\pi \frac{\Delta \kappa}{\lambda}$, $\varphi$ is the wavelength, $M_o$ is the number of the elements, and $(\cdot)^T$ denotes transpose. We obtain the uplink receiving vector $\mathbf{u}_u^a(\theta^A, \varphi^A, M_o)$ by interchanging $\theta^\theta \rightarrow \theta^A$ and $\varphi^\theta \rightarrow \varphi^A$ in (1), where $\theta^A \sim U(0, 2\pi)$ is the azimuth Angle of Arrival (AoA) and $\varphi^A \sim U(0, \pi)$ is the angle of depression for AoA, respectively.

In the ground network, the ground IoTs are only equipped with single-omnidirectional-antenna, which are labeled as $u_g = [1]$. Then we have the downlink and uplink ULA steering channel columns given as

$$\mathbf{U}_u = \mathbf{u}_u^a(\theta^A_o, \varphi^A_o, M_o) u_g^H.$$  \hspace{1cm} (2)

$^1$We consider UAVs with sufficient onboard energy that can be stored for supporting stable transmit power.

$^2$Once collected the data from ground IoT devices, each UAV will hover in the current location and wait for another call until the storage space is full.

Notice $(\cdot)^H$ is the conjugate transpose $^3$.

It is obvious that the transmitting and receiving array antenna gain from the UAV BS to its serving ground IoT device is $M_o$. Based on Euler’s formula, Chebyshev polynomials and trigonometric identities, the average interference antenna gain for downlink and uplink are expressed as

$$G_D = \left|\frac{\mathbf{u}_u^a(\theta^\theta, \varphi^\theta, M_o)}{\sqrt{M_o}} \mathbf{U}_u \mathbf{U}_u^H \right|^2 = \frac{1}{M_o} \left(\frac{1}{2\pi}\right)^2 \left(\frac{1}{\pi}\right)^2 \times \int_{0}^{\pi} \int_{0}^{\pi} \int_{0}^{\pi} 1 - \cos (M_o \psi_{\theta^\theta}) d\theta^\theta d\varphi^\theta d\beta^\theta,$$  \hspace{1cm} (4)

and

$$G_u = \left|\frac{\mathbf{u}_u^H}{1} \mathbf{U}_u \mathbf{u}_u^a(\theta^A_o, \varphi^A_o, M_o)\right|^2 = \frac{1}{M_o} \frac{1}{2\pi} \times \int_{0}^{\pi} \int_{0}^{\pi} \int_{0}^{\pi} 1 - \cos (M_o \psi_{\theta^A_o}) d\theta^A_o d\varphi^A_o, $$  \hspace{1cm} (5)

respectively, where we have defined $\psi^\theta = \sin \theta^\theta \sin \varphi^\theta$ and $\psi^A_o = \sin \theta^A_o \sin \varphi^A_o$.

B. Downlink Power Transfer Model

During the downlink power transmission phase, the associated UAV BS first transmits energy for the duration $\tau T$ with the instantaneous velocity $v(t)$ (m/s) and constant acceleration $a$ (m/s$^2$) toward the typical ground IoT device. Considering blockage effects in the wireless channel of the UAV-to-ground network, different path loss probabilities have been applied to Line-of-Sight (LoS) links and Non-Line-of-Sight (NLoS) links. Due to the sparse scattering in the MMW channel, we have neglected small scale fading $^{[13]}$.

The total harvested energy from associated UAV BS and ambient UAV BSs to the ground IoT device as

$$E_{\text{sum}} = \eta \frac{\tau T P_U \mu_{M_o}}{D(|X_{u}(t)|)} \sum_{q \in \Phi_U} P_{\mu^q B} \mathcal{G}_D,$$  \hspace{1cm} (6)

where $\mathcal{E}_1$ is the directed energy from the associated UAV, $P_U$ is the transmitting power from all the UAV BSs and $X_{u}(t)$ is the instant projection distance between the moving associated UAV BS to the typical IoT device. Notably, the horizontal distance $X_{u}(t) = r_o - s(t)$ is dynamic, i.e., varying with time $t$, where $t \in [0, \tau T]$, $r_o$ is the initial closest association-projection distance from UAV to typical IoT devices based on the associated probability density functions, which is given by $f(r_o) = 2\pi \lambda_U r_o \exp(-\pi \lambda_U r_o^2)$ $^{[14]}$. $\mathcal{E}_2$ is the harvested energy from the ambient UAVs, and $X_q(t)$ is the dynamic projection distances between typical ground IoT device and the ambient wireless power charging UAV BSs which varies with time $t$. $\eta$ is the energy conversion efficiency factor, and $\beta$ is the frequency-dependent constant value.

The path loss gain function can be expressed by

$$D(X) = \frac{p_L(X)}{\sqrt{X^2 + H^2}} + \frac{p_N(X)}{\sqrt{X^2 + H^2}},$$  \hspace{1cm} (7)

$^3$$\theta^A_o$ and $\varphi^A_o$ are the channel angles.
where $X$ indicates the projection distance from the serving UAV to the typical user, $\alpha_1$ and $\alpha_N$ are the LoS and NLoS path loss exponents, respectively, $p_L(X)$ is the LoS connection probability, while the NLoS probability of a link is $p_N(X) = 1 - p_L(X)$.

### C. Uplink Information Transmission

The received Signal-to-Interference-plus-Noise Ratio (SINR) of the serving UAV BS with distance $|X_o|$ is given by

$$\gamma = \frac{P_T M_o \beta D (|\hat{X}_o|)}{\sum_{k \in \Phi_0 \setminus P_T \sigma_0^2 D (|Z_k|)} + \sigma^2},$$

where $P_T$ is the maximum stable transmit power from the ground IoT device, and $\hat{X}_o$ is the projection distance between the serving UAV BS and its intended IoT device, $\sigma_0^2$ is the uplink array gain and $Z_k$ is the projection distance between the typical ground IoT device and $k$-th interfering UAV BSs, and $\sigma^2$ is the noise power.

### III. Performance Analysis

In this section, the downlink average harvested energy and average achievable rate in the uplink are analyzed.

#### A. UAV-to-ground Wireless Power Transfer

In the wireless power transfer phase, each typical ground IoT device is associated with the nearest UAV BS. The associated UAV BS flies towards the serving ground IoT device whilst transmitting energy.

Note that we assumed that each associated UAV flies at constant acceleration as in the beginning. Then, each UAV is stopped right above the typical user and remained aloft, so that the minimum path-loss fading between the typical IoT device and serving UAV in the information transmission process is guaranteed. In the first phase (i.e., from a hovering state to maximum velocity), an adaptive and dynamical solution has been designed where UAVs fly at constant acceleration to achieve the maximum velocity. Then, the UAVs decelerate to the destination, stopping and hovering on the top of the typical IoT device during the second duration (i.e., from the maximum velocity to hovering state). For further analysis, we calculated the instant velocity and constant acceleration has been calculated, which was based on the given distance $r_o$ expression as

$$v_1(r_o, \tau, t) = 4 r_o / (\tau T)^2 \quad 0 \leq t \leq \frac{\tau T}{2},$$

$$v_2(r_o, \tau, t) = (4 r_o - 4 r_o / \tau T) / (\tau T) \quad \frac{\tau T}{2} \leq t \leq \tau T,$$

where the acceleration can be expressed as

$$a_1(r_o, \tau) = 4 r_o / (\tau T)^2 \quad 0 \leq t \leq \frac{\tau T}{2},$$

$$a_2(r_o, \tau) = -4 r_o / (\tau T)^2 \quad \frac{\tau T}{2} \leq t \leq \tau T.$$

Note that $v_m = a_m \tau T / 2$ is the constant for the velocity, $0 < a_1(r_o, \tau) < a_m$ and $-a_m < a_2(r_o, \tau) < 0$ are the acceleration and the deceleration along the UAV’s flying direction, $a_m$ and $-a_m$ are the constant for the acceleration and deceleration, respectively.

**Theorem 1:** The average harvested energy for the associated typical IoT device served by the UAV-BSs with the power transfer time allocation $\tau$ is given by (11) on the top of this page. Note that the azimuth AoD $\theta^a$ and depression AoD $\theta^b$ from the associated UAV BS will change as the UAV flies, which adapt to the moving direction as the UAV BS flies.

**Proof 1:** Based on (11), the average harvested energy for a typical IoT device projection distance is written as

$$E_{sum}(r_o, \tau) = \eta \{ E_1(r_o, \tau) + E_2(r_o, \tau) \}.$$

The average harvested energy directly from the associated UAV BS can be written as

$$E_1(r_o, \tau) = P_T M_o \beta \left\{ \int_0^{\tau T/2} D(r_o - s_1(r_o, \tau, t)) dt + \int_{\tau T/2}^{\tau T} D(r_o - s_2(r_o, \tau, t)) dt \right\}$$

with

$$s_1(r_o, \tau, t) = \frac{2 r_o}{(\tau T)^2} t^2,$$

$$s_2(r_o, \tau, t) = \frac{4 r_o}{(\tau T)^2} t - \frac{2 r_o}{(\tau T)^2} t^2 - r_o,$$

where $s_1$ and $s_2$ are referred to the moving distance in the straight line during first phase and second phase, respectively, and $r_o$ is the distance between the staring point to the destination. To avoid the high efficiency association link and high moving cost, we prevent the association distance $r_o$ larger than $r_o(\tau) = a_m(\tau T)^2 / 4$, where the associated UAV cannot fly to the top of the typical user.

The ambient harvested energy $E_2$ under the prescribed association distance and time allocation is calculated as

$$E_2(\tau, r) = \tau T 2 \pi \lambda U \pi G_D \beta \int_0^{\tau T/2} \int_0^{2\pi} \left\{ \int_0^{r_o} D(U_1(\phi, t, u)) du + \int_{r_o}^{\tau T} D(U_2(\phi, t, u)) du \right\} d\phi du$$

$$\approx \tau T 2 \pi \lambda U \int_0^{\tau T/2} P_T G_D \beta D(u) du,$$

where $U_1$ and $U_2$ are the instant projection distance from interference UAV to the typical IoT device in the first and second phase at time $t$, respectively.

$$U_1(\phi, t, u) = \left( u^2 + s_1(\pi_i, \tau, t)^2 - 2 u s_1(\pi_i, \tau, t) \cos \phi \right)^{1/2},$$

$$U_2(\phi, t, u) = \left( u^2 + s_2(\pi_i, \tau, t)^2 - 2 u s_2(\pi_i, \tau, t) \cos \phi \right)^{1/2},$$

where $s_1(\pi_i, \tau, t)$ and $s_2(\pi_i, \tau, t)$ are obtained by interchanging the parameters $r_o \rightarrow r_o$ in (14), and $u$ is the projection distance from interference UAV to the typical IoT device. $\phi$ is the inclined angle with original interference UAV to the typical IoT device and the interference UAV to the destination IoT device. We simply use the average nearest distance to replace the dynamic distance from the interference UAV to its serving IoT device as $\pi_i = \int_0^r r_o f(r_o) dr_o$. 
\[
\mathcal{E}_{\text{sum}}(r_o, \tau) = \eta T 2\pi \lambda_t R \sum_{\text{d}} D(u) \, du \nonumber \\
+ \eta P_o M_o \beta \left\{ \int_0^{\tau T} D\left( r_o \left( 1 - 2 \left( \frac{t}{\tau T} \right)^2 \right) \right) dt + \int_{\tau T}^{\tau T} D\left( r_o \left( 2 - 4 \frac{t}{\tau T} + 2 \left( \frac{t}{\tau T} \right)^2 \right) \right) dt \right\}. \tag{11}
\]

Note that the approximation \((a)\) in (15) is obtained by assuming each interference UAV flies to the destination UAV with random inclined angle \(\phi\), which will counteract the impact of mobility. Moreover, consider the interference only has negligible effect on MMW links, then we can obtain it by approximating the generating function of PPP \([15]\). By applying (13) and (15) into (12), we obtain the desired result in (11).

**B. Ground-to-UAV Wireless Information Communication**

After the energy transfer phase, the IoT devices transmit their information signals to the associated UAV BSs \(^4\). Since the uplink information transmission energy consumed could not exceed the received energy \(\mathcal{E}_{\text{sum}}\), and the average transmit power in the ground IoT device is \(P_t(r_o, \tau) = \mathcal{E}_{\text{sum}}(r_o, \tau)/(1 - \tau)T\), where \(\mathcal{E}_{\text{sum}}(r_o, \tau)\) is given by (11).

**Theorem 2:** For a UAV BS associated with its intended ground IoT device, the average achievable rate at each UAV BS can be found as

\[
\mathcal{R}(r_o, \tau) = \frac{(1 - \tau)T}{\ln 2} \int_0^{\infty} \frac{1}{w} \left( 1 - \exp\left( -w M_o \beta H^{-\alpha_n} \right) \right) \\
\times \exp\left( -w 2\pi \lambda_t G_{\text{d}} \beta \int_0^{\infty} D(v) \, dv \right) \, dw. \tag{17}
\]

**Proof 2:** The average uplink rate from the typical ground IoT device to the associated UAV BS can be expressed as

\[
\mathcal{R}(r_o, \tau) = \frac{(1 - \tau)T}{\ln 2} \int_0^{\infty} \frac{1}{w} \left( 1 - e^{-w \gamma} \right) \, dw = \frac{(1 - \tau)T}{\ln 2} \\
\times \int_0^{\infty} \frac{1}{w} \left( 1 - e^{-w S} \right) e^{-w I} e^{-w \Delta C / \tau} \, dw. \tag{18}
\]

Since the received signal and interference are independent, we derive the signal expression as \(\Theta_S(w) = \exp(-w M_o \beta H^{-\alpha_n})\), and then \(\Theta_I(w)\) is calculated as

\[
\Theta_I(w) = \mathbb{E} \left\{ \exp\left( -w \sum_{k \in S_U} G_{U_k} \beta \frac{u_k^2 + H_{\alpha_k}}{\tau} \right) \right\} \\
\approx \exp\left\{ -w 2\pi \lambda_t G_{\text{d}} \beta \int_0^{\infty} D(v) \, dv \right\}. \tag{19}
\]

Substituting \(\Theta_S(w)\) and \(\Theta_I(w)\) into (18), we obtain the desired result (17).

**C. Energy Efficiency**

The energy efficiency of the overall UAV-to-ground downlink and uplink system is defined as the ratio of the average achievable rate to the total average power consumption. We consider the total average power consumption composed of the energy transfer phase and the information transfer phase, which includes flying power and hovering power consumption, respectively. This problem can be formulated as

\[
\mathbb{P} : \max_{\tau} B_{\text{low}}^E(\tau, r_o) = \int_0^{r_m(\tau)} \frac{R(r_o, \tau)}{\mathcal{E}_E(r_o, \tau) + \mathcal{E}_I(r_o, \tau)} f(r_o) \, dr_o, \tag{20}
\]

where the average flying energy \(\mathcal{E}_E(r_o, \tau)\) is given as

\[
\mathcal{E}_E(r_o, \tau) = \int_0^{\tau T} k_2 v_1(r_o, \tau, t) \Delta t + k_2 \frac{1 + |a(r_o)|^2 / g^2}{v_2(r_o, t)} \Delta t, \tag{21}
\]

where \(k_1\) and \(k_2\) are the constant values and \(g\) is the gravitation acceleration with the nominal value is 9.8 m/s\(^2\). The remaining consumption energy is \(\mathcal{E}_I(r_o, \tau) = \tau T P_t + (1 - \tau)T P_H\), while \(P_H\) is the hovering power which ensures that the UAV remains aloft \([5]\). We formulate the optimization problem to find the optimal time allocation of \(\tau\) to maximize the average energy efficiency. Since the optimization of the energy efficiency \(B_{\text{low}}^E\) for time allocation \(\tau\) does not permit a closed-form solution, we solve the problem by using a simple one-dimensional search in the numerical results.

**IV. Numerical Results and Discussions**

In this section, we present numerical results of UAV to ground channel characteristics and multiple 3D ULA antenna array on the achievable energy efficiency. We assume the bandwidth with BW = 1GHz, where the pathloss exponent are \(\alpha_L = 2.5\) and \(\alpha_N = 3.71\), respectively. The noise figure is \(N_f = 10\)dB, the noise power is \(\sigma^2 = -174 + 10 \log(10(BW)) + N_J\)dBm. Then we have the frequency-dependent constant value given by \(\beta = \left( \frac{c}{\pi f_c} \right)^2\) with \(c = 3 \times 10^8\)m/s. We also assume that \(k_1 = 9.26 \times 10^{-4}\) and \(k_2 = 2.25 \times 10^3\) in the constant for the UAV flying power \([5]\), \(a_m = 4\text{m/s}^2\), \(\eta = 0.9\), \(P_U = 46\text{ dBm}\), \(M_o = 16\), \(P_H = 80\text{ W}\). In the ULA configuration, we choose the antenna spacing as half wavelength \(\Delta \kappa = \frac{1}{2} \phi\).

The blockages are modeled as \([16]\), and the LoS connection probability function in a network is computed as

\[
p_L(X) = 1 + a \exp(-b [\arctan(H/X) - a]), \tag{22}
\]

where \(a = 9.6\) and \(b = 0.28\), respectively. For comparison, we consider the static hovering scheme, in which all the UAVs hover at their original location and do not fly to the IoT devices.
V. Conclusions and Future Work

This letter has proposed an improved dynamic process for downlink wireless power transfer and uplink information transfer architecture for UAV-to-ground networks. Based on the adaptive flying scheme, each link minimizes path loss fading and avoids blockage effects. We have considered SE and EE in order to evaluate the performance of this network. The numerical results indicated that although the proposed moving scheme consumed considerable energy, it still demonstrated considerable advantages for SE and EE as compared to the conventional static hovering network. Besides, optimizing the time allocation can maximize SE and EE, respectively. We expect future advances to reduce the energy consumption of UAV flights and to design a tradeoff between EE and SE.

REFERENCES