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# Alloy selections in high-temperature metal hydride heat pump systems for industrial waste heat recovery

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#### ARTICLE INFO

Article history: Received 20 December 2021 Received in revised form 12 February 2022 Accepted 23 February 2022 Available online xxxx

Keywords: Waste heat recovery High-temperature metal hydride (MH) heat pumps Alloy selections System efficiencies

### ABSTRACT

In an energy intensive industrial site such as a steel plant, there are plenty of medium and low temperature waste heat which could be recovered for heating purposes with advanced and feasible technologies for example metal hydride (MH) heat pumps. Compared to other heat pump systems such as those with compression and absorption cycles, the MH heat pump has some distinctive advantages including low carbon system in terms of less electricity input and environmentally friendly working mediums, compactness, and most importantly achievable heat output with relatively high temperature. However, the applicable alloys for the high-temperature MH heat pump systems are critical and need to be purposely selected. Accordingly, in this paper, a comprehensive procedure to select alloys for the high-temperature BMH heat pump systems of literatures, totally 82 alloys are potentially used for this special application of which 1560 alloy pairs are formed and each pair consists of one high-temperature alloy and another low-temperature alloy. Subsequently, a number of applicable alloys are selected for each designed temperature of heat pump output and one pair is ultimately finalised. The alloy can be further examined considering of its thermophysical properties, heat transfer behaviours, costs and safety issues.

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#### 1. Introduction

Industrial waste heat recovery for decarbonised heating and cooling is an attractive concept that could simultaneously reduce fossil fuel consumption and CO<sub>2</sub> emissions. In the UK, based on a recent report, of the total industrial waste heat sources, about 28 TWh/yr could be potentially used in district heat networks (Anon, 2014). The waste heat sources from different industrial sectors can have different temperature grades and various applications.

\* Corresponding author. E-mail address: yunting.ge@lsbu.ac.uk (Y.T. Ge). For the low grade heat sources with temperature below 230 °C, Organic Rankine Cycles (ORCs) might be applied for potential power generations. However, the thermal (electric) efficiency of an ORC with the low grade heat source is quite low (about 10% or below) which might not be a good investment from the economic point of view (L. Li et al., 2017). In addition, a typical energy intensive industrial site such as steel plant also has plenty of waste heat with extra low grade around 40 °C which is conventionally exhaust to ambient directly (Patsos, 2010). These low grade waste heat sources can be combined with some advanced energy conversion systems such as heat pump to produce average low grade heat sources at temperature around 130 °C which

https://doi.org/10.1016/j.egyr.2022.02.279

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| Nomenclature   |   |
|----------------|---|
| $C_v$          | specific heat at constant volume (J/mol<br>alloy K) |
| C <sub>p</sub> | specific heat at constant pressure (J/kg<br>K)      |
| COA            | coefficient of amplification                        |
| $\Delta H$     | standard enthalpy ( $kJ/mol H_2$ )                  |
| HT             | high temperature                                    |
| LT             | low temperature                                     |
| n              | molar number  |
| Р              | pressure (atm)                                      |
| Q              | heat capacity (W or kW)                             |
| R              | universal gas constant                              |
| $\Delta S$     | standard enthalpy and entropy (J/mol                |
|                | H <sub>2</sub> K)                                   |
| Т              | Temperature (K)                                     |
| W              | Weight (kg)   |
| WM             | molar weight (g/mol)                                |
| $\psi$         | exergy efficiency                                   |
| Subscripts     |   |
| с              | Carnot  |
| h              | high  |
| 1              | low   |
| m, MH          | metal hydride                                       |
| R              | reactor   |
| t              | transfer  |
| 1              | reactor one   |
| 2              | reactor 2   |
|                |   |

are more applicable for district heating at remote areas. Correspondingly, the conventional absorption or adsorption heat pump systems might be applied but they are hard to obtain heat output with temperature as high as 130 °C. Alternatively, a hydrogen related technology namely metal hydride (MH) heat pump can be a feasible option to achieve a high temperature heat output. Its working mechanism is quite similar to that of absorption or adsorption heat pump. However, for a MH heat pump, high and low temperature metal hydride alloys and hydrogen working fluid are applied to absorb heat from high and low temperature heat resources and produce heat at medium temperature. Meanwhile, the hydrogen desorption and absorption processes are conducted respectively during the heat input and output operations. Comparing to absorption or adsorption heat pump, the MH heat pump has similar operation efficiency but is more compact and can achieve higher temperature heat output. The MH heat pump has been investigated mostly in conventional heat pump systems (Gamnini, 1989; Bjurstrom and Suda, 1989), but has not been applied in district heating systems with industrial waste heat due to relatively high temperature heat input and output. To facilitate this, one of the critical points is to select appropriate alloy pairs for the MH heat pump at the applicable operating conditions and acceptable system performance efficiency.

Conventionally, the applicable alloys for the MH heat pump (MHHP) systems are categorised as intermetallics with conventions of AB, AB<sub>2</sub>, A<sub>2</sub>B and AB<sub>5</sub>, where 'A' is usually a lanthanide element (Atomic numbers 57–71), such as La, or mischmetal (rare earth metal mixture), and 'B' is Ni, Co, Al, Mn, Fe, Sn, Cu, Ti etc. (D. Chandra et al., 2006). In addition, element 'A' refers to rare earth and alkaline elements, presenting a high affinity for hydrogen to form stable hydride, while element 'B' is generally a

transition metal and it usually presents a poor affinity for hydrogen and thus forming unstable hydrides (Pavá Herrero, 2010). The  $A_x B_y$  alloys can be modified by changing the alloy composition of x or y such that metal hydride with suitable properties can be formed (Nakamura et al., 1997; Muthukumar and Groll, 2010). Therefore, plenty of such alloys have been synthesised, characterised and are recommended for use in MHHPs. In addition, these intermetallic materials can be used as either low or high temperature alloys in their associated heat pump systems based on their corresponding operating temperatures and pressures. Satheesh and Muthukumar (2010) investigated a single-stage metal hydride heat pump working with five different alloy pairs of AB<sub>5</sub>, AB<sub>2</sub>, AB types of alloys. These included MmNi<sub>4.6</sub>Al<sub>0.4</sub>/ MmNi<sub>4.6</sub>Fe<sub>0.4</sub>, LaNi<sub>4.61</sub>Mn<sub>0.26</sub>Al<sub>0.13</sub>/La<sub>0.6</sub>Y<sub>0.4</sub>Ni<sub>4.8</sub>Mn<sub>0.2</sub>, LmNi<sub>4.91</sub> Sn<sub>0.15</sub>/Ti<sub>0.99</sub>Zr<sub>0.01</sub>V<sub>0.43</sub>Fe<sub>0.09</sub>Cr<sub>0.05</sub>Mn<sub>1.5</sub>, LaNi<sub>4.6</sub>Al<sub>0.4</sub>/MmNi<sub>4.15</sub>Fe<sub>0.85</sub> and  $Zr_{0.9}Ti_{0.1}Cr_{0.9}Fe_{1.1}/Zr_{0.9}Ti_{0.1}Cr_{0.6}Fe_{1.4}$ . The high (T<sub>H</sub>), medium  $(T_M)$  and low  $(T_I)$  MH temperatures in the system were in the ranges of 110~170 °C, 25~35 °C and -30~20 °C respectively, while the high and low operating pressures were in the ranges of  $30 \sim 40$  bar and  $0.1 \sim 2$  bar each. Based on the calculated system COP with each alloy pair, the optimum operating temperature ranges of each pair were suggested. At a heat source temperature of 130 °C and a refrigeration temperature of 20 °C, a single-stage MHHP working with LmNi<sub>4.91</sub>Sn<sub>0.15</sub>/ Ti<sub>0.99</sub>Zr<sub>0.01</sub>V<sub>0.43</sub>Fe<sub>0.09</sub>Cr<sub>0.05</sub> Mn<sub>1.5</sub> was investigated numerically and experimentally (Linder and Laurien, 2009). The COP was calculated as 0.25 which was relatively low. A MHHP with MmNi<sub>4.5</sub>Al<sub>0.5</sub>/MmNi<sub>4.2</sub>Al<sub>0.1</sub>Fe<sub>0.7</sub> MH alloy pair was studied theoretically by Mellouli et al. (2009). For the operating temperature ranges of 52~167 °C/0~20 °C/-23~-8 °C (TH/TM/TL), the COP was calculated as 0.45~0.5. There are also some other research investigations from literatures on MHHPs (Qin et al., 2007; Ni and Liu, 2007; Lee et al., 1995). The heat source temperature can be as high as 200 °C but the heat output temperatures are mostly below 50 °C. If a MHHP is applied for space heating purpose, a higher heat output temperature up to 100 °C is required. In addition, for the applications of industrial processes, the heat output temperature from the heat pump up to 150 °C is expected (George et al., 2020). However, such a high temperature is hard to be achieved with conventional compression and absorption heat pumps. Potentially, the MHHPs can obtain the heat output with such a high temperature but the applied MH alloys should be purposely selected, which have not been done yet from literatures.

Subsequently, in this paper, a comprehensive procedure to select alloys for the high-temperature MH heat pump systems is explained based on the operating temperatures, system efficiencies and thermodynamic equilibriums. From the database of literatures, totally 82 alloys are potentially used for this special application of which 1560 alloy pairs are formed and each pair consists of one high-temperature alloy and another low-temperature alloy. Subsequently, a number of applicable alloys are selected for each designed temperature of heat pump heat output. An applicable MH alloy pair is thus finalised based on its operating pressures and performance efficiencies.

#### 2. System description

The schematic diagram of the MHHP system and its operating cycle on a Van't Hoff plot is shown in Fig. 1. As depicted, the system consists of two MH reactor pairs, MH1a and MH2a, and MH1b and MH2b. Each pair has one high temperature MH reactor (MH1a or MH1b) and one low temperature MH reactor (MH2a or MH2b). For each MH reactor pair, a hydrogen connection pipe with a control valve is connected in-between to facilitate hydrogen to flow between two reactors. In the system, there are one heat input ( $Q_h$ ) with high temperature ( $T_h$ ), one heat input ( $Q_l$ )



**Fig. 1.** Schematic diagram of a single stage metal hydride heat pump and its operating cycle on a Van't Hoff plot . ( $Q_h$  =heat input at high temperature heat source  $T_h$ ;  $Q_{m1}$ ,  $Q_{m2}$ =heat outputs at output temperature  $T_m$ ;  $Q_l$ =Heat absorption at low temperature heat source  $T_l$ ).

with low temperature  $(T_1)$ , and two heat outputs  $(Q_{m1} \text{ and } Q_{m2})$ with medium temperature (T<sub>m</sub>). The system operation consists of two half cycles. For the first half cycle (solid line in the system layout), the high temperature heat Q<sub>h</sub> is input to MH1a such that hydrogen (H2) is desorbed from MH1a and passes through the H2 connection pipe and is absorbed by MH2a. The reaction heat Q<sub>m2</sub> at temperature T<sub>m</sub> during the absorption process is therefore released from MH2a. Meanwhile, the low temperature heat Q<sub>1</sub> is added to MH2b to desorb H2 from the reactor. The H2 released from MH2b then passes through the H2 connection pipe and is absorbed by MH1b such that the heat  $Q_{m1}$  at temperature  $T_m$  is released. For the second half cycle (dot line in the system layout), the directions of heat inputs to and outputs from the reactors are swapped. In that case, Q<sub>h</sub> and Q<sub>l</sub> are inputs to MH1b and MH2a respectively while  $Q_{m1}$  and  $Q_{m2}$  are outputs from MH1a and MH2b each. In addition, the H2 flows in those two connection pipes flow in opposite directions to those in the first half cycle. The operating cycle can thus ensure continuous operation of the system. It should be noted that the temperatures of heat source  $(T_h \text{ and } T_l)$  and heat sink  $(T_m)$  are assumed the same as those of their corresponding reactors.

#### 3. MH alloy selection

#### 3.1. Thermodynamic analysis

For the application of industrial waste heat recovery using the MHHP system described in Section 2, the designed temperature ranges of high temperature ( $T_h$ ), medium temperature ( $T_m$ ) and low temperature ( $T_1$ ) heat sources are specified as 180~240 °C, 120~140 °C and 25~45 °C respectively. For the hydrogen absorption or desorption process of a MH reactor in the system, the MH alloy (M) reacts reversibly with hydrogen ( $H_2$ ) as follows:

$$M + (\frac{x}{2})H_2 \stackrel{absorption}{\rightleftharpoons} MH_x + Q \tag{1}$$

where x is the hydrogen atom number in the metal hydride, Q is heat release during hydrogen absorption (exothermic) process or heat input during hydrogen desorption (endothermic) process. For each reaction process, the van't Hoff's law applies with following form:

$$\ln P_{\rm H_2} = -\frac{\Delta H \times 1000}{RT} + \frac{\Delta S}{R}$$
(2)

where  $P_{H_2}(atm)$  is hydrogen pressure,  $\Delta H$  (kJ/mol H<sub>2</sub>) and  $\Delta S$  (J/mol H<sub>2</sub>.K) are the standard enthalpy and entropy of hydride formation respectively, R is the gas constant (8.134 J/mol.K) and *T* is the hydrogen temperature (K). This equation is schematically

represented in Fig. 1 for both MH1 and MH2 with two reaction processes including desorption and absorption. For a particular MH, the  $\Delta$ H and  $\Delta$ S are fixed such that the hydrogen absorption or desorption pressure is a function of reactor or hydrogen temperature only. For this MHHP system, since the designed temperatures of  $T_h$ ,  $T_m$  and  $T_l$  are specified, the corresponding hydrogen pressure  $P_h$ ,  $P_{m1}$ ,  $P_{m2}$  and  $P_l$  can be calculated with Eq. (2).  $P_{m1}$  and  $P_{m2}$  represent hydrogen pressures in MH1 and MH2 respectively at the same medium temperature T<sub>m</sub>. As seen from Fig. 1, the system operates at two different pressure levels, high and low. At the high pressure level, the hydrogen with temperature  $T_{\rm h}$  and pressure  $P_{\rm h}$  is desorbed at MH1 and flows to MH2 at temperature  $T_m$  and pressure  $P_{m2}$  and is absorbed there. At the low pressure level, the hydrogen with temperature T<sub>1</sub> and pressure P<sub>1</sub> is desorbed at MH2 and flows to MH1 at temperature  $T_m$  and pressure  $P_{m1}$  and is absorbed there. Practically, to enable the hydrogen to flow from one reactor to another, the pressure P<sub>h</sub> and P<sub>l</sub> should be slightly higher than P<sub>m2</sub> and P<sub>m1</sub> respectively. However, to facilitate the MH alloy selection, P<sub>h</sub> and P<sub>l</sub> are assumed the same as  $P_{m2}$  and  $P_{m1}$  correspondingly. In that case, the following formulas will follow:

$$-\frac{\Delta H_1 \times 1000}{T_h} + \Delta S_1 = -\frac{\Delta H_2 \times 1000}{T_m} + \Delta S_2 \tag{3}$$

$$-\frac{\Delta H_1 \times 1000}{T_m} + \Delta S_1 = -\frac{\Delta H_2 \times 1000}{T_l} + \Delta S_2 \tag{4}$$

where, the subscripts 1 and 2 indicate the MH reactor 1 (MH1) and 2 (MH2) respectively. To simply, two parameters of  $\eta$  and  $\xi$  are defined as below:

$$\eta = \frac{\Delta S_1 - \Delta S_2}{\Delta H_2} \tag{5}$$

$$\xi = \frac{\Delta H_1}{\Delta H_2} \tag{6}$$

Accordingly, the following equations are obtained:

$$\eta = \left(\frac{\xi}{T_h} - \frac{1}{T_m}\right) \times 1000\tag{7}$$

$$\eta = (\frac{\xi}{T_m} - \frac{1}{T_l}) \times 1000$$
(8)

From Eqs. (5) and (6), the parameters  $\eta$  and  $\xi$  are the functions of thermophysical properties of the MH alloy pair applied particularly the values of their  $\Delta$ H and  $\Delta$ S. Based on Eqs. (7) and (8), the parameters  $\eta$  and  $\xi$  are also constrained by the operating temperatures of T<sub>h</sub>, T<sub>m</sub> and T<sub>l</sub>. Therefore, at specified temperature ranges of T<sub>h</sub>, T<sub>m</sub> and T<sub>l</sub>, the potential MH alloy pairs used in the MHHP system can be identified. From literature review, as listed in Table 1, totally 82 MH alloys are chosen



**Fig. 2.** Coordinate points  $(\xi, \eta)$  for all the available MH alloy pairs.

from which the potential MH alloy pairs for the MHHP system will be selected (Satheesh and Muthukumar, 2010; Dantzer and Orgaz, 1986; Huston, 1980; Kim et al., 1997; Yasuda et al., 2013; Lototskyy et al., 2016; Qin et al., 2007b; Skripnyuk and Ron, 1999; Linder and Kulenovic. 2011: Rusman and Dahari. 2016: Weckerle et al., 2019). As listed in the table, the important parameters of  $\Delta H$  and  $\Delta S$  for each MH alloy are listed. In addition, for this particular MHHP, it is known that the lowest average MH reactor temperature T<sub>1</sub> is 35 °C. Correspondingly, the hydrogen pressure P<sub>1</sub> is calculated for each MH reactor. In the proposed system, it consists of two identical high temperature (HT) MH alloys and two identical low temperature (LT) MH alloys. Therefore, two types of MH alloys, HT and LT, need to be identified in the system. To classify, if the calculated P<sub>1</sub> is less than 1 bar, the MH alloy is HT one otherwise it is LT one. Subsequently, of the total 82 MH alloys, 30 are classified as HT types and 52 are belonged to LT alloys. For each HT MH alloy, it can be paired with any of the LT MH alloys such that totally 1560 MH pairs can be formed.

Based on the Eqs. (5) and (6), the coordinate points  $(\xi, \eta)$  of all the available MH alloy pairs (1560 in total) can be demonstrated in a  $\xi - \eta$  diagram, as shown in Fig. 2. From this statistical diagram, it can see roughly a linear relation between  $\eta$  and  $\xi$ although further verification is needed. In addition, according to Eqs. (7) and (8), at a constant  $T_h$  and  $T_m$  or constant  $T_l$  and  $T_m$ , a straight line of function  $\eta(\xi)$  can be drawn. From the system design, the maximum and minimum values of T<sub>h</sub> are set to 220 °C and 180 °C respectively, while the maximum and minimum values of T<sub>1</sub> are set to 25 °C and 45 °C each. Therefore, at a constant T<sub>m</sub>, four straight lines at the maximum and minimum values of  $T_h$  and  $T_l$  can be shown in the same diagram. Correspondingly, when temperatures of  $T_m$  are set to 120 °C, 130 °C and 140 °C coordinate points  $(\boldsymbol{\xi}, \boldsymbol{\eta})$  for the available MH alloys and four straight lines at maximum and minimum temperatures of T<sub>h</sub> and  $T_1$  are shown in Figs. 3–5 respectively. At a constant  $T_m$ , the system should operate with the temperatures of T<sub>h</sub> and T<sub>l</sub> at their respective temperature ranges. As such, the coordinate points ( $\xi$ ,  $\eta$ ) representing the applicable MH alloy pairs (solid circles in the diagram) should be enclosed with those four straight lines. Subsequently, there are 109, 35 and 12 applicable MH alloy pairs for T<sub>m</sub> temperatures at 120 °C, 130 °C and 140 °C respectively. It can be seen that the higher the heat pump output temperature is the less the applicable MH alloy pairs would be. However, the applicable MH alloys need to be further evaluated and identified based on the system performance when these alloy pairs are applied.

It should be noted that due to the inherent hysteresis in a MH alloy, at a constant temperature the MH absorption pressure is higher than that of desorption pressure. However, to simplify the selection procedure, the effect of the hysteresis on the MH alloy selection is neglected. In a practical application, once the MH alloys are identified, the heat source and sink temperatures can always be adjusted slightly to meet the pressure difference requirement of hydrogen transfer between two reactors.

#### 3.2. Operation analysis

To analyse the system performance at the specified operating condition and MH alloy pairs, the energy input or output from each MH reactor in the system shown in Fig. 1 needs to be identified and calculated. To achieve that, it is necessary to fully understand the system operating cycle and the role of each MH reactor. For the HT MH reactors MH1a and MH1b, one reactor receives heat  $Q_h$  and another releases heat  $Q_{m1}$  for the first half cycle while for the second half cycle, the roles of these two reactors are changed over. Similarly, for the LT MH reactors MH2a and MH2b, one reactor receives heat  $Q_{I}$  and another releases heat  $Q_{m2}$  for the first half cycle while for the second half cycle, the roles of these two reactors are swapped. In addition, the directions of hydrogen transports from one reactor to another also changed over between two half cycles. Subsequently, the  $Q_h$ ,  $Q_{m1}$ ,  $Q_{m2}$  and  $Q_I$  can be calculated by Eqs. (9) to (12) respectively.

$$Q_h = n_{t1}\Delta H_1 + (n_1 C v_1 + W_{1R} C p_{1R})(T_h - T_m)$$
(9)

$$Q_{m1} = n_{t2}\Delta H_1 + (n_1 C v_1 + W_{1R} C p_{1R}) (T_h - T_m)$$
(10)

$$Q_{m2} = n_{t1}\Delta H_2 - (n_2 C v_2 + W_{2R} C p_{2R}) (T_m - T_l)$$
(11)

$$Q_l = n_{t2} \Delta H_2 - (n_2 C v_2 + W_{2R} C p_{2R})(T_m - T_l)$$
(12)

In these equations,  $n_{t1}$  and  $n_{t2}$  are the total amount of hydrogen (mol) transferred from reactor MH1 and MH2 respectively, which should be the same at steady state. The  $n_{t1}$  or  $n_{t2}$  can be calculated based on the weight and gravimetric hydrogen storage capacity of respective metal hydride alloy charged in the reactor. The  $n_1$  and  $n_2$  are the number of moles of MH alloys for MH1 and MH2 respectively, which are dependent on the weight and type of MH alloy charged in each reactor. The  $W_{1R}$  and  $W_{2R}$  are the metal weight of reactor MH1 and MH2 respectively. The  $Cp_{1R}$ and  $Cp_{2R}$  are the specific heat capacity of metal reactor MH1 and MH2 respectively. It is noted that at the stage of MH alloy selection, the heat capacity rate of each reactor is not included in the energy calculation. However, these heat capacity rates should

|          |  | kJ/mol H2      | J/K/mol H2      | °C | bar       |           |                                  |
|----------|--|----------------|-----------------|----|-----------|-----------|----------------------------------|
| 1        | Mg(LaNis)20%   | 76.99          | 138.32          | 35 | 1.517E-06 | HT        | Dantzer and Orgaz (1986)         |
| 2        | Mg <sub>2</sub> Cu   | 72.80          | 142.34          | 35 | 1.258E-05 | HT        | Huston (1980)                    |
| 3        | Mg <sub>2</sub> Ni   | 64.43          | 122.30          | 35 | 2.962E-05 | HT        | Huston (1980)                    |
| 4        | Mg <sub>2 4</sub> Ni   | 64.31          | 122.30          | 35 | 3.111E-05 | HT        | Dantzer and Orgaz (1986)         |
| 5        | LaNia os Mno 94  | 48.70          | 116.90          | 35 | 7.186E-03 | HT        | Dantzer and Orgaz (1986)         |
| 6        | LaNi <sub>4</sub> Al   | 47.70          | 118.83          | 35 | 0.013     | HT        | Dantzer and Orgaz (1986)         |
| 7        | $Z r_0 \circ Ce_0 \circ Mn_2$  | 44.89          | 110.00          | 35 | 0.014     | HT        | Dantzer and Orgaz (1986)         |
| 8        | $LaNi_{4,20}Mn_{0,70}$   | 44.27          | 115.14          | 35 | 0.033     | HT        | Dantzer and Orgaz (1986)         |
| 9        | NiZr   | 30.42          | 7163            | 35 | 0.039     | HT        | Dantzer and Orgaz (1986)         |
| 10       | ZrMn <sub>2</sub> Cu <sub>2</sub>  | 25.82          | 57.74           | 35 | 0.044     | нт        | Kim et al. (1997)                |
| 11       | LaNia as Alo as  | 44 35          | 117 99          | 35 | 0.045     | HT        | Dantzer and Orgaz (1986)         |
| 12       | $2rMn_2Cu_{2,2}$   | 25.82          | 57.91           | 35 | 0.045     | нт        | Dantzer and Orgaz (1986)         |
| 12       |  | 35.60          | 94.65           | 35 | 0.043     | нт        | Vasuda et al. (2013)             |
| 14       | $7r_0 - Ti_0 - Mn_0$   | 32 30          | 87.36           | 35 | 0.002     | нт        | Dantzer and Orgaz (1986)         |
| 15       |  | 39.50          | 113 22          | 35 | 0.124     | нт        | Dantzer and Orgaz (1986)         |
| 16       | Ear Nia - Ti   | 41 00          | 119.22          | 35 | 0.100     | нт        | Huston (1980)                    |
| 17       | I aNi - Ala -  | 38.40          | 111 20          | 35 | 0.102     | нт        | Dantzer and Orgaz (1986)         |
| 17       | LaNi Mp. Al.   | 37.00          | 110.25          | 25 | 0.137     | 111<br>UT | Sathoosh and Muthukumar (2010)   |
| 10       | Latvi $4.61$ Where Alexa   | 27.20          | 04.60           | 25 | 0.221     | 111<br>UT | Satheesh and Muthukumar (2010)   |
| 19       | $Lalvi_{4.61}$ WD  | 32.30<br>37.93 | 94.09<br>112.55 | 25 | 0.291     |           | Dantzer and Orgaz (1986)         |
| 20<br>21 | LaNi Al.   | 36.40          | 100.20          | 25 | 0.237     | 111<br>UT | Dantzer and Orgaz (1980)         |
| 21<br>วว | ZrMp   | 10.40          | FD 20           | 25 | 0.340     |           | Dantzer and Orgaz (1986)         |
| 22       | $Z_{IIVIII}_{2.8}$   | 10.41          | 52.50<br>85.60  | 25 | 0.414     |           | Sathoosh and Muthukumar (2010)   |
| 23       | 210.9110.1C10.9FC1.1   | 27.97          | 03.00<br>100.75 | 22 | 0.344     |           | Sattleesh allu Muthukumai (2010) |
| 24       | LdNI4.7AI0.3   | 33.89          | 106.75          | 30 | 0.087     |           | Huston (1980)                    |
| 25       |  | 19.71          | 61.50           | 35 | 0.755     | HI        | Dantzer and Orgaz (1986)         |
| 26       | LaNI <sub>4.75</sub> AI <sub>0.25</sub>                                  | 34.73          | 110.46          | 35 | 0.774     | HI        | Dantzer and Orgaz (1986)         |
| 27       | CalNI5   | 31.80          | 101.18          | 35 | 0.796     | HI        | Huston (1980)                    |
| 28       | $V_{0.9}Cr_{0.1}$  | 41./1          | 133.89          | 35 | 0.848     | HI        | Kim et al. (1997)                |
| 29       | LaN1 <sub>4.83</sub> Min <sub>0.17</sub>                                 | 34.52          | 111.25          | 35 | 0.924     | HT        | Dantzer and Orgaz (1986)         |
| 30       | LaN1 <sub>4.8</sub> Al <sub>0.2</sub>                                    | 34.90          | 112.65          | 35 | 0.942     | HT        | Lototskyy et al. (2016)          |
| 31       | LaN1 <sub>4.6</sub> Al <sub>0.4</sub>                                    | 30.68          | 99.73           | 35 | 1.034     | LT        | Satheesh and Muthukumar (2010)   |
| 32       | $La_{0.6}Y_{0.4}Ni_{4.9}Al_{0.1}$  | 26.85          | 87.35           | 35 | 1.040     | LT        | Qin et al. (2007b)               |
| 33       | $\operatorname{ZrCr}_{0.6}\operatorname{Fe}_{1.4}$                       | 26.90          | 89.50           | 35 | 1.319     | LT        | Dantzer and Orgaz (1986)         |
| 34       | Zr <sub>0.8</sub> Ti <sub>0.2</sub> MnFe                                 | 11.13          | 39.25           | 35 | 1.476     | LT        | Dantzer and Orgaz (1986)         |
| 35       | LaNi <sub>4.9</sub> Al <sub>0.1</sub>                                    | 32.64          | 110.46          | 35 | 1.752     | LT        | Dantzer and Orgaz (1986)         |
| 36       | LaNi <sub>4.95</sub> Mn <sub>0.05</sub>                                  | 32.30          | 110.37          | 35 | 1.976     | LT        | Dantzer and Orgaz (1986)         |
| 37       | LaNi <sub>5</sub>  | 31.80          | 110.04          | 35 | 2.309     | LT        | Dantzer and Orgaz (1986)         |
| 38       | Zr <sub>0.9</sub> Ti <sub>0.1</sub> Cr <sub>0.6</sub> Fe <sub>1.4</sub>  | 23.61          | 85.23           | 35 | 2.860     | LT        | Satheesh and Muthukumar (2010)   |
| 39       | LmNi <sub>4.91</sub> Sn <sub>0.15</sub>                                  | 25.90          | 93.82           | 35 | 3.282     | LT        | Satheesh and Muthukumar (2010)   |
| 40       | $MNi_{4.5}Al_{0.46}Fe_{0.05}$  | 31.05          | 110.88          | 35 | 3.426     | LT        | Kim et al. (1997)                |
| 41       | $Zr(Fe_{0.75}Cr_{0.25})_2$   | 24.77          | 91.63           | 35 | 3.920     | LT        | Kim et al. (1997)                |
| 42       | La <sub>0.6</sub> Y <sub>0.4</sub> Ni <sub>4.8</sub> Mn <sub>0.2</sub>   | 23.25          | 86.78           | 35 | 3.961     | LT        | Satheesh and Muthukumar (2010)   |
| 43       | Fe <sub>0.85</sub> Mn <sub>0.15</sub> Ti                                 | 29.46          | 107.11          | 35 | 4.052     | LT        | Kim et al. (1997)                |
| 44       | Ce <sub>0.5</sub> La <sub>0.5</sub> Ni <sub>2.5</sub> Cu <sub>2.5</sub>  | 23.01          | 86.61           | 35 | 4.255     | LT        | Kim et al. (1997)                |
| 45       | Fe <sub>0.9</sub> Mn <sub>0.1</sub> Ti                                   | 29.29          | 107.00          | 35 | 4.269     | LT        | Huston (1980)                    |
| 46       | La <sub>0.6</sub> Y <sub>0.4</sub> Ni <sub>4.8</sub> Mn <sub>0.2</sub>   | 27.05          | 100.50          | 35 | 4.678     | LT        | Satheesh and Muthukumar (2010)   |
| 47       | Z r <sub>0.8</sub> Ti <sub>0.2</sub> Cr <sub>0.6</sub> Fe <sub>1.4</sub> | 26.90          | 100.46          | 35 | 4.929     | LT        | Dantzer and Orgaz (1986)         |
| 48       | Ca <sub>0.7</sub> M <sub>0.3</sub> Ni <sub>5</sub>                       | 26.78          | 100.42          | 35 | 5.151     | LT        | Kim et al. (1997)                |
| 49       | Ca <sub>0.7</sub> M <sub>0.3</sub> Ni <sub>5</sub>                       | 26.78          | 100.43          | 35 | 5.161     | LT        | Huston (1980)                    |
| 50       | MmNi 4.6Al <sub>0.4</sub>  | 24.68          | 93.82           | 35 | 5.278     | LT        | Satheesh and Muthukumar (2010)   |
| 51       | Ce <sub>1.1</sub> Ni <sub>2.5</sub> Cu <sub>2.5</sub>                    | 20.71          | 81.04           | 35 | 5.350     | LT        | Dantzer and Orgaz (1986)         |
| 52       | MNi <sub>4.5</sub> Al <sub>0.5</sub>                                     | 28.03          | 104.84          | 35 | 5.372     | LT        | Huston (1980)                    |
| 53       | MNi <sub>4.5</sub> Al <sub>0.05</sub>                                    | 28.03          | 105.44          | 35 | 5.772     | LT        | Kim et al. (1997)                |
| 54       | FeTi   | 28.03          | 106.09          | 35 | 6.242     | LT        | Huston (1980)                    |
| 55       | V <sub>0.95</sub> Cr <sub>0.05</sub>                                     | 37.36          | 139.33          | 35 | 8.913     | LT        | Kim et al. (1997)                |
| 56       | Ca <sub>0.5</sub> M <sub>0.5</sub> Ni <sub>5</sub>                       | 25.77          | 103.76          | 35 | 11.400    | LT        | Kim et al. (1997)                |
| 57       | CeNi 25Cu25  | 16.90          | 75.31           | 35 | 11.867    | LT        | Dantzer and Orgaz (1986)         |
| 58       | MmNi 46Fe04  | 21.68          | 91.22           | 35 | 12.432    | LT        | Satheesh and Muthukumar (2010)   |
| 59       | CeNi <sub>3</sub> Cu <sub>2</sub>  | 15.31          | 70.58           | 35 | 12.500    | LT        | Dantzer and Orgaz (1986)         |
| 60       | CeNi 4 5 Alo 5   | 21.88          | 92.05           | 35 | 12.722    | LT        | Kim et al. (1997)                |
| 61       | Tio 95 Zro 05 Mn 1 48 Vo 43 Feo 08 Alo 01                                | 25.35          | 103.65          | 35 | 13.267    | LT        | Skripnyuk and Ron (1999)         |
| 62       | $Ti_{0.95}Zr_{0.05}Mn_{1.46}V_{0.45}Fe_{0.09}$                           | 25.26          | 103.55          | 35 | 13.578    | LT        | Linder and Kulenovic (2011)      |
| 63       | MmNi 4 15 Fe0 85   | 21.73          | 92.13           | 35 | 13.641    | LT        | Satheesh and Muthukumar (2010)   |
| 64       | V0 025 CT0 075   | 36.32          | 139.75          | 35 | 14.099    | LT        | Kim et al. (1997)                |
| 65       | CeNi <sub>3</sub> Zr <sub>2</sub>  | 29.55          | 118.25          | 35 | 14.897    | LT        | Rusman and Dahari (2016)         |
| 66       | MNi <sub>4</sub> 15 Feo 85   | 25.10          | 104.60          | 35 | 16.372    | LT        | Kim et al. (1997)                |
| 67       | MNi <sub>4</sub> 15 Fe <sub>0.85</sub>                                   | 25.10          | 104.76          | 35 | 16.683    | LT        | Huston (1980)                    |
| 68       | Cao 4 Mo 6 Nis   | 25.27          | 105.44          | 35 | 16.961    | LT        | Kim et al. (1997)                |
| 69       | $Ti_0 \propto Zr_0 \approx V_0 \ll Fe_0 \propto Cr_0 \approx Mn_1 \ll$   | 19.85          | 87.85           | 35 | 16.974    | <br>LT    | Weckerle et al. (2019)           |
| 70       | CeNi <sub>4</sub> Zr   | 21.08          | 93 30           | 35 | 20 220    | LT        | Rusman and Dahari (2016)         |
| 71       | PrNi <sub>c</sub>  | 29.04          | 119.24          | 35 | 20 529    | LT        | Kim et al. (1997)                |
| 72       | NdNi <sub>5</sub>  | 27.82          | 116 32          | 35 | 23,177    | LT        | Kim et al. (1997)                |
| 73       | $Ti_{0.99}Zr_{0.01}V_{0.43}Fe_{0.09}Cr_{0.05}Mn_{1.5}$                   | 19.77          | 90.35           | 35 | 23.620    | LT        | Linder and Kulenovic (2011)      |
| -        | 0.00 - 0.01 - 0.40 - 0.09 - 0.00 - 0.00                                  |                |                 |    |           |           |                                  |

No

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Table 1MH alloys to be selected. Alloy

 ${\bigtriangleup}{H}$ 

 $\triangle S$ 

 $T_1$ 

 $P_1$ 

LT or HT

Ref

(continued on next page)

#### Table 1 (continued).

| No | Alloy   | $\triangle H$ | $\triangle S$ | T <sub>1</sub> | P <sub>1</sub> | LT or HT | Ref                      |
|----|---|---------------|---------------|----------------|----------------|----------|--------------------------|
|    |   | kJ/mol H2     | J/K/mol H2    | °C             | bar            |          |                          |
| 74 | CeNi <sub>4</sub> Cr  | 16.63         | 81.59         | 35             | 28.095         | LT       | Rusman and Dahari (2016) |
| 75 | CeNi <sub>3</sub> Cr <sub>2</sub>   | 14.55         | 75.31         | 35             | 29.729         | LT       | Rusman and Dahari (2016) |
| 76 | MNi <sub>5</sub>  | 20.92         | 96.65         | 35             | 32.219         | LT       | Kim et al. (1997)        |
| 77 | MNi <sub>5</sub>  | 20.92         | 96.77         | 35             | 32.705         | LT       | Huston (1980)            |
| 78 | V <sub>0.85</sub> Cr <sub>0.15</sub>  | 29.71         | 125.52        | 35             | 33.629         | LT       | Kim et al. (1997)        |
| 79 | Ti <sub>0.99</sub> Zr <sub>0.01</sub> V <sub>0.43</sub> Fe <sub>0.09</sub> Cr <sub>0.05</sub> Mn <sub>1.5</sub> | 20.25         | 95.15         | 35             | 34.939         | LT       | Weckerle et al. (2019)   |
| 80 | Ca <sub>0.2</sub> M <sub>0.8</sub> Ni <sub>5</sub>  | 24.27         | 108.75        | 35             | 37.376         | LT       | Huston (1980)            |
| 81 | Ca <sub>0.2</sub> M <sub>0.8</sub> Ni <sub>5</sub>  | 24.27         | 108.78        | 35             | 37.542         | LT       | Kim et al. (1997)        |
| 82 | CeNi <sub>5</sub>   | 22.18         | 111.71        | 35             | 120.821        | LT       | Kim et al. (1997)        |



**Fig. 3.** Coordinate points ( $\xi$ ,  $\eta$ ) for the applicable MH alloys and four straight lines at maximum and minimum temperatures of T<sub>h</sub> and T<sub>l</sub>, and constant temperature T<sub>m</sub>(=120°C).



**Fig. 4.** Coordinate points ( $\xi$ ,  $\eta$ ) for the applicable MH alloys and four straight lines at maximum and minimum temperatures of T<sub>h</sub> and T<sub>l</sub>, and constant temperature T<sub>m</sub>(=130°C).

be included and considered in the system energy calculation once the MH alloys are determined. The  $Cv_1$  and  $Cv_2$  are the specific heat capacity of MH alloys at constant volume for reactors MH1 and MH2 respectively. These MH alloy properties are important to calculate the energy inputs and outputs in the system but mostly are not available such that some modes of calculation correlations are necessarily generated. Henceforward, based on available data from literature, it is found that the specific heat capacity Cv is closely related to the molar mass of the MH alloy applied, as shown in Fig. 6. A linear correlation is therefore obtained to calculate the  $C_v$  with the function of molar mass of the MH alloy, if the data is not available:

$$C_v = 0.3995WM_{MH} + 33.287 \tag{13}$$

For this MHHP, the system efficiency is defined as coefficient of amplification (COA) and calculated as below:

$$COA = \frac{Q_{m1} + Q_{m2}}{Q_h}$$
(14)

Compared to conventional COP, the coefficient COA is of practical important for the specified application of hydride chemical heat pump (Grandjean et al., 1995). It should be noted that the LT heat source heat input  $Q_1$  is not taken into account in



**Fig. 5.** Coordinate points ( $\xi$ ,  $\eta$ ) for the applicable MH alloys and four straight lines at maximum and minimum temperatures of T<sub>h</sub> and T<sub>l</sub>, and constant temperature T<sub>m</sub>(=140°C).



Fig. 6. Correlation of specific heat capacity at constant volume with molar mass for metal hydride alloys.

the calculation of COA since it is conventionally exhausted into ambient. Supposing all the system processes are reversible, the total entropy production during the system operation will be zero such that the Carnot coefficient of amplification  $COA_c$  can be derived and calculated as:

$$COA_c = \frac{T_m(T_h - T_m)}{T_h(T_m - T_l)}$$
(15)

The system exergy efficiency  $\psi$  can therefore be calculated as the ratio of COA and COA<sub>c</sub>:

$$\psi = \frac{COA}{COA_C} \tag{16}$$

Based on the analysis results above, the applicable MH alloy pairs at heat output temperatures ( $T_m$ ) 130 °C and 140 °C are listed in Tables 2 and 3 respectively. In addition, some important parameters including COA, COA<sub>c</sub>,  $\psi$ , W<sub>1</sub>, W<sub>2</sub>, P<sub>h</sub>, P<sub>l</sub>, T<sub>h</sub> and T<sub>l</sub> are calculated and listed in each table, in which W<sub>1</sub> and W<sub>2</sub> are the weights of MH alloys charged in reactors MH1(MH1a or MH1b) and MH2 (MH2a or MH2b) respectively.

To evaluate and compare the system performance when different MH alloy pairs are applied, the variations of COA,  $COA_c$  and  $\psi$  with various MH alloy pairs at  $T_m$  temperatures of 130 °C and 140 °C are shown in Figs. 7 and 8 respectively. In addition, the

variations of hydrogen high and low pressures with various MH alloy pairs at  $T_m$  temperatures of 130 °C and 140 °C are shown in Figs. 9 and 10 respectively. For the heat pump application, the system is applicable only if its system efficiency COA is higher than one. In that case, for the temperatures  $T_m$  at 130  $^\circ$ C and 140 °C, respectively 24 and 8 MH alloy pairs can be applied. For the high and low hydrogen pressures, the low hydrogen pressures are acceptable since almost all the low pressures are below 30 bar. However, some of the high pressures are quite high with the values up to 150 bar which need to be considered in the manufacturer's ability, cost and operating safety. As seen from Tables 2 and 3 and Figs. 7-10, only two MH alloy pairs can be applicable for both temperatures of T<sub>m</sub> and acceptable COA values which are LaNi  $_{4.25}Al_{0.75}/Zr_{0.9}Ti_{0.1}Cr_{0.6}Fe_{1.4}$  (HT/LT) (pair number 6 in Table 2 and pair number 5 in Table 3) and LaNi 4.8Al<sub>0.2</sub>/ CeNi<sub>3</sub>Cr<sub>2</sub>(HT/LT) (pair number 23 in Table 2 and pair number 9 in Table 3). However, the high hydrogen pressure with LaNi<sub>4.8</sub>Al<sub>0.2</sub>/CeNi<sub>3</sub>Cr<sub>2</sub>(HT/LT) is about 126 bar while the high hydrogen pressure with LaNi<sub>4.25</sub>Al<sub>0.75</sub>/Zr<sub>0.9</sub>Ti<sub>0.1</sub>Cr<sub>0.6</sub>Fe<sub>1.4</sub> is below 30 bar. Therefore, from the system performance point of view, the MH alloy pair of LaNi<sub>4.25</sub>Al<sub>0.75</sub>/ Zr<sub>0.9</sub>Ti<sub>0.1</sub>Cr<sub>0.6</sub>Fe<sub>1.4</sub> is preferred.

| Pair no | o MH alloy pair  |  | COA   | COAc  | ψ     | $W_1$ | $W_2$ | Ph      | Pl     | T <sub>h</sub> | Tl    |
|---------|--|--|-------|-------|-------|-------|-------|---------|--------|----------------|-------|
|         | HT MH alloy  | LT MH alloy  | -     | -     | -     | kg    | kg    | bar     | bar    | °C             | °C    |
| 1       | LaNi <sub>4.6</sub> Al <sub>0.4</sub>                      | CeNi <sub>3</sub> Cu <sub>2</sub>  | 0.969 | 1.421 | 0.682 | 0.59  | 1     | 51.122  | 9.853  | 202.04         | 23.20 |
| 2       | LaNi <sub>4.5</sub> Al <sub>0.5</sub>                      | Ce <sub>1.1</sub> Ni <sub>2.5</sub> Cu <sub>2.5</sub>  | 1.005 | 1.538 | 0.653 | 0.395 | 1     | 35.947  | 6.789  | 198.44         | 44.36 |
| 3       | LaNi <sub>4.6</sub> Al <sub>0.4</sub>                      | CeNi 2.5Cu2.5  | 1.019 | 1.464 | 0.696 | 0.589 | 1     | 56.178  | 9.853  | 206.95         | 26.55 |
| 4       | CaNi <sub>5</sub>  | CeNi <sub>3</sub> Cu <sub>2</sub>  | 1.052 | 1.482 | 0.710 | 0.525 | 1     | 51.122  | 14.823 | 190.51         | 44.05 |
| 5       | LaNi <sub>4.7</sub> Al <sub>0.3</sub>                      | CeNi 2.5Cu2.5  | 1.110 | 1.499 | 0.741 | 0.441 | 1     | 56.178  | 15.518 | 188.77         | 48.06 |
| 6       | LaNi <sub>4.25</sub> Al <sub>0.75</sub>                    | Zr <sub>0.9</sub> Ti <sub>0.1</sub> Cr <sub>0.6</sub> Fe <sub>1.4</sub>  | 1.258 | 1.532 | 0.821 | 1.96  | 1     | 25.079  | 2.646  | 212.56         | 32.42 |
| 7       | LaNi <sub>4.30</sub> Mn <sub>0.70</sub>                    | ZrCr 0.6Fe <sub>1.4</sub>  | 1.289 | 1.608 | 0.802 | 0.714 | 1     | 15.660  | 1.926  | 206.03         | 46.54 |
| 8       | LaNi <sub>4.75</sub> Al <sub>0.25</sub>                    | Ti <sub>0.98</sub> Zr <sub>0.02</sub> V <sub>0.41</sub> Fe <sub>0.09</sub> Cr <sub>0.05</sub> Mn <sub>1.46</sub> | 1.306 | 1.572 | 0.831 | 2.13  | 1     | 105.369 | 18.880 | 210.21         | 39.29 |
| 9       | LaNi <sub>4.5</sub> Al <sub>0.5</sub>                      | Z r <sub>0.8</sub> Ti <sub>0.2</sub> Cr <sub>0.6</sub> Fe <sub>1.4</sub>   | 1.296 | 1.699 | 0.763 | 0.93  | 1     | 58.536  | 6.789  | 223.09         | 44.69 |
| 10      | LaNi <sub>4.7</sub> Al <sub>0.3</sub>                      | Ti <sub>0.98</sub> Zr <sub>0.02</sub> V <sub>0.41</sub> Fe <sub>0.09</sub> Cr <sub>0.05</sub> Mn <sub>1.46</sub> | 1.324 | 1.586 | 0.835 | 1.38  | 1     | 105.369 | 15.518 | 224.22         | 31.47 |
| 11      | LaNi <sub>4.5</sub> Al <sub>0.5</sub>                      | La <sub>0.6</sub> Y <sub>0.4</sub> Ni <sub>4.8</sub> Mn <sub>0.2</sub>   | 1.325 | 1.703 | 0.778 | 0.867 | 1     | 56.311  | 6.789  | 221.04         | 46.27 |
| 12      | LaNi <sub>4.56</sub> Mn <sub>0.44</sub>                    | La <sub>0.6</sub> Y <sub>0.4</sub> Ni <sub>4.8</sub> Mn <sub>0.2</sub>   | 1.326 | 1.685 | 0.787 | 0.698 | 1     | 56.311  | 6.342  | 221.70         | 44.15 |
| 13      | LaNi <sub>4.8</sub> Al <sub>0.2</sub>                      | Ti <sub>0.98</sub> Zr <sub>0.02</sub> V <sub>0.41</sub> Fe <sub>0.09</sub> Cr <sub>0.05</sub> Mn <sub>1.46</sub> | 1.357 | 1.569 | 0.865 | 1.25  | 1     | 105.369 | 23.342 | 198.23         | 48.21 |
| 14      | LaNi <sub>4.83</sub> Mn <sub>0.17</sub>                    | CeNi <sub>4</sub> Zr   | 1.441 | 1.611 | 0.894 | 3.85  | 1     | 140.580 | 22.112 | 218.26         | 38.39 |
| 15      | LaNi <sub>4.8</sub> Al <sub>0.2</sub>                      | CeNi <sub>4</sub> Zr   | 1.467 | 1.604 | 0.915 | 2.87  | 1     | 140.580 | 23.342 | 214.01         | 40.47 |
| 16      | LaNi <sub>4.61</sub> Mn <sub>0.26</sub> Al <sub>0.13</sub> | La <sub>0.6</sub> Y <sub>0.4</sub> Ni <sub>4.8</sub> Mn <sub>0.2</sub>   | 1.370 | 1.714 | 0.799 | 0.52  | 1     | 56.311  | 7.232  | 219.40         | 48.26 |
| 17      | LaNi <sub>4.61</sub> Mn <sub>0.26</sub> Al <sub>0.13</sub> | Z r <sub>0.8</sub> Ti <sub>0.2</sub> Cr <sub>0.6</sub> Fe <sub>1.4</sub>   | 1.340 | 1.710 | 0.784 | 0.56  | 1     | 58.536  | 7.232  | 221.47         | 46.68 |
| 18      | LaNi <sub>4.83</sub> Mn <sub>0.17</sub>                    | Ti <sub>0.98</sub> Zr <sub>0.02</sub> V <sub>0.41</sub> Fe <sub>0.09</sub> Cr <sub>0.05</sub> Mn <sub>1.46</sub> | 1.338 | 1.575 | 0.849 | 1.68  | 1     | 105.369 | 22.112 | 202.04         | 45.89 |
| 19      | LaNi <sub>4.8</sub> Al <sub>0.2</sub>                      | CeNi <sub>4</sub> Cr   | 1.342 | 1.477 | 0.909 | 2.50  | 1     | 129.697 | 23.342 | 209.49         | 26.44 |
| 20      | LaNi <sub>4.8</sub> Al <sub>0.2</sub>                      | Ti <sub>0.99</sub> Zr <sub>0.01</sub> V <sub>0.43</sub> Fe <sub>0.09</sub> Cr <sub>0.05</sub> Mn <sub>1.5</sub>  | 1.318 | 1.567 | 0.842 | 1.22  | 1     | 145.585 | 23.342 | 215.99         | 34.53 |
| 21      | LaNi <sub>4.56</sub> Mn <sub>0.44</sub>                    | Z r <sub>0.8</sub> Ti <sub>0.2</sub> Cr <sub>0.6</sub> Fe <sub>1.4</sub>   | 1.297 | 1.681 | 0.771 | 0.748 | 1     | 58.536  | 6.342  | 223.71         | 42.58 |
| 22      | LaNi <sub>4</sub> Al                                       | La <sub>0.6</sub> Y <sub>0.4</sub> Ni <sub>4.9</sub> Al <sub>0.1</sub>   | 1.302 | 1.563 | 0.833 | 3.7   | 1     | 14.921  | 1.521  | 221.31         | 46.60 |
| 23      | LaNi <sub>4.8</sub> Al <sub>0.2</sub>                      | CeNi <sub>3</sub> Cr <sub>2</sub>  | 1.301 | 1.417 | 0.919 | 2.713 | 1     | 125.899 | 30.032 | 207.85         | 35.55 |
| 24      | LaNi <sub>4</sub> Al                                       | ZrCr 0.6Fe <sub>1.4</sub>  | 1.177 | 1.564 | 0.752 | 2     | 1     | 15.660  | 1.078  | 223.38         | 29.19 |
| 25      | LaNi <sub>4.7</sub> Al <sub>0.3</sub>                      | CeNi <sub>3</sub> Cu <sub>2</sub>  | 1.062 | 1.452 | 0.731 | 0.444 | 1     | 51.122  | 15.518 | 183.89         | 46.57 |
| 26      | LaNi <sub>4.61</sub> Mn <sub>0.26</sub> Al <sub>0.13</sub> | Ce <sub>1.1</sub> Ni <sub>2.5</sub> Cu <sub>2.5</sub>  | 1.014 | 1.546 | 0.655 | 0.234 | 1     | 35.947  | 7.232  | 196.62         | 46.94 |
| 27      | LaNi <sub>4.65</sub> Mn <sub>0.35</sub>                    | CeNi 2.5Cu2.5  | 1.016 | 1.447 | 0.702 | 0.538 | 1     | 56.178  | 9.641  | 204.62         | 25.59 |
| 28      | LaNi <sub>4.56</sub> Mn <sub>0.44</sub>                    | Ce <sub>1.1</sub> Ni <sub>2.5</sub> Cu <sub>2.5</sub>  | 0.984 | 1.524 | 0.645 | 0.313 | 1     | 35.947  | 6.342  | 199.60         | 41.62 |

#### Table 3

Applicable MH alloy pairs for  $T_m\text{=}140~^\circ\text{C}.$ 

| Pair no | MH alloy pair                           |   | COA   | COAc  | $\psi$ | $W_1$ | $W_2$ | Ph      | $P_1$  | T <sub>h</sub> | $T_1$ |
|---------|---|---|-------|-------|--------|-------|-------|---------|--------|----------------|-------|
|         | HT MH alloy                             | LT MH alloy   | -     | _     | -      | kg    | kg    | bar     | bar    | °C             | °C    |
| 1       | LaNi <sub>4.65</sub> Mn <sub>0.35</sub> | CeNi <sub>3</sub> Cu <sub>2</sub>                                       | 0.954 | 1.405 | 0.679  | 0.54  | 1     | 57.100  | 12.669 | 205.44         | 35.69 |
| 2       | LaNi <sub>4.6</sub> Al <sub>0.4</sub>   | CeNi <sub>3</sub> Cu <sub>2</sub>                                       | 0.956 | 1.421 | 0.673  | 0.59  | 1     | 57.100  | 12.816 | 207.81         | 36.29 |
| 3       | LaNi <sub>4.65</sub> Mn <sub>0.35</sub> | CeNi 2.5Cu2.5   | 1.026 | 1.447 | 0.709  | 0.538 | 1     | 63.472  | 12.669 | 210.83         | 38.08 |
| 4       | LaNi <sub>4.6</sub> Al <sub>0.4</sub>   | CeNi 2.5Cu2.5   | 1.030 | 1.464 | 0.703  | 0.589 | 1     | 63.472  | 12.816 | 213.47         | 38.63 |
| 5       | LaNi <sub>4.25</sub> Al <sub>0.75</sub> | Zr <sub>0.9</sub> Ti <sub>0.1</sub> Cr <sub>0.6</sub> Fe <sub>1.4</sub> | 1.139 | 1.532 | 0.743  | 1.96  | 1     | 29.740  | 3.644  | 220.22         | 43.32 |
| 6       | LaNi <sub>4.83</sub> Mn <sub>0.17</sub> | CeNi <sub>4</sub> Cr  | 1.310 | 1.482 | 0.884  | 3.35  | 1     | 146.246 | 28.372 | 220.57         | 35.47 |
| 7       | LaNi <sub>4.8</sub> Al <sub>0.2</sub>   | CeNi <sub>4</sub> Cr  | 1.288 | 1.477 | 0.873  | 4.95  | 1     | 146.246 | 30.032 | 216.25         | 38.20 |
| 8       | LaNi <sub>4.83</sub> Mn <sub>0.17</sub> | CeNi <sub>3</sub> Cr <sub>2</sub>                                       | 1.260 | 1.422 | 0.887  | 3.65  | 1     | 125.899 | 28.372 | 211.93         | 32.49 |
| 9       | LaNi <sub>4.8</sub> Al <sub>0.2</sub>   | CeNi <sub>3</sub> Cr <sub>2</sub>                                       | 1.245 | 1.417 | 0.879  | 5.41  | 1     | 125.899 | 30.032 | 207.85         | 35.55 |
| 10      | LaNi <sub>4.75</sub> Al <sub>0.25</sub> | CeNi <sub>3</sub> Cr <sub>2</sub>                                       | 1.240 | 1.419 | 0.874  | 4.62  | 1     | 125.899 | 24.261 | 220.38         | 24.35 |
| 11      | Fe <sub>0.8</sub> Ni <sub>0.2</sub> Ti  | CeNi 2.5Cu2.5   | 0.996 | 1.412 | 0.705  | 0.464 | 1     | 63.472  | 10.655 | 212.62         | 30.05 |
| 12      | Fe <sub>0.8</sub> Ni <sub>0.2</sub> Ti  | CeNi <sub>3</sub> Cu <sub>2</sub>                                       | 0.922 | 1.373 | 0.672  | 0.465 | 1     | 57.100  | 10.655 | 207.61         | 26.98 |



Fig. 7. Variation of COA, COA<sub>c</sub> and  $\psi$  with different alloy pair numbers for T<sub>m</sub>=130 °C.



Fig. 8. Variation of COA, COA<sub>c</sub> and  $\psi$  with different alloy pair numbers for T<sub>m</sub>=140 °C.



Fig. 9. Variation of high and low hydrogen pressures with different alloy pair numbers for T<sub>m</sub>=130 °C.



Fig. 10. Variation of high and low hydrogen pressures with different alloy pair numbers for  $T_m$ =140 °C.

#### 3.3. System performance prediction

Based on the thermodynamic and operation analyses, the MH alloy pair LaNi\_{4.25}Al\_{0.75}/ Zr\_{0.9}Ti\_{0.1}Cr\_{0.6}Fe\_{1.4}(HT/LT) is determined

for the proposed MHHP system. The system performance at different design and operating conditions can therefore be predicted. To simply the process, the effect of hysteresis on the MH absorption and desorption pressures at the same temperature is



Fig. 11. Variation of high and low heat source temperatures  $(T_h \text{ and } T_l)$  with heat output temperature  $T_m$ .



Fig. 12. Variation of high and low heat source temperatures  $(T_h \text{ and } T_l)$  with heat output temperature  $T_m$ .

neglected. In addition, it is assumed that there is no temperature difference between heat source or sink temperature with its corresponding MH temperature. Nevertheless, effects of MH reactor heat capacity and hydrogen pressure difference for hydrogen transport through each MH rector pair are considered in the performance prediction. The metal material for each MH reactor is assumed as stainless steel and the meal reactor weight is assumed as 50% of its corresponding MH alloy charged. Since the weights of MH alloys in reactors MH1 and MH2 are 1.96 kg and 1 kg respectively, the corresponding reactor metal weights are 0.98 kg and 0.5 kg each. The hydrogen pressure difference between hydrogen transport through each MH rector pair on either high or low pressure side is assumed as 2 bar to facilitate the hydrogen transport. Accordingly, the variations of high and low temperature heat source temperatures  $T_h$  and  $T_l$  with heat output temperature T<sub>m</sub> are calculated and shown in Fig. 11. It is seen from the prediction, the T<sub>h</sub> and T<sub>l</sub> both increase linearly with higher heat output temperature T<sub>m</sub>. This indicates that to obtain a higher heat output temperature, both heat source temperatures of T<sub>h</sub> and T<sub>l</sub> need to be increased. Correspondingly, the variations of hydrogen pressures at those four reactors Ph, Pm2, Pm1 and  $P_{l}\xspace$  with heat output temperature  $T_{m}\xspace$  are calculated and shown in Fig. 12. Similarly, the high and low side hydrogen pressures both increase with higher heat output temperature although the increase rates of the high side hydrogen pressures ( $P_h$  and  $P_{m2}$ )

are relatively higher. This implies that the maximum MH reactor pressure should be considered at design stage based on the applicable maximum heat output temperature in the system. On the other hand, the system efficiencies in terms of COA<sub>c</sub>, COA and  $\psi$  can be calculated at varied heat output temperatures as shown in Fig. 13. As depicted, the COA<sub>c</sub> decreases with increased heat output temperature while the COA decreases slightly with higher heat output temperature. Subsequently the exergy efficiency  $\psi$  increases somewhat with the amplified heat output temperatures.

At constant heat output temperature  $T_m$  at 140 °C, the variations of low temperature heat input  $Q_l$ , heat output  $Q_m$  and system cycle time with high temperature heat input  $Q_h$  are calculated and demonstrated in Fig. 14. As depicted, both low temperature heat input  $Q_l$  and heat output  $Q_m$  increase with higher high temperature heat input  $Q_h$ . Meanwhile, the system cycle time decreases rapidly at the beginning and slows down a bit with the increased high temperature heat input. This indicates that at a designed heat output temperature, the heat output capacity, system cycle time and low temperature heat input can be controlled by the high temperature heat input.

#### 4. Conclusions

There are plenty of low grade waste heat from industries which can be recovered and converted to useful heat for district



**Fig. 13.** Variation of COAc, COA, and  $\Psi$  with heat output temperature T<sub>m</sub>.



Fig. 14. Variation of low temperature heat input  $Q_{l}$ , heat output  $Q_{m}$  and cycle time with high temperature heat input  $Q_{h}$ .

heating network with the technology of metal hydride (MH) heat pump (MHHP). The MHHP has several advantages compared with other heat pump technologies. However, one of the important tasks to utilise this technology in the industrial waste heat recovery is to find out the appropriate MH alloys for the system. Therefore, in this paper, a detailed MH alloy selection procedures are explained for the proposed high temperature MHHP system. Of the total available MH alloys, an efficient method is proposed to classify the applicable high and low temperature MH alloys based on the lowest hydrogen operation temperature and its corresponding pressure. A number of MH alloy pairs can therefore be formed, and each MH pair consists of one high temperature alloy and one low temperature alloy. For these MH alloy pairs, thermodynamic analysis is conducted based on thermodynamic equilibrium in the system and specified operating conditions. The applicable MH pairs are therefore figured out for each designed heat output temperature. It is found that the higher the designed heat output temperature, the less the applicable MH pairs. Thereafter, operation analysis is carried out to evaluate and compare the system energy and exergy efficiencies and operating pressures at specified heat output temperatures. Meanwhile, a correlation to calculate alloy specific heat capacity at constant volume based on its molar mass is obtained which is quite useful for the operation analysis. The MH alloy pair for the proposed MHHP system is thus identified and finalised. The system performance is then predicted at various heat output temperatures and high temperature heat inputs. The predicted results can be applied for the optimal system designs and operation controls.

#### **Declaration of competing interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Acknowledgement

The authors would like to acknowledge the support received from Research Councils UK (RCUK, EP/T022760/1) for this research project.

#### References

Anon, 2014. Element Energy- The potential for recovering and using surplus heat from industry. Final Report for DECC.

- Bjurstrom, H., Suda, S., 1989. The metal hydride heat pump: dynamics of hydrogen transfer. Int. J. Hydrogen Energy 14, 19–28.
- D. Chandra, D., Reilly, J.J., Chellappa, R., 2006. Metal hydrides for vehicular applications: The state of the art. JOM 58, 26–32.
- Dantzer, P., Orgaz, E., 1986. Thermodynamics of hydride chemical heat pump-II. How to select a pair of alloys. Int. J. Hydrogen Energy 11, 797–806.

- Gamnini, M., 1989. Performance of metal hydride heat pumps operation under dynamic conditions. Int. J. Hydrogen Energy 14, 821–830.
- George, K., Cordin, A., Panagiotis, N., Stefan, B., 2020. Techno-economic analysis of high-temperature heat pumps with low-global warming potential refrigerants for upgrading waste heat up to 150 C. Energy Convers. Manage. 226, 113488.
- Grandjean, F., Long, G.J., Buschow, K.H.J., 1995. Interstitial Intermetallic Alloys. Springer Netherlands, p. 728.
- Huston, E.L., 1980. Engineering properties of metal hydrides. J. Less-Common Metals 74, 435–443.
- Kim, K.J., Feldman Jr., K.T., Lloydt, G., Razanit, A., 1997. Compressor-driven metal-hydride heat pumps. Appl. Therm. Eng. 17, 551–560.
- L. Li, L., Ge, Y.T., Luo, X., Tassou, S.A., 2017. Experimental investigations into power generation with low grade waste heat and R245fa organic rankine cycles (ORCs). Appl. Therm. Eng. 115, 815–824.
- Lee, S.G., Kim, Y.K., Lee, J.Y., 1995. Operating characteristics of metal hydride heat pump using Zr-based laves phases. Int. J. Hydrogen Energy 20, 77–85.
- Linder, M., Kulenovic, R., 2011. An energy-efficient air-conditioning system for hydrogen driven cars. Int. J. Hydrogen Energy 36, 3215–3221.
- Linder, M., Laurien, E., 2009. Thermally driven sorption machine for fast hydrogen exchange. In: Proceedings of hydrogen and hydrogen storage – methods and materials. H3-2009, Indian Institute of Science, Bangalore, India, pp. 3–6.
- Lototskyy, M.V., Tolj, I., Davids, M., Yevgeniy, V., Parsons, A., Swanepoel, D., et al., 2016. Metal hydride hydrogen storage and supply systems for electric forklift with low-temperature proton exchange membrane fuel cell power module. Int. J. Hydrogen Energy 41, 13831–13842.
- Mellouli, S., Askri, F., Dhaou, H., Jemni, A., Nasrallah, S.B., 2009. Parametric studies on a metal hydride cooling system. Int. J. Hydrogen Energy 34, 3945–3952.
- Muthukumar, P., Groll, M., 2010. Metal hydride based heating and cooling systems: A review. Int. J. Hydrogen Energy 35, 3817–3831.

- Nakamura, H., Nakamura, Y., Fujitani, S., Yonezu, I., 1997. A method for designing a hydrogen absorbing laNi5-x-ymnxaly alloy for a chemical refrigeration system. J. Alloys Compd. 252, 83–87.
- Ni, J., Liu, H., 2007. Experimental research on refrigeration characteristics of a metal hydride heat pump in auto air-conditioning. Int. J. Hydrogen Energy 32, 2567–2572.
- Patsos, A., 2010. Port Talbot Exergy Mapping and waste heat recovery opportunities. Project Report 150552, Corus Research, Development & Technology.
- Payá Herrero, J., 2010. Modelling and analysis of a metal hydride cooling system. (Ph.D. thesis). Valencia.
- Qin, F., Chen, J., Lu, M., Chen, Z., Zhou, Y., Yang, K., 2007. Development of a metal hydride refrigeration system as an exhaust gas-driven automobile air conditioner. Int. J. Hydrogen Energy 32a, 2034–2052.
- Qin, F., Chen, J., Lu, M., Chen, Z., Zhou, Y., Yang, K., 2007b. Development of a metal hydride refrigeration system as an exhaust gas-driven automobile air conditioner. Renew. Energy 32, 2034–2052.
- Rusman, N., Dahari, M., 2016. A review on the current progress of metal hydrides material for solid-state hydrogen storage applications. Int. J. Hydrogen Energy 41, 12108–12126.
- Satheesh, A., Muthukumar, P., 2010. Performance investigations of a single-stage metal hydride heat pump. Int. J. Hydrogen Energy 35, 6950–6958.
- Skripnyuk, V.M., Ron, M., 1999. Evaluation of kinetics by utilizing the normalized pressure dependence method for the alloy ti<sub>0.95</sub>zr<sub>0.05</sub>mn<sub>1.48</sub>v<sub>0.43</sub>fe<sub>0.08</sub>al<sub>0.01</sub>. J Alloys Compd 293–295, 385–390.
- Weckerle, C., Bu rger, I., Linder, M., 2019. Numerical optimization of a plate reactor for a metal hydride open cooling system. Int. J. Hydrogen Energy 44, 16862–16876.
- Yasuda, N., Tsuchiya, T., Okinaka, N., Akiyama, T., 2013. Application of metal hydride sheet to thermally driven cooling system. Int. J. Hydrogen Energy 38, 7469–7476.